Adsorption of Methyl Iodide on Reduced Silver-Functionalized Silica Aerogel: Kinetics and Modeling

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Abstract

The low concentration methyl iodides (CH₃I) adsorption process on reduced silver-functionalized silica aerogel (Ag⁰-Aerogel) was studied. The kinetic data were acquired using a continuous flow adsorption system. Because the corresponding physical process was observed, the shrinking core model (SCM) was modified and applied. An average CH₃I pore diffusivity was calculated, the CH₃I-Ag⁰-Aerogel reaction was identified as a 1.37 order reaction instead of first order reaction, and the nth order reaction rate constant was determined. This modified SCM significantly increases the accuracy of adsorption behavior prediction at low adsorbate concentration. Modeling results indicate that the overall adsorption process is controlled by the pore diffusion. However, at low adsorbate concentration (<100 ppbv), the CH₃I adsorption is limited to the surface reaction due to the low uptake rate in a predictable time period.

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Topical Heading

Separations: Materials, Devices and Processes

Keywords

Adsorption, iodine removal, separation, silver aerogel, shrinking core model

Introduction

Nuclear power has been widely used since the $20^{\rm th}$ century for its low emission rate of air pollutants.¹⁻³ However, multiple radioactive isotopes, including radioactive Iodine (129 I), are produced in the uranium fission.^{4,5} During aqueous reprocessing of the nuclear waste, 85 Kr, 14 C, 129 I, and 3 H are released to the offgas streams. The off-gas streams include dissolver off-gas (DOG), cell off-gas (COG), waste off-gas (WOG) and vessel off-gas (VOG).⁶ According to Bruffey et al.^{6,7}, approximately 95% - 98% of iodine is contained in DOG, remaining iodine (in I₂ and organic iodides form) exists in VOG, and VOG flow rate is $100 \times$ higher than that of DOG. Therefore, unlike the ppm level in DOG, the iodine concentration in VOG decreases to below 100 ppbv. Although only trace amount of iodine exists in VOG, the off-gas cannot be emitted directly into atmosphere, and the emissions are governed by 10 CFR 20, 40 CFR 61 and 40 CFR 190.⁸⁻¹⁰ The composition of the organic iodides existing in VOG varies from methyl iodide (CH₃I) to iodododecane (C₁₂H₂₅I) and among 12 different organic iodides, CH₃I and C₁₂H₂₅I were reported to be the two most abundant components.^{6,11,12}

Multiple silver containing materials, including macroreticular resins, silver impregnated alumina (AgA), silver exchanged faujasite (AgX), hydrogen-reduced silver exchanged mordenite (Ag⁰Z) and reduced silver-functionalized silica aerogel (Ag⁰-Aerogel), have been developed and studied for I₂ and organic iodides adsorption. The reason for selecting silver-containing materials over traditional liquid scrubbing methods is concluded to be stronger Ag-I bond and solid form, therefore, higher removal efficiency and lower operation cost. Along these silver-containing materials, Ag⁰Z and Ag⁰-Aerogel have been studied continuously in US national laboratories and universities for their high iodine removal efficiency and relatively greater resistance to aging caused by potential contaminants in VOG and DOG (NO_x, water vapor, air). Nan et.al^{16,19} have conducted the single layer adsorption experiments of I₂ on Ag⁰Z and reported approximately 12 wt% I₂ adsorption capacity at 423K. Deep-bed adsorption of I₂ and CH₃I on Ag⁰Z at both ppb and ppm level have been studied by Jubin et al. Along et al. Bruffey et al. Along et al. Bruffey e

Deep-bed Ag⁰-Aerogel adsorption experiments of CH₃I and I₂ under the VOG conditions were conducted in multiple US national laboratories. Strachan et al.²⁷ performed 4.2 ppmv I₂ adsorption experiments at 150 , concluding that fresh Ag⁰-Aerogel was able to remove I₂ for at least 99.99% efficiency and observing that Ag⁰-Aerogel changed from black to a brown, earth-tone color during the adsorption experiment. Soelberg and Watson^{28,29} conducted I₂ adsorption on Ag⁰Z and Ag⁰-Aerogel at 150 with NO_x and H₂O present, with I₂ concentration ranging from 2 to 370 ppmv. Their results indicated, at similar conditions, Ag⁰-Aerogel obtained higher resistance to NO_x than Ag⁰Z did and, therefore, showed higher removal efficiency in deep-bed adsorption experiments. In addition, deep-bed CH₃I adsorption studies have also been conducted by Bruffey and Jubin⁷, Jubin et al.¹⁴ and Soelberg and Watson¹⁷. Ag⁰-Aerogel showed an adequate capability to adsorb CH₃I at various conditions such as ppb or ppm level concentrations and with or without the presence of NO_x. The penetration depth of CH₃I in the column was measured to be 3-7 cm, depending on the CH₃I and NO_x concentration; and the decontamination factor (DF), defined as inlet concentration of desired adsorbed species (eg. I₂ and CH₃I) over outlet concentration, can reach approximately 1000.

