1 **Improving Discharge Predictions in Ungauged Basins: Harnessing the Power of**

2 **Disaggregated Data Modeling and Machine Learning**

3

4 Aggrey Muhebwa[1], Colin J. Gleason[2], Dongmei Feng[3] and Jay Taneja[1]

5 [1]Department of Electrical and Computer Engineering, University of Massachusetts, Amherst, MA, USA

6 [2]Department of Civil and Environmental Engineering, University of Massachusetts Amherst, MA, USA

7 [3]Department of Chemical and Environmental Engineering, University of Cincinnati, Ohio, USA

8

9 **Abstract**

10 Current machine learning methods for discharge prediction often employ aggregated basin-wide

11 hydrometeorological data (lumped modeling) for parametric and non-parametric training. This

12 approach may overlook the spatial heterogeneity of river systems and their impact on discharge

13 patterns. We hypothesize that integrating temporal-spatial hydrologic knowledge into the data

14 modeling process (distributed/disaggregated modeling) can improve the performance of discharge

15 prediction models. To test this hypothesis, we designed experiments comparing the performance of

16 identical Long Short-Term Memory Recurrent Neural Network (LSTM-RNN) models forced with

17 either lumped or distributed features. We gather meteorological forcing and static attributes for the

18 Mackenzie basin in Canada- a large and unique basin. Importantly, discharge performance is

19 assessed out-of-sample with k-fold replication across gauges. Results reveal a 9.6% improvement in

20 the mean Nash-Sutcliffe Efficiency (NSE) and a 4.6% improvement in mean Kling-Gupta

21 Efficiency (KGE) when LSTMs are trained with distributed information. Notably, the models

22 exhibit consistently unbiased predictions, with a negligible relative bias (RBias ≈ 0.0) across all

23 predictions. These experiments and results demonstrate the importance of integrating topologically

24 guided geomorphologic and hydrologic information (distributed modeling) in data-driven discharge

25 predictions.

26

27 **Plain Language**

28 Accurate river discharge prediction is critical for sustainable water resource management and

29 effective flood mitigation. Traditional methods often treat the entire river basin as a homogenous

30 unit, neglecting crucial hydrologic and hydrometeorological variations that significantly impact water

31 flow across different locations. This "lumped" approach can lead to inaccurate predictions. We

32 propose a "distributed" modeling approach incorporating detailed information about the river

basin's spatial heterogeneity. Applying this method to the Mackenzie River, a vast and complex river system in Canada, resulted in significantly more accurate discharge predictions compared to traditional lumped models. This confirms the critical importance of considering the river basin's spatial variability for better understanding and predicting water flow dynamics. Our work paves the way for enhanced water management strategies and improved flood preparedness by providing more precise and reliable discharge predictions.

Main Points

1. Current Machine Learning models rely on aggregated hydrometeorological data, ignoring the spatial heterogeneity inherent in river systems.
2. Incorporating topological-guided spatiotemporal hydrologic data can improve understanding of discharge dynamics within the river basin.

1. Introduction

The hydrologic cycles that generate river discharge are stochastic, complex, and non-deterministic systems characterized by processes and events whose dynamics depend on various direct (e.g., meteorological and environmental factors) and indirect (e.g., human interactions) inter-connected phenomena (Dimitriadis et al., 2021; Zounemat-Kermani et al., 2021). This complexity ensures that in situ monitoring via gauges is the best way to understand rivers: a direct measurement is best. However, continuous in situ monitoring of global rivers is challenging due to logistical difficulties, expense, and politics (Hannah et al., 2011; Wu et al., 2016; Gleason & Hamdan, 2017). Despite these challenges, the importance of monitoring river discharge cannot be overstated, as it aids in detecting climatic and environmental changes across time and space.

As a result of these challenges, process-based hydrology models are often deployed to estimate river discharge. Process-based models are rapidly scalable to different hydro-meteorological conditions and can explain and interpret underlying model performance. However, they are highly dependent on their calibrated parameters, which can degrade significantly when applied to rivers with different average discharges, seasonal variations, river widths, and geographical characteristics (e.g., Wagener et al., 2011; Arsenault et al., 2014; Pool & Seibert, 2021). This is important for modeling discharge in remote and developing regions where many assumptions must be made to achieve accurate predictions (Marshall et al., 2005; Thyer et al., 2009; Clark et al., 2016; Pilz et al., 2020). The needs and benefits of process-based models are an especially circular problem in ungauged basins between

64 the need for robust models to replace gauges and the need for more gauged data to calibrate them.

65 Watershed regionalization techniques such as spatial calibration, interpolation, and regression of

66 basin and hydro-meteorological characteristics are often used to adopt these models and their

67 parameters to ungauged basins (Hrachowitz et al., 2013; Pagliero et al., 2019; Belvederesi et al.,

68 2022). Finally, models can simulate future projections based on physically realistic processes, i.e.,

69 'what if' scenarios (Montanari & Koutsoyiannis, 2012; Basijokaite & Kelleher, 2021; Mai et al., 2022).

70 This is especially important given the expected increase in the intensity and frequency of

71 hydrological extremes due to climate change (Shrestha et al., 2021; Leng, Tang, and Rayburg, 2015;

72 Tabari, 2020).

73 Despite their widespread adaptation and credibility in hydrology, process-based models have several

74 limitations that hinder their ability to fully capture the complexities of real-world hydrologic systems.

75 First, the dominant physical processes that govern water movement and transformation within a

76 watershed exhibit significant temporal-spatial heterogeneity, reflecting variations in fluvial,

77 geomorphological, and soil characteristics (Kirchner, 2006; McDonell et al., 2007; Sidle et al., 2017;

78 Royall, 2021). This heterogeneity challenges the development of a single model structure that

79 adequately represents all interacting processes across the diverse landscapes encountered in natural

80 watersheds. Second, equifinality - the ability of multiple parameter settings to produce similar model

81 outputs - obscures a proper process-based understanding of models with many parameters, making

82 it difficult to discern the proper combination of underlying mechanisms responsible for hydrologic

83 responses. Third, the limited spatial and temporal scales at which process-based models are typically

84 developed and calibrated constrain their ability to effectively represent fast-evolving temporal-spatial

85 variability in physical processes across different scales (Yoshida et al., 2022; Clark et al., 2015a,

86 Clark2015b; Clark, 2016). This limitation hinders their applicability in assessing and predicting

87 hydrologic response under changing climate and land-use scenarios. To address these limitations,

88 modelers must incorporate heterogeneity and temporal-spatial variability of physical processes into

89 their models or use remote sensing to gather more primary data (e.g., Oubanas et al., 2018; Xie et al.,

90 2021; Tsai et al., 2021).

91 Therefore, gauges are the best means of monitoring rivers, but they are impractical to deploy

92 globally. Hydrologic models and remote sensing are excellent tools, whether used separately or in

93 combination, but they have unique challenges, especially in ungauged basins. How, then, can we best

94 combine the richness of primary data with process-based hydrologic knowledge and sparse in situ

95 data? We argue the answer can be found in machine learning (ML). Early ML studies (e.g., Hsu et al.,

96 1995) demonstrated the ability of feed-forward networks to outperform calibrated process-based

97 models in predicting discharge across flow regimes. Recent studies (e.g., Ouyang et al., 2021; Feng et

98 al., 2020; Feng 2021; Ma et al., 2021; Kratzert et al., 2019a; Kratzert2019b) have shown that Long

99 short-term memory (LSTM) artificial neural networks can outperform process-based models in

100 ungauged basins. Transfer learning (e.g., Zhuang et al., 2020; Tan et al., 2018; Long et al., 2017;

101 Zamir et al., 2018; Ma et.al, 2021), which is analogous to regionalization (Kittel et al., 2020; Wang et

102 al.,2021; Yang et al., 2020; Oudin et al., 2008), also shows promise in tuning ML models to well-

103 measured basins and applying them to ungauged basins. At its core, ML for hydrology involves the

104 automatic discovery of inherent temporal-spatial patterns in historical hydrological data. While

105 current ML approaches have demonstrated improved streamflow predictions, they still have several

106 limitations. First, ML models, especially deep learning models, are still relatively non-interpretable,

107 meaning we can produce accurate streamflow hydrographs without knowing how or why they were

108 produced or which combinations of hydrological processes improved the model's learning process.

109 However, ML is moving toward improved interpretability (e.g., Marcinkevič & Vogt, 2020;

110 Lundberg et al., 2017; Lundberg, 2020; Wanner et al., 2020; Lees et al., 2021), but for now, it

111 remains a powerful predictive tool that often divides opinions in the traditionally process-based

112 discipline of hydrology. Second, ML models are complex and require access to specialized

113 computing, such as GPU clusters. Third, ML models typically require much more training data with

114 stricter consistency requirements than hydrologists are used to working with: the amount of data

115 needed for quality ML training far outstrips the amount needed to calibrate a model or remote

116 sensing technique (Mastorakis, 2018; D'Amour et al., 2020; Seifert & Rasp, 2020).

117 Current ML for hydrology retrofits ML techniques to hydrological data. However, we argue that

118 aspects of hydrologic modeling and remote sensing for hydrology can be easily implemented in an

119 ML-driven hydrology framework to move toward a more hydrologically aware and purpose-built

120 ML for the discipline. For instance, hydrologists have long known that distributed modeling—where

121 inputs are spatiotemporally heterogeneous - outperforms lumped modeling - where inputs are

122 spatiotemporally homogeneous (Baroni et al., 2019; Ntegeka et al., 2014; Fry & Maxwell, 2018; Tran

123 et al., 2018; Muhammad et al., 2019; Dembele et al., 2020). Yet almost all previous ML in hydrology

124 has been lumped modeling. Moving to distributed ML would allow known correlations between

125 altitude and temporal-spatial variation in isotopic signatures of snowmelt, glacier melt, and rainwater

126 to express themselves in the predictions (Immerzeel et al., 2010; Pokhrel et al., 2018; Scown et al.

127 2020; Fujita et al., 2008; Nepal et al. 2014; Pant & Semwal, 2021). This shift would require changes

128   to the input structure of ML models, but it should improve them considerably. Further, since ML

129   requires huge quantities of training data, remotely sensed inputs are the best way of obtaining this

130   needed primary data in ungauged basins (Gleason and Durand, 2020) in conjunction with globally

131   available climate model output currently used in ML-driven hydrology modeling (e.g., Larnier &

132   Monnier 2020; Ma et al., 2021; Feng et al., 2020; Asanjan et al., 2018; Kratzert et al., 2019; Kratzert

133   2019b; Ouyang et al., 2021).