The detailed organic iodides-Ag reaction mechanism was not conclusive. Scheele et al.³⁰ proposed several possible reactions between Ag and CH_3I in Ag^0Z :

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In these proposed reactions, organic compounds are generated in gas form and only iodine is captured by silver. The generated CH_3OCH_3 (dimethyl ether) and CH_3OH (methanol) were observed by Soelberg and Watson²⁵ and the desorption of C_2H_6 in similar reactions was suggested by Zhou et al³¹. With the presence of NO_x in the gas stream, other organic compounds such as CH_3NO_2 (nitromethane) and C_3H_9NO (3-amino1-propanol) were also detected.²⁶ Assuming similar reactions happen between Ag^0 -Aerogel and CH_3I and only iodine is left in Ag^0 -Aerogel pellets, the maximum iodine capture capacity for I_2 should be the same as that for CH_3I .

Limited by the nature of deep-bed adsorption experiments, the mass of deep-bed adsorption column cannot be measured continuously and most of the curves were composed by discrete data points instead of real-time data. Therefore, as complements to the deep-bed adsorption experiments, single-layer CH_3I adsorption experiments on Ag^0 -Aerogel were conducted in the present work. One of the purposes of performing the single-layer adsorption experiments is determining the pore diffusivity and reaction rate constant and these parameters can be related and applied for column adsorption modeling. $^{32-34}$

In the single-layer adsorption experiments, Ag^0 -Aerogel was placed in a tray connected to a microbalance, enabling real-time and high-precision measurement of the mass change. The CH_3I concentrations selected were 113, 266, 1130 and 10400 ppbv; temperature was 150, same as the experiments described above; and gas flow rate was set to be 500 sccm in order to satisfy 1.1 m/s superficial gas velocity suggested by Nan et al.¹⁹ The adsorption kinetic data at various CH_3I concentrations were obtained and used to evaluate the pore diffusivity and reaction rate of CH_3I in Ag^0 -Aerogel. To explain the inconsistency of reaction rate constants at different concentrations, an n^{th} -order shrinking core model was applied and the modeling results were used to improve the predictions of adsorption behavior at various CH_3I concentrations.

Materials and Methods

Silver-Functionalized Silica Aerogel

Reduced silver-functionalized silica aerogel (Ag⁰-Aerogel) was obtained from the Pacific North National Laboratory (PNNL) in 2017. It was first developed there for gaseous iodine capturing in nuclear waste treatment.^{35,36} The Ag⁰-Aerogel pellets are primarily black; the shape and size are arbitrary and some of the pellets contain certain yellow areas which may be due to unevenly coated silver in the manufacturing process. The particle radius is approximately 0.1 cm. Reported by Jubin et al.¹⁴, the bulk density of the pellet is $0.54~\rm g/cm^3$ and $0.62~\rm g/cm^3$ for 'as-received material' and 'post-run material' respectively. For the modeling work to be discussed in the following sections, an average value of $0.58~\rm g/cm^3$ was used. The maximum iodine loading capacity reported ranged from 33 to 47 wt%^{27,29,37}. To achieve accurate modeling results, the iodine loading capacity was measured to be approximately 37 wt% using the continuous flow adsorption system.

Continuous Flow Adsorption System

The continuous flow adsorption system was used for iodine and water vapor adsorption on multiple materials previously by Nan et al. 19,38,39 and Lin et al. 40,41 and has been modified for performing the adsorption of CH₃I on Ag⁰-Aerogel experiments. Figure 1 shows the schematic diagram of the modified adsorption system.