134   Therefore, we compare the impact of aggregating LSTM training data over the entire upstream basin

135   (lumped modeling) against separating upstream basin information based on the Strahler River order

136   system (distributed modeling) while holding the LSTM architecture and input data constant. This

137   tests the hypothesis that creating a distributed LSTM model based on topologically organized

138   geomorphologic and hydrologic information can improve discharge estimation performance in

139   ungauged basins. We demonstrate this comparison in ungauged basins by training generalizable

140   machine learning models in hydrologically similar basins to validation zones in ungauged basins. We

141   also compare results to previously published LSTMs and a recent remotely sensed data assimilation

142   product (Feng et al., 2021). Ultimately, we aim to show how tenets of hydrologic modeling improve

143   ML in ungauged basins.

144   **2. Data and Methods**

145   **2.1. Data**

146   We tested our proposed ML approach on the Mackenzie basin (Figure 1). This basin covers

147   approximately 1.8 million square kilometers and encompasses various climatic conditions, including

148   mountainous, cold temperate, subarctic, and arctic zones. The Mackenzie River drains approximately

149   one-fifth of Canada's total land area, including the Rocky and Mackenzie mountains and the

150   Canadian Shield. It contains over 39,000 river reaches in the MERIT Basin River network (Lin et al.,

151   2019), developed on the MERIT HYDRO topography data (Aziz and Burn, 2006; Yamazaki et al.,

152   2019). We selected a subset (n = 69) of all gauge stations in the Mackenzie basin, limited to those

153   with at least ten years of consistent daily gauge data available from Environment and Climate

154   Change Canada (ECCC). These gauge data formed the basis of training and validation for our work.
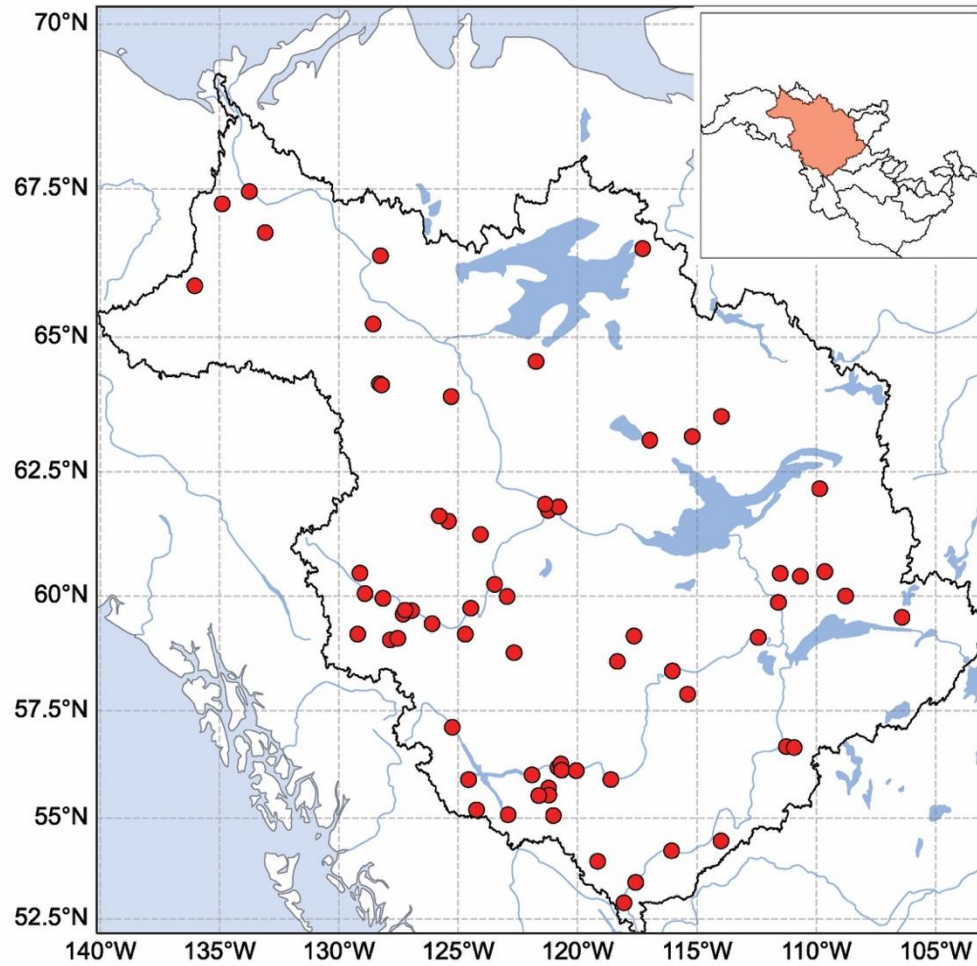
155

156　Figure 1: A Map showing the location of gauge stations (red circles) in the Mackenzie basin used in the study. Inset shows a map of

157　the 20 biggest basins in Canada, including the Mackenzie Basin (shaded).

158　Our training data include both static and dynamic variables. Static variables, such as bed slope,

159　sinuosity, and stream length, do not change over a few decades. Dynamic features, on the other

160　hand, reflect changing hydrologic processes. We gathered daily data from 1981 to 2010, including

161　simulated discharge and runoff from the GRADES database (Lin et al., 2019), reach averaged widths

162　obtained from the Global Long-term river Width (GLOW) database (Feng et al., 2022), and climate

163　model data. Climate data were from the Global Land Data Assimilation System (GLDAS)-2.1 model

164　(Rodell et al., 2014; Beaudoing and Rodell, 2019) and included three hourly climate data gridded at

165　0.25 x 0.25 degrees resolution, which were downsampled to daily data. These data were downloaded

166　from the Google Earth Engine platform (Gorelick et al., 2017). Previous studies have shown that

167　stationary data are relatively easy to model with ML (e.g., Hosking, 1984; Dickey and Pantula, 1987).

168　Appendix A lists all variables used in this study.

169   We include river width as one of the input features for all models used in this study. Previous studies

170   have shown that river width has a strong correlation with river discharge (Gleason and Smith, 2014;

171   Gleason et al., 2014; Hagemann et al., 2017; Brinkerhoff et al., 2019; Feng et al., 2019; Feng et al.,

172   2021). However, Landsat-derived river widths are only available at best every 16 days, considering

173   cloud cover and seasonality. This is not a problem for hydrological approaches, but long short-term

174   memory (LSTM) models require training data without gaps (e.g., Bengio and Gingras, 1995; Che et

175   al., 2018; Lim et al., 2021). Therefore, we impute a complete width record from the Landsat

176   observations in the GLOW dataset (Feng et al., 2022). Imputation is a statistical process of

177   determining and assigning replacement values for missing or invalid data points in a multivariate

178   dataset by leveraging possible correlations between covariates (Buck, 1960; Jamshidian and Mata,

179   2007). Thus, we estimated missing width values using a regression model fitted with the remaining

180   covariates in the dataset. We chose this imputation approach to retain river widths as a strong

181   predictor of discharge.

182   To compare lumped and distributed ML approaches, we trained and tested our models only at

183   gauges with at least five upstream reaches. This ensured that we had sufficient data to quantify the

184   impact of upstream climatology factors on daily discharge at a given gauge station. We also limited

185   our selection to gauges with at least ten years of daily discharge data. Preliminary tests indicated that

186   this was the scale of data needed to train an LSTM model accurately without overfitting (Ying,

187   2009). Finally, we selected Strahler River orders with at least four gauge stations: order 4 (25 gauge

188   stations), order 5 (23 gauge stations), order 6 (13 gauge stations), order 7 (4 gauge stations), and

189   order 8 (4 gauge stations). This gave us a total of 69 gauge stations.

190

191   **2.2.   Sequential Learning Via LSTMs**

192   Our ML models are based on the LSTM model architecture. This artificial neural network,

193   introduced by Hochreiter and Schmidhuber in 1997, excels at processing sequential data, a hallmark

194   of hydrometeorological and hydrologic time series. LSTMs have demonstrated remarkable success in

195   diverse applications, including language modeling, video understanding, music transcription, and,

196   crucially, discharge prediction for hydrology (e.g., Eck and Schmidhuber, 2002; Srivastava et al.,

197   2015; Ghosh et al., 2016; Ouyang et al., 2021; Feng et al., 2020; Kratzert et al., 2019). Unlike

198   standard neural networks that solely capture the spatial context of data, LSTMs are uniquely

199   equipped to extract temporal and spatial information embedded within the training data (e.g., Yin et

200   al., 2017; Wu and Prasad, 2017).

201   This ability to grasp the intricate interplay of spatial and temporal dynamics is paramount for

202   accurately modeling hydrological processes. Structurally, an LSTM network comprises a series of

203   identical recurrent neural networks, each building upon the information passed from its predecessor.

204   This cascading architecture enables LSTMs to handle the sequential context inherent in historical

205   data, particularly in hydrologic time series. Unlike traditional RNNs, LSTMs possess an inherent

206   memory mechanism that allows them to retain information over extended periods, effectively

207   overcoming the vanishing gradient problem (Chung et al., 2014; Hu et al., 2018). This memory

208   capability empowers LSTMs to capture long-term temporal dependencies, where desired outputs

209   depend on inputs presented far in the past (lookback window). This capability is critical for

210   modeling physical processes unfolding at varying spatial resolutions, a characteristic of hydrological

211   phenomena. Consequently, the lookback window size dictates how much information a model can

212   learn about a particular physical process at any given time.

213   The LSTM network architecture can be implemented in either a unidirectional or bidirectional

214   fashion (Graves & Schmidhuber, 2005; Siami-Namini et al., 2019; Fraiwan & Alkhodari, 2020).

215   Unidirectional LSTMs process and encode features in a forward manner, sequentially learning

216   information from each feature at each timestep $t = \{t[0], t[1], t[2], …, t[n]\}$. However, they only

217   utilize information from preceding timesteps (t_i-1) to enhance prediction at the current timestep (t_i).

218   This unidirectional approach limits the model's ability to capture dependencies between features and

219   information encoded in subsequent timesteps ($t+1$).
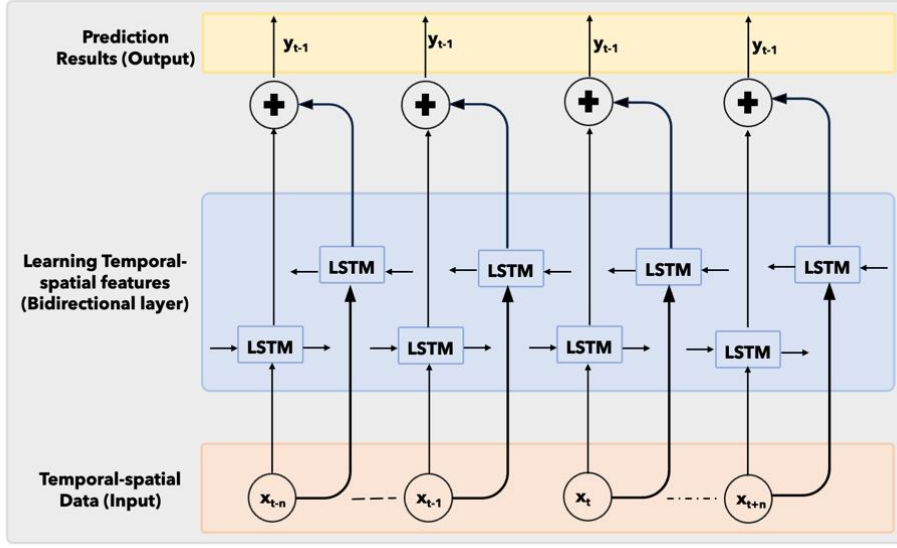
220

221

Figure 2: An architectural overview of a Bidirectional Long Short-Term Memory (Bi-LSTM) Network for time series prediction, showcasing the flow of temporal-spatial data through LSTM units in both forward and backward directions to enhance feature learning and improve prediction accuracy.