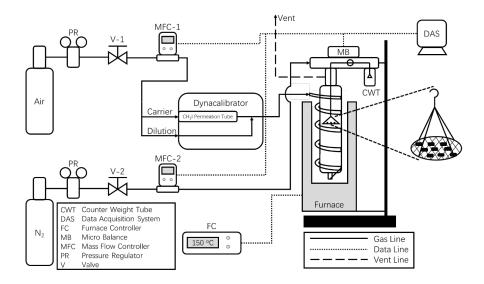


Figure 1. Schematic diagram of the continuous flow CH₃I adsorption system

Dry air flowed through Dynacalibrator (VICI, Model 500), in which a permeation tube (VICI) was placed, as the carrier gas to generate CH_3I . The CH_3I concentration was controlled by the specific permeation tube model and the temperature of the permeation chamber. 500 sccm of gas mixture was preheated to 150 in the preheating coil wound around the adsorption column and then sent to the adsorption column (I.D.= 30 mm). In the adsorption column, one layer of Ag^0 -Aerogel pellets was placed on a tray and suspended under the microbalance. The microbalance has a variance of approximately 30 μ g and a sensitivity of 0.1 μ g. When the CH_3I vapor was absorbed by Ag^0 -Aerogel pellets, mass change was measured by the microbalance and saved by the data acquisition system. During the adsorption process, the temperature was controlled by the furnace controller and N_2 was used as the protective gas for the microbalance system.

Modeling

Multiple gas-solid adsorption models have been used in explaining adsorption kinetics of I_2 and Organic Iodides including Linear Driving Force Model (LDFM), Shrinking Core Model (SCM), Volume Reaction Model (VRM) and Pore Diffusion Model (PDM). $^{16,18,38,42-46}$ I_2 adsorption on Ag^0Z has been identified as the shrinking core process because the core shrinkage was observed by Nan. $^{16}Shown$ in Figure 2, a similar process was observed in CH_3I adsorption on Ag^0 -Aerogel by cutting a partially reacted pellet in half. The yellow area is the reacted Ag^0 -Aerogel and the black area is the unreacted core. Therefore, the shrinking core model was selected to model the adsorption kinetics.



Figure 2. Shrinking core process observed in CH₃I adsorption on Ag⁰-Aerogel, two cut halves of a partially reacted pellet

SCM was developed by Yagi and Kunii⁴⁷ in 1955 and modified by Levenspiel⁴⁸. It consists of a gas film diffusion term, pore diffusion term and reaction term. In a typical SCM gas-solid adsorption process, the adsorbate first reaches the pellet surface by diffusing through a gas film around the pellet. Then, the gas reacts with the adsorbent surface. When the adsorbent surface is fully reacted, the adsorbate diffuses into the pellet and reacts with the second layer of the adsorbent. Because the size of the unreacted core decreases as the adsorption proceeds, the model is named as 'shrinking core'. This model has been widely used in the nuclear waste treatment area including water adsorption on molecular sieves $3A^{40}$, water adsorption on $Ag^0Z^{16,38}$, I_2 adsorption on $Ag^0Z^{16,19}$, CH_3I adsorption on Ag^0Z^{18} , etc.

SCM relates the time and adsorption mass by using 3 parts shown in Eq. 1:

where q is average sorbate (CH₃I) concentration (mol/g) at time t (s) and q_e is equilibrium sorbate (CH₃I) concentration (mol/g). For convenience, q and q_e are sometimes represented as 'mass uptake' and 'equilibrium mass uptake/adsorption capacity' in wt%, which can be easily converted by the CH₃I molar mass. τ_I , τ_2 , and τ_3 are gas film diffusion term, pore diffusion term, and 1st order reaction term respectively. By assuming gas-solid reaction is 1st order, τ_I , τ_2 , and τ_3 can be calculated by Eq. 2,3 and 4

where R_a is radius of the pellet (cm), ρ_{π} is density of the pellet (g/cm³), C_b is bulk adsorbate (CH₃I) concentration (mol/cm³), k_f is gas film mass transfer coefficient (cm/s), D_p is pore diffusivity (cm²/s), k_s is 1st order reaction rate constant (cm/s) and b is stoichiometric coefficient of Ag in Ag-CH₃I reaction, which is 1.