In contrast, bidirectional LSTMs combine two unidirectional LSTMs operating in opposite directions, as shown in Figure 2. The core LSM equations, shared by both forward and backward passes, are summarized as follows:

Forget gate: $f_t = \sigma\big(W_f \cdot [h_{prev}, x_t] + b_f\big)$ (1)

Input gate: $i_t = \sigma\big(W_i \cdot [h_{prev}, x_t] + b_i\big)$ (2)

Candidate state: $\tilde{C}_t = tanh\big(W_c \cdot [h_{prev}, x_t] + b_C\big)$ (3)

Cell state update: $C_t = f_t * C_{prev} + i_i * \tilde{C}_t$ (4)

Output gate: $o_t = \sigma\big(W_\circ \cdot [h_{prev}, x_t] + b_0\big)$ (5)

Hidden state update: $h_t = o_t * tanh(C_t)$ (6)

Where x_t is the input at timestep t, h_{prev} and C_{prev} are the previous hidden and cell states, respectively. Furthermore, the final output at each timestep t, represented as y_t, in a Bidirectional LSTM is the concatenation of the forward and hidden states represented as $y_t = \big[h_t^{(f)}; t_t^{(b)}\big]$. Finally, for the forward pass, $h_{prev} = h_{t-1}^{(f)}$ and $C_{prev} = C_{t-1}^{(f)}$ while for the backward pass, $h_{prev} = h_{t+1}^{(b)}$ and $C_{prev} = C_{t+1}^{(b)}$.

240   This architecture enables the model to learn encoded features forward and backward, simultaneously

241   processing information from past and future timesteps. This bidirectional approach is particularly

242   advantageous in hydrological modeling, where river discharge at the next timestep (t_i+1) can provide

243   valuable context for improving prediction at the current timestep (t_i). For instance, knowledge of

244   future rainfall patterns can inform the model about potential changes in river discharge.

245   Additionally, Bi-directional LSTMs have demonstrated superior prediction accuracy, efficiency, and

246   stability in various applications (e.g., Ma et al., 2021; Atef and Eltawil, 2020; Siami-Namini, et al.,

247   2019; Althelaya et. al., 2018), underscoring their versatility and effectiveness in handling diverse

248   time-series data, robustness to noise, and long-term trends than uni-directional LSTMs. Finally, the

249   structure of Bi-LSTMs offers more opportunities to improve performance through epochs and

250   hyperparameter tuning. Recognizing the importance of this bidirectional relationship, we employed

251   the bidirectional LSTM network architecture for our experiments.

252   To mitigate overfitting and enhance model generalizability, we employed several strategies.

253   Regularization techniques (Bickel et al., 2006; Ghojogh & Crowley, 2019) impose constraints on the

254   model's coefficient estimates (learned parameters), effectively preventing it from overfitting the

255   training data and improving its generalizability to new data. This is achieved by adding a penalty term

256   to the loss function - the measure of how well the model fits the training data. The penalty term

257   typically increases with the complexity of the model, thus incentivizing simpler models that

258   generalize better to unseen data. Additionally, we utilized dropout layers (Hinton et al., 2012; Wager

259   et al., 2013) between each LSTM layer. These dropout layers randomly drop a certain percentage of

260   connections during training, effectively preventing individual neurons from becoming overly reliant

261   on specific features in the training data. This stochasticity enhances model generalizability by

262   encouraging it to learn more robust and transferable data representations.

263   We opted for a bidirectional LSTM network with four layers. This architecture was chosen based on

264   its ability to capture both temporal and spatial dependencies in the data, which is crucial for accurate

265   hydrological modeling. Increasing the number of layers beyond four yielded minimal performance

266   improvements, suggesting that the four-layer architecture was sufficient for capturing the relevant

267   patterns in the data. Finally, we selected the Swish activation function (Ramachandran et al., 2017)

268   for the output layer. This activation function has a smoother and more non-linear nature compared

269   to ReLU - the most common activation function in ML, which enhances the flow of gradients

270   through the network, contributing to improved performance. In addition to its computational

271   efficiency, Swish also mitigates the dying ReLU problem, a phenomenon where ReLU neurons

272 become inactive during training. By maintaining active neurons throughout the training process,

273 Swish ensures that the network continues to learn and adapt. Furthermore, Swish offers efficiency

274 advantages over ReLU, particularly when training deep neural networks with numerous layers,

275 further reducing computational burdens. Overall, our hyperparameter tuning strategy and network

276 architecture choices resulted in a robust and generalizable bidirectional LSTM model capable of

277 accurately predicting hydrological time series.