To improve the SCM, the unnecessary 1st order reaction assumption may be replaced by the nth order reaction, which τ_1 and τ_2 remain the same and τ_3 is replace by nthorder reaction term τ_3^* given in Eq. 5:

where n is reaction order and k_s^* is nthorder reaction rate constant $((cm/s)[?](mol/cm^3)^{1-n})$

To reduce the variables to be fitted in the model and increase the accuracy of the result, an alternative method of determining k_f was used by Nan. $^{16,19}k_f$ can be determined using Eq. 6 - 9. $^{49-52}$

Sh, Sc, and Re are Sherwood number, Schmidt number, and Reynolds number respectively. D_{AB} is the binary diffusion coefficient (cm²/s), T is temperature (K), P is pressure (bar), M_{AB} is the average molecular weight of species A, CH_3I , and species B, air, and ν is the atomic diffusion volume (cm³). For current

experimental condition, T = 423 K, P = 1 bar, $M_{AB} = 48.12 \text{ g/mol}$, $= 52.63 \text{ cm}^3 \text{ and} = 19.7 \text{ cm}^3$. The D_{AB} determined using this method is approximately 0.196 cm²/s, which is similar to the value of 0.207 cm²/s measured experimentally by Matsunaga et al.⁵³

Procedure description

As mentioned above, the CH₃I concentration in VOG is below 100 ppb. Measuring mass adsorbed at such low concentrations is beyond the capability of microbalances. More specifically, the mass uptake cannot be detected confidently by using microbalances in an acceptable time frame. Therefore, the CH₃I concentrations used for adsorption were selected to be 113, 266, 1130 and 10400 ppbv. Other experimental conditions such as temperature and gas flow rate are selected base on previous studies. 150 / 423K was reported as the preferred experiment temperature for I₂and CH₃I adsorption and has been widely used in multiple studies. ¹⁶⁻¹⁸ The gas flow rate may impact the adsorption rate by varying superficial gas velocity and therefore changing k_f . Nan et al. ¹⁹indicated that no obvious impact was observed at 423 K for superficial velocity greater than 1.1 m/min. To satisfy this condition, the gas flow rate measured at room temperature is set to be approximately 500 cm³/min. To prevent any significant concentration gradient caused by overlapping, one layer of Ag⁰-Aerogel pellets (0.1-0.2 g) was placed in the tray suspended under the microbalance, shown in Figure 1.

At ppb level concentration, the adsorption rate of $\mathrm{CH_{3}I}$ is significantly lower than that of ppm level adsorption. Therefore, the pellets must be dried carefully to prevent any misleading result caused by moisture loss during the $\mathrm{CH_{3}I}$ adsorption. Over 150 h is required to air-dry $\mathrm{Ag^{0}}$ -Aerogel, in other words, placing in the tray and flow dry air (Dew Point = -70) until no mass loss is observed. To accelerate this process, the $\mathrm{Ag^{0}}$ -Aerogel was vacuum dried at 150 overnight using the degas function of a Surface Area and Porosity Analyzer (Micromeritics, ASAP 2020) and stored under $\mathrm{N_{2}environment}$ before conducting the adsorption experiments.

Unlike previous 10-50 ppm level adsorption studies 16,18,19 , reaching equilibrium is not practicable at ppb level. For example, based on experimental results and predictions, it may take over 3 years for Ag⁰-Aerogel to reach equilibrium at 1130 ppbv CH₃I condition. Therefore, the adsorption experiments were stopped after a certain period instead of reaching equilibrium.

Results

Adsorption Kinetics

Four adsorption experiments with 113, 266, 1130 and 10400 ppbv CH₃I in dry air were conducted. The concentrations were calculated from the data provided by the permeation tube manufacturer and confirmed by measuring the mass differences of the permeation tubes before and after the experiments. Approximately 288 hours adsorption data of 113, 266, 1130 and 10400 ppbv CH₃I adsorption on Ag⁰-Aerogel are plotted in Figure 3. For 288 hours, mass uptakes reached 0.17, 0.91, 3.7 and 14.7 wt% at 113, 266, 1130 and 10400 ppbv respectively. To eliminate the physically adsorbed CH₃I, the Ag⁰-Aerogel was left in the adsorption column and desorbed by stopping CH₃I generation and flowing only dry air for 24 h. During this desorption process, no significant mass losses were observed, indicating CH₃I adsorption on Ag⁰-Aerogel was mostly chemisorption. Limited by the low mass uptake, 113 and 266 ppbv adsorption curve cannot be identified well in Figure 3 and a close view of 4 uptake curves is shown in Figure 4.

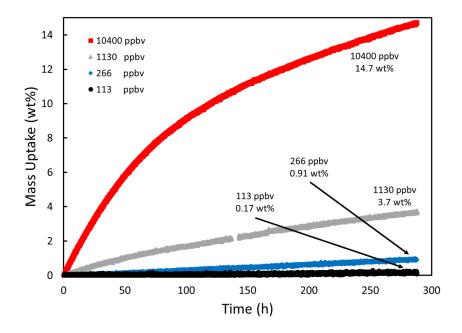


Figure 3. Uptake curves of 113, 266, 1130 and 10400 ppbv ${\rm CH_3I}$ adsorptions on ${\rm Ag^0}$ -Aerogel for up to 288 hours.

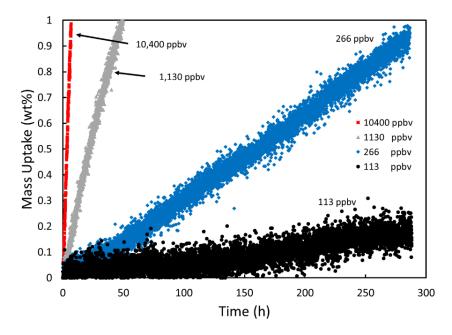


Figure 4. Closer view of uptake curves of 113, 266, 1130 and 10400 ppbv ${\rm CH_3I}$ adsorptions on ${\rm Ag^0}$ -Aerogel for up to 288 hours.

Model Fitting Result

The 1st order SCM was used to fit the kinetic data to determine D_p and k_s in Eq. 3 and 4. To average the weights of different sections in the adsorption curves and increase the accuracy of data fitting, t 's were rescaled by \log_{10} before applying the least square regressions. More specifically, was used instead of , which f is Eq. 1-4, subscript i is the number of experimental data and exp is the indication of experimental data.

The model-fitting results and parameters are shown in Table 1. k_f , calculated theoretically to be 5.99 cm/s by applying Eq. 6-9, kept constant at 4 different concentrations; D_p and k_s were determined in model fitting and AARD is calculated using , where model indicates model fitting result and N is the number of data points.

Concentration (ppbv)	$\begin{array}{c} {\rm Concentration} \\ {\rm (mol/cm3)} \end{array}$	$k_f ({ m cm/s})$	$D_p \ (\mathrm{cm}^2/\mathrm{s})$	$k_s \text{ (cm/s)}$	AARD~(%)
113 266 1130 10400 *Calculated theoretically **Not determined	4.64×10^{-12} 1.09×10^{-11} 4.64×10^{-11} 4.27×10^{-10} *Calculated theoretically **Not determined	5.99* 5.99* 5.99* 5.99*	N/A^{**} 4.50×10^{-4} 4.70×10^{-4} 4.56×10^{-4}	5.43×10^{-2} 1.45×10^{-1} 2.28×10^{-1} 3.53×10^{-1}	12.75 0.27 1.02 0.26

Table 1. Parameters and results of SCM fitting.

 D_p 's were determined to be 4.50×10^{-4} , 4.70×10^{-4} and 4.56×10^{-4} for 266, 1130 and 10400 ppbv respectively. For 113 ppbv CH₃I adsorption, limited by the nature of low CH₃I concentration, D_p was not determined. As discussed previously, at low concentration, the CH₃I has not consumed all Ag on the surface of Ag⁰-Aerogel pellet during the test time frame and therefore no significant pore diffusion was observed. The average D_p was $4.59\pm0.102\times10^{-4} {\rm cm}^2/{\rm s}$. Different from 3 similar D_p 's, k_s 's increase from 5.43×10^{-2} cm/s at 113 ppbv to 3.53×10^{-1} cm/s at 10400 ppbv. The concentration-dependent k_s is highly questionable. Theoretically, for a given reaction, the k_s only depends on temperature and shall not change with the reactant concentration. ⁵⁴ Therefore, the orderly changed k_s indicates an nth order reaction instead of the assumed 1st order.

Discussion

Nth Order Shrinking Core Model

The nth order SCM cannot be used directly to fit an adsorption curve because $k_s^* C_b^n$ term in Eq. 5 contains two variables $(k_s^* \& n)$ and one constant (C_b) . There exists an unlimited amount of combinations to yield the desired value. Instead, k_s^* and n were determined by plotting k_s (cm/s) and C_b (mol/cm³) using Eq. 10 and 11.

The reaction order and nth order reaction constant were determined using Figure 5 and shown in Table 2. For CH₃I-Ag⁰-Aerogel adsorption system, n=1.37 and $k_s^*=1287$ (cm/s)[?](mol/cm³)¹⁻ⁿ. As mentioned earlier, the SCM results can be applied to deep-bed adsorption analysis. However, keeping the nth order reaction assumption may introduce certain difficulties in calculations. Therefore, Eq. 10 can be rewritten as Eq. 12 to calculate the nth-order-compensated, concentration-dependent pseudo k_s 's (cm/s).