278

279 **2.3. Experiment Design**

280 We hypothesize that an LSTM model trained with topologically organized distributed

281 geomorphologic and hydrologic information should outperform the same LSTM that lumps the

282 same training data. To this end, we estimate discharge in five ways: three experiments with identical

283 ML models per Section 2.2 but with different organizations of the training data, and comparisons

284 with two state-of-the-art approaches: an assimilation product (RADR- Feng et al., 2021) and a

285 recently published LSTM model (PUB-LSTM- Kratzert et al., 2019). By organizing the training data

286 consistently with topology, we aim to capture these spatial relationships and allow the ML model to

287 learn more intricate patterns in the data. This approach differs from traditional methods that

288 aggregate data into a single-point representation, which may lead to the loss of critical spatial

289 information.

290 **2.3.1. Experiments and literature comparisons**

291 I. **At-station experiment**: We used dynamic and geomorphological static variables and

292   climate data in a 25 km buffer around a given gauge station as input features to an ML

293   model. These are the fewest possible data we can use to train any ML model that leverages

294   temporal and spatial information encoded in historical data around a gauge station.

295 II. **Lumped experiment:** In addition to leveraging local information around the river outlet

296   (the at-station experiment), we included integrated aggregated climate data from the largest

297   possible upstream basin. Therefore, this experiment has static and dynamic variables from

298   the prediction reach and averaged upstream climatology. This represents the approach taken

299   by Ouyang (2021), Feng (2020; 2021), Ma (2021), and Kratzert (2019a; 2019b), among

300   others.

301 III. **Distributed experiment:** Here, we expanded on the methodology used in experiments (I)

302   and (II) by segmenting the upstream climate data according to the Strahler River order

system. Although traditional clustering methods such as DBSCAN are better at clustering data (e.g., Brinkerhoff et al., 2020; Muhebwa et al., 2021), we chose the Strahler River ordering because it is an objective, consistent, and physically meaningful method for hierarchical clustering of hydrometeorological information, making it useful for various hydrological and geomorphological studies. This stratification was applied to dynamic variables in the entirety of the upstream basin. Thus, for a river system encompassing 'n' orders of upstream sub-basins, we introduced a more nuanced set of input features. Specifically, for each river order, we generated a distinct set of input features corresponding to each of the modeled hydrometeorological processes. The total number of additional input features was thus calculated as (n*x), where 'x' represents the total number of these processes. By averaging the data across all sub-basins per order (Figure 3), we were able to effectively capture the spatial variability of hydrological processes, resulting in more accurate river discharge predictions. The distributed approach aligns with those of Baroni et al. (2019) and Moore et. al. (1991), who emphasize the effectiveness of integrating data from various sources and considering spatial variability in hydrological processes, respectively. This method adheres to the principles of distributed data modeling, as it enhances river discharge prediction by incorporating the spatial distribution of hydrological processes, such as snowmelt, soil moisture, and evapotranspiration, across the watershed.

IV. **Comparison datasets:** We compare our approach against off-the-shelf results from the RADR model and a re-implementation of the PUB-LSTM model. The RADR (Feng et al., 2021) model was calibrated on data from 1984 to 1998 and assimilated with remotely sensed discharge data from 1984 to 2018 for the entire Arctic region (including the Mackenzie basin). Data assimilation in process-based modeling provides time-dependent distributed estimates that are updated whenever new data become available, i.e., the model's states are updated in response to how it performs at a given time (McLaughlin, 1995; Clark et al.,2008). We also implemented the PUB-LSTM model defined in Kratzert (2019) – a state-of-the-art unidirectional LSTM model. We trained this model with data defined in the lumped experiment but consolidated the data from all gauge stations into a single set (irrespective of the river order) before performing k-fold cross-validation. This means that each subset of stations in training/validation can contain data across any of the orders 4 to 8.

334 Our approach requires us to develop order-specific ML models given the rigid requirements for

335 LSTM training. That is, each of our three ML experiments has five different LSTMs - one for each

336 order from 4 to 8, as these orders contain sufficient training data. In order to apply our model to an

337 ungauged basin, we would need first to identify the order of the river reach of interest and then

338 select the appropriate order model to deploy. This means that our methods cannot predict flows in

339 orders other than 4-8, but in return for this compromise, we can estimate flows quickly, efficiently,

340 and accurately in ungauged basins, as shown below. Further, global datasets like those used to build

341 our models already identify the order of all global rivers, so there is no additional computational

342 burden on future users of these methods.

343 **2.3.2. Validation design and applicability to ungauged basins**

344 Our objective is to develop ML models that can accurately forecast daily river discharge in ungauged

345 basins: watersheds lacking discharge monitoring stations (gauge stations). A standard approach in

346 machine learning is to split the model's input data into training and validation sets by a particular

347 ratio (Wu et al., 2013; Rácz et al., 2021; Shen et al., 2022). This implies that training and validation

348 occur on data from the same distribution, known as independent and identically distributed (IID)

349 data, where each random variable follows the same probability distribution, and all variables are

350 independent. Consequently, it is simple to train models that perform well on training and validation

351 data but struggle to generalize effectively to unseen data, a phenomenon known as overfitting.

352 However, our goal is to transfer hydrological knowledge to ungauged basins. Therefore, we employ

353 cross-validation to assess the performance of our ML models. Cross-validation (Stone, 1987; Rao et

354 al., 2008; Refaeilzadeh et al., 2009; Berrar, 2019) is a technique where multiple ML models are

355 trained on subsets of the available input data and evaluated on complementary subsets of the same

356 data. This introduces heterogeneity in the training data by repeated resampling, thereby improving

357 the ability of models to generalize to previously unseen data.

358 Since we use stream order as a unifying concept for our distributed modeling, we must build, train,

359 and validate models that function per order. Previous studies (e.g., Feng et al., 2021; Kratzert el at.,

360 2019; Sun et al., 2021) have either treated training data as a single entity, thereby making it easier to

361 implement out-of-sample testing using k-fold validation (dividing data into groups of approximately

362 equal sizes) or splitting training data by a given percentage (e.g., 70/30 split) for models trained and

363 tested on IID data. Conversely, different Strahler River orders in our training data have unequal

364 gauge stations (Table 1), making it difficult to implement an identical k-fold validation strategy. The

365   imbalance in data across different orders can result in model uncertainties. We mitigate this by

366   combinatorial training data selection for individual models in each order and by maintaining an equal

367   number of stations (x) in each training and validation subset. This strategy of organizing training

368   data maintains a relatively consistent volume of training data across the entire data strata. Consider a

369   stream order with n stations; we can create sets of all possible combinations of stations in that order

370   where each set contains x stations where x is any arbitrary number less than n. We chose x=3 for

371   our experiment as a tradeoff between the minimum number of stations in each order (orders 7 and 8

372   each have 4 stations) and the computation time to train models for all subsets in each order. We

373   then train a model on each subset and evaluate it on the complementary subsets of the same order.

374   Therefore, in a basin with n=25 gauge stations, we try all combinations of x=3 training and (n-x)=22

375   validation stations. For stations with many subsets, i.e., orders 4 to 6 (Table 1), we randomly select

376   24 sets from all possible $^{n}C_{x}$ combinations to balance model compute time with statistical

377   representativeness. Preliminary experiments to increase the size of the sets from 24 to 50 and 100

378   had no substantial improvement/degradation in model performance. Our results are presented as

379   distributions of predictions across the complementary (validation) sets instead of reporting the

380   results of individual or selected ML models that may perform particularly well or poorly at a gauge

381   station. Therefore, the width of these distributions corresponds to the sensitivity of our three

382   experiments to a particular combination of training/validation data.

383   Note that orders 7 and 8 have sufficient data to train and test but insufficient data to cross-validate.

384   Also, remember that we build per-order ML models; thus, the performances here reflect only rivers

385   of that order. Finally, given the available gauge data in the Mackenzie, we cannot predict in orders

386   below 4 and above 8.

387   Table 1: Table showing the number of generated and contributed sets used for training in each

388   Strahler River order.

Strahler order	Number of gauge stations (n)	Number of training stations per set (x)	Number of ungauged validation stations per set (n-x)	Possible training/validation combination sets ($^{n}C_{x}$)	Number of selected sets used to report results
4	25	3	22	2300	24
5	23	3	21	1771	24

6	13	3	10	286	24
7	4	3	1	4	4
8	4	3	1	4	4

389

390 Ultimately and importantly, all results represent an ungauged case where validation is only done on
391 the n-x stations not used in training and then tested in combinations per Table 1. This represents a
392 common hydrologic situation where some gauge data are in a basin but not in areas where desired.
393 Our methods would use the gauge data in hand, per order, to make estimates at all ungauged reaches
394 of the basin of the same order. Here, we withhold gauge data to make that test, and each validation
395 set, is completely independent of the others for a true ungauged case.

Figure 3: Schematic representation of an order eight basin network. The red circle represents the location of a gauge station on the delineated basin's outlet. At each hierarchical level, a single-order basin and its lower-order basins are selected (filled), while the remaining basins on the same level or not upstream of the selected basin within that level are ignored (hatched). This topological representation integrates the temporal-spatial variation of physical processes at different stages of a river network.

2.4. Evaluation Metrics

We report our results based on four major metrics used to evaluate the performance of discharge prediction models: Kling-Gupta Efficiency (KGE) (Gupta et al., 2009), Nash-Sutcliffe Efficiency (NSE) (Nash & Sutcliffe, 1970), Relative Bias, and Normalized Root Mean Squared Error (NRMSE).

406

407     $KGE = 1 - \sqrt{(\gamma - 1)^2 + (\alpha - 1)^2 + (\beta - 1)^2}$ (7)

408   where γ is the Pearson correlation between observed and actual discharge, α is the ratio of the

409   standard deviation of actual vs. observed discharge, and β is the ratio of the mean of observed vs.

410   actual discharge.

411     $NSE = 1 - \dfrac{\sum_{i=1}^{N}(Q_i - Q_i^I)^2}{\sum_{i=1}^{N}(Q_i - \bar{Q})^2}$ (8)

412   Where Q_i is the observed discharge at timestep ι and Q_i^I is the simulated discharge at timestep ι.

413   These standard hydrology metrics assess different aspects of the hydrograph and errors in both

414   timing and volume of water (e.g., Lin et al., 2019; Hagemann et al., 2017).