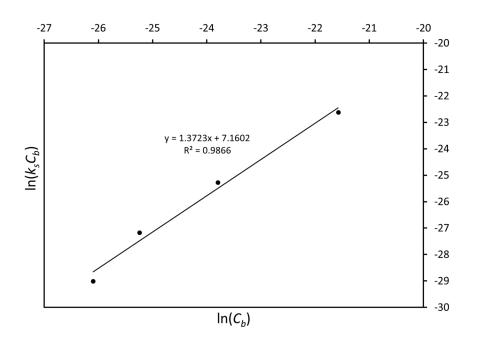


Figure 5. Reaction order plot, $\ln(C_b)$ vs. $\ln(k_s C_b)$

Concentration (ppbv)	$C_b(\mathrm{mol/cm}^3)$	$k_s \text{ (cm/s)}$	$\ln(k_s C_b)$	$\ln(C_b)$	$pseudo k_s (cm/s)$
113	4.64×10^{-12}	5.43×10^{-2}	-29.01	-26.10	7.76×10^{-2}
266	1.09×10^{-11}	1.45×10^{-1}	-27.17	-25.24	1.07×10^{-1}
1130	4.64×10^{-11}	$2.28{ imes}10^{-1}$	-25.27	-23.79	1.83×10^{-1}
10400	4.27×10^{-10}	$3.53{ imes}10^{-1}$	-22.62	-21.57	4.18×10^{-1}
n = 1.37					
$k_s^* = 1287 \text{ (cm/s)}[?](\text{mol/cm}^3)^{1-\text{n}}$	$k_s^*=1287 \text{ (cm/s)}[?](\text{mol/cm}^3)^{1-\text{n}}$				

Table 2. Parameters and results of determining reaction order

The reason for this fractional order reaction between CH₃I and Ag⁰-Aerogel is not determined yet. This fractional-reaction order was also observed in other silver-containing materials. Zhou and White⁵⁵ suggested that the desorption of organic products from Ag(111) surface changes the reaction order and Robb and Harriott⁵⁶ indicated that the diffusion limitation in supported silver catalysts does. Therefore, the fractional reaction order maybe not only caused by the specific reaction mechanism but also the physical process.

Nth Order SCM Examination and Application

The effectiveness of the nth order SCM can be demonstrated by comparing predictions made by the nth order SCM and 1st order SCM with $averagek_s$, which the $average\ k_s=0.195$ cm/s was calculated by averaging 4 k_s 's directly. Figure 6 shows the prediction of 113 ppbv CH₃I adsorption behavior generated by using nth order SCM and 1st order SCM with $averagek_s$. Comparing with 1st order SCM with $average\ k_s$, the nth order SCM decreases AARD by approximately 175%. The mass uptakes in 288 hours predicted by using nth order SCM and 1st order SCM with $average\ k_s$ were 0.24 wt% and 0.59 wt% respectively, where the measured mass uptake is approximately 0.17 wt%.

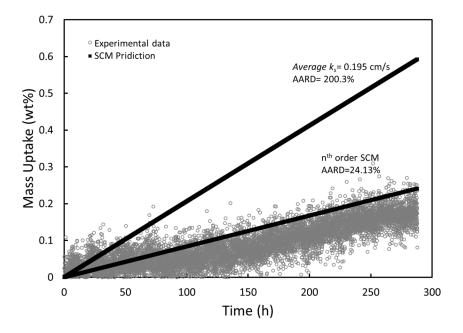


Figure 6. 113 ppbv CH₃I on Ag⁰-Aerogel, SCM prediction using nth order SCM and 1st order SCM with average k_s .

With the developed nth order SCM, the adsorption behavior can be predicted more accurately. Figure 7 shows the predicted behavior of 113, 266, 1130 and 10400 ppbv CH₃I adsorption on Ag⁰-Aerogel at 150 using nth order SCM. The capacity loss caused by dry air aging effect was not considered, which means $q_e = 37$ wt% or 2.9×10^{-3} mol/g, and other parameters are $k_f = 5.99$ cm/s, $D_p = 4.59 \times 10^{-4}$ cm²/s, n = 1.37 and k_s * = 1287 (cm/s)[?](mol/cm³)¹⁻ⁿ. Based on the results, for CH₃I adsorption on Ag⁰-Aerogel at 150 reaching equilibrium, 19K days are required at 113 ppbv condition, 7.6K days at 266 ppbv, 1.6K days at 1130 ppbv and 170 days at 10400 ppbv.

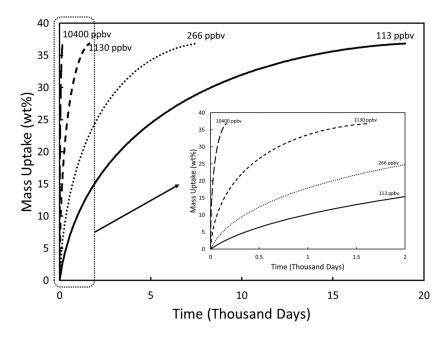


Figure 7. 113, 266, 1130 and 10400 ppby CH₃I adsorption behavior prediction using nth order SCM

Rate-Controlling Step

For further analysis and application of the SCM results, it is necessary to understand the rate-controlling step of the process. To determine how the CH₃I-Ag⁰-Aerogel adsorption is controlled, τ_1 , τ_2 , and τ_3 at 4 different concentrations were calculated using Eq 2-4 with the determined parameters shown in Table $1.\tau_1$, τ_2 , and τ_3 are the partial adsorption equilibrium time contributed by the gas film diffusion, pore diffusion, and reaction term. More straightforwardly, the equilibrium time, t_{eq} , can be expressed as $t_{eq} = \tau_1 + \tau_2 + \tau_3$. For the SCM, the control term can be represented by overall resistance ratio, τ_1 / t_{eq} , where i=1,2, or $3.^{38}$ Figure 8 shows the resistance contributions of pore diffusion term and reaction term, whereas the gas film diffusion term is less than 1% and not shown in the figure. It was found that the reaction resistance contribution decreases from 25% at 113 ppbv to 6% at 10400 ppbv and the pore diffusion resistance contribution increases accordingly. Generally, for a given adsorption system, the resistance contribution is independent of the concentration of the adsorbate. Therefore, the change shown in Figure 8 is due to the n^{th} order reaction which has been discussed previously.

The adsorption rate is determined by the process with the highest resistance. Visualized from Figure 8, the pore diffusion contributes the most among the gas film diffusion, pore diffusion, and reaction term, especially for high CH₃I concentration. Therefore, the CH₃I-Ag⁰-Aerogel adsorption is identified as an 'overall' diffusion-controlled process. The overall process is diffusion-controlled, but at certain conditions, the process may not be controlled by diffusion, which will be discussed in the following section. Moreover, as the concentration decreased from 10400 to 113 ppbv, the ratio of reaction resistance contribution increases significantly, indicating that the CH₃I-Ag⁰-Aerogel adsorption may change from a pore diffusion-controlled to a reaction-controlled process if the concentration decreases substantially.

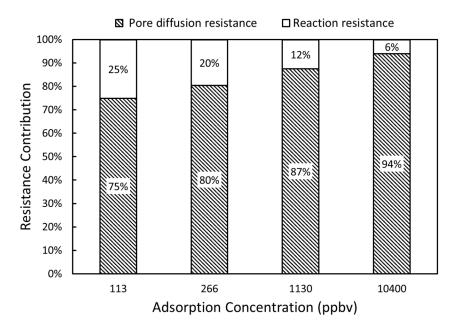


Figure 8. Resistance contributions of pore diffusion and reaction terms for CH_3I-Ag^0 -Aerogel adsorption at 113, 266, 1130 and 10400 ppbv.

Although the overall process is controlled by the pore diffusion of CH₃I, at VOG conditions, the rate determining step may vary because of the actual adsorption process. As mentioned above, in the VOG stream,

the CH₃I concentration is lower than 100 ppbv, more dilute than the low boundary of the current work, and the adsorption rate is extremely low. For example, at 113 ppbv, the prediction shows that the adsorption may not reach equilibrium in approximately 50 years if the capacity loss is neglected. Therefore, the actual active regions are only the initial parts of the adsorption curves. These regions correspond to the surface reaction between CH₃I and Ag⁰-Aerogel, which are highly reaction-controlled. In this process, CH₃I reacts with Ag on the surface of Ag⁰-Aerogel and only a limited amount of CH₃I diffuses into the pellets. Quantitatively speaking, at VOG conditions, the q/q_e term in Eq. 1 is much smaller than 1 and by specifying the q/q_e values, the real-time contributions of diffusion term and reaction term can be calculated. For example, as Figure 9 shows, at 113 ppbv, the reaction term contributes approximately 62% at $q/q_e = 0.2$ or q = 7.4 wt%, which approximately 600 days are required to reach this point. Additionally, within one year, the reaction term contribution is higher than 93% and the mass uptake is below 0.74 wt%. Therefore, it is important to notice that although the overall adsorption process is controlled by the pore diffusion, at actual VOG conditions, the effect of pore diffusion to the uptake rate is minor in at least 1-2 years. To determine the CH₃I-Ag⁰-Aerogel adsorption behavior at low concentration conditions, the analysis should focus on the reaction rate instead of pore diffusivity.

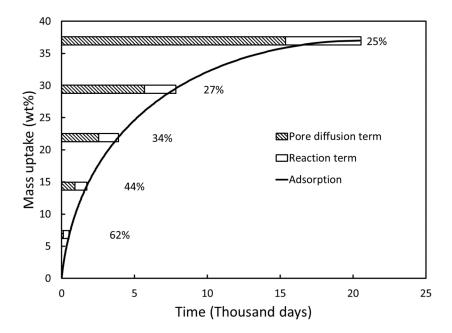


Figure 9. Real-time contribution of reaction term and pore diffusion term in CH₃I-Ag⁰-Aerogel adsorption at 113 ppbv (percentage represents reaction contribution).

Because the adsorption behavior at low concentration minorly depends on gas film diffusion and pore diffusion term, the SCM in Eq. 1 can be reduced to Eq. 13 and the mass uptake rate is given in Eq. 14.

Since at the initial region, $t<<\tau_3$, Eq. 14 can be written as Eq. 15 for ${\bf n}^{\rm th}$ order reaction.

Furthermore, by replacing R_a and ρ_{π} , Eq. 15 becomes,

where A is the specific surface area (cm²/g) of the material. This result indicates that at VOG conditions, the initial part, the only region need be considered, of nth order SCM reduces to a simple nth order surface reaction with a constant uptake rate, which can be demonstrated by 113 and 266 ppbv adsorption curves in Figure 3 and Figure 4. However, to increase the adsorption efficiency, simply increasing the surface area by reducing the diameter may not be applicable. The surface reaction condition may not hold due to the change of flow regime caused by fine pellets.

Conclusion

The kinetic data of $\mathrm{CH_{3}I}$ adsorption on $\mathrm{Ag^{0}}$ -Aerogel at 150 were obtained using the continuous flow adsorption system. The $\mathrm{CH_{3}I}$ concentrations were 113, 266, 1130 and 10400 ppbv. Because the corresponding shrinking core process was observed, the shrinking core model was applied to determine the gas film diffusivity, pore diffusivity and reaction rate constant. The 1st order reaction was originally assumed. The well-agreed pore diffusivities were determined in three of the total four trails. The average value was 4.59 \pm 0.102 \times 10⁻⁴ cm²/s. Orderly increasing reaction rate constants were observed and, therefore, the modified nth order SCM was selected for analysis.

The reaction order of CH₃I-Ag⁰-Aerogel adsorption was calculated to be approximately 1.37 and the reaction rate constant was approximately 1287 (cm/s)[?](mol/cm³)¹⁻ⁿ. This nth order SCM effectively increases the accuracy of adsorption behavior prediction. Using nth order SCM instead of 1st order SCM, the AARD of 113 ppbv adsorption behavior prediction decreases from 200.3% to 24.13%. Furthermore, the overall adsorption behaviors at 113, 266, 1130 and 10400 ppbv were predicted. It requires more than 50 years for Ag⁰-Aerogel reach to equilibrium at 113 ppbv condition if the capacity loss due to dry air aging effects is not considered.

The rate-controlling step of CH_3 -Ag⁰-Aerogel adsorption was identified by plotting the resistance of different rate-dependent terms. Although the overall adsorption process is controlled by pore diffusion, the surface reaction between CH_3I and Ag is more crucial at VOG conditions. The nature of low concentration in VOG streams ($C_b < 100$ ppbv) limits the adsorption from a full nth order SCM to a surface reaction. To increase the adsorption efficiency, decreasing the size of pellets is a theoretically applicable method. However, the detailed solution still requires further studies in deep-bed adsorption. As replacing the 1st order SCM by nth order SCM, the accuracy of adsorption behavior prediction at VOG conditions was increased significantly. The parameters determined can be widely applied to the deep-bed adsorption system design of the off-gas treatment in the nuclear fuel reprocessing process.

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