3. Results

416   Our experiments show that a distributed data modeling approach outperforms at-station and

417   lumped approaches in training ML models for predicting discharge in ungauged basins. Figure 4

418   illustrates this outcome by presenting cumulative distribution functions (CDFs) for KGE and NSE

419   across the experiments defined in Section 2.3.1. Note that all results pertain to ungauged cases where

420   validation is performed exclusively on the n-x stations not used for training and then tested in

421   combinations as per Table 1.
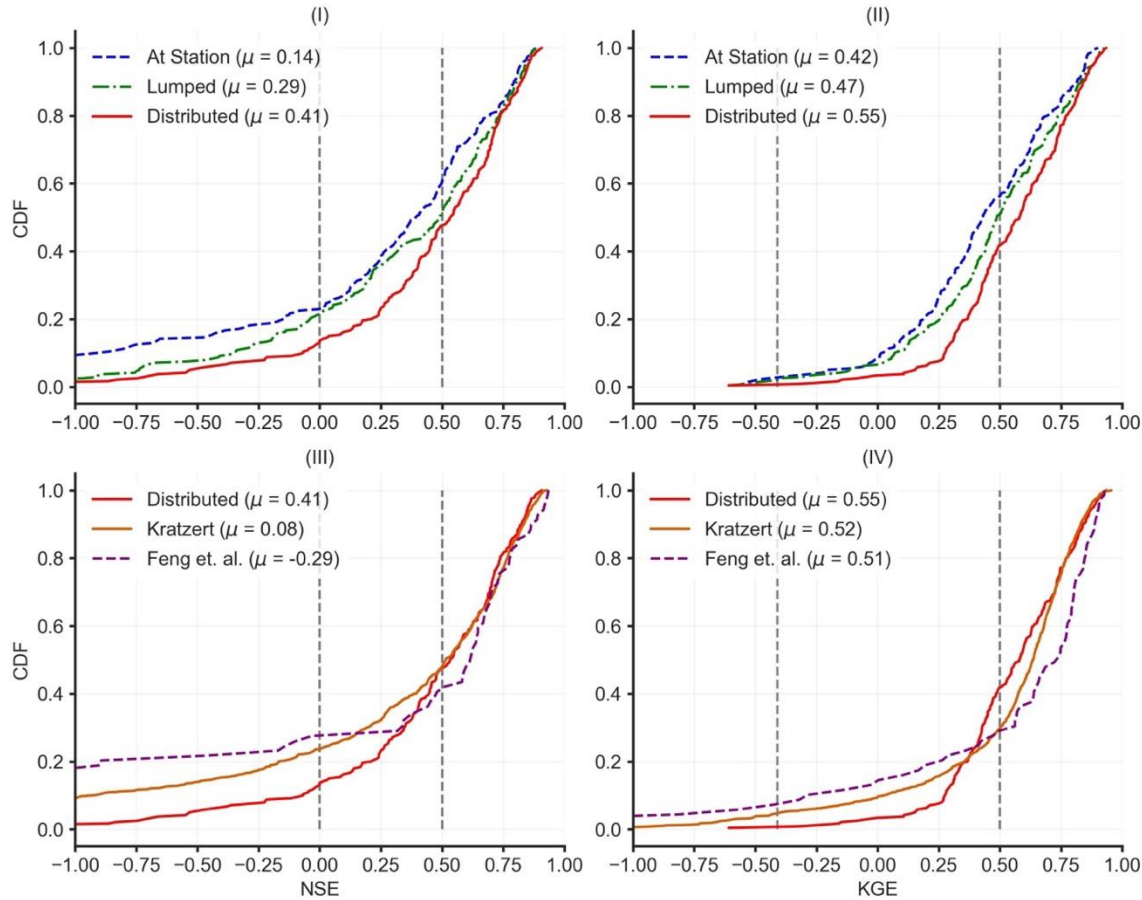
3.1.   Predictions in Ungauged basins

Figure 4: Cumulative distribution functions (CDFs) of NSE and KGE for defined experiments and selected benchmarks calculated from distributions across all Strahler River orders. Figures (I) and (II) compare the performance of models in the at-station and lumped experiments against the models trained with data from the distributed experiment. Figures (III) and (IV) compare the performance of models in the distributed experiment against two literature models: Feng et al. (2021) and Kratzert et al. (2019). A shift to the right indicates an improvement in model performance. Baseline models from the literature show lower skill than the ML here when all models perform poorly ($-\infty < $ NSE&KGE ≤ 0.0) but better performance when all models have good predictions ($0.5 < $ NSE &KGE ≤ 1.0). The distributed model outperforms the at-station and lumped models across the entirety of the results. CDFs are preferred because they represent the overall model performance across the entire test dataset.

Comparing results from at-station, lumped, and distributed experiments reveals that incorporating increasing amounts of upstream basin data universally enhances discharge estimation. In Figures 4(I) and (II), the rightward shift of the distributed experiment's cumulative distribution function (CDF) curve relative to those of the at-station and lumped experiments indicates performance improvement. Order level-specific models trained with minimal data (at-station experiment) achieve 77% positive NSE predictions and 92% positive KGE predictions. KGE and NSE values range between ($-\infty$, 1]; positive values are generally desirable, while negative NSE values indicate that the

439 mean of observed values is a better predictor than the predicted value. KGE is a more 'forgiving'

440 metric that takes a value of -0.41 when the mean hydrograph is predicted (NSE scores 0 in this

441 case), as shown by Knoben, Freer, & Woods (2019). Incorporating aggregated upstream basin

442 information (lumped experiment) into model training yielded no significant performance

443 improvement (P-value > 0.05). However, training the same models with topologically organized data

444 (distributed modeling) led to a 6.4-point increase in mean NSE and a 9.8-point increase in mean

445 KGE.

446

447 Figure 5: Top to Bottom: Distribution comparisons of selected metrics on held-out predictions for at-station (I-IV), lumped (V-VII),

448 and distributed (IX-XII) experiments. Note that distributions for seventh and eighth orders are not included due to the limited

449 number of gauge stations in the training set. Figure S1 shows a distribution comparison across all experiments and literature models.

450 When ML models were trained with the least possible data (at-station experiment), i.e., Figure 5(I)-

451 (IV), we observed a significant (p ≤ 0.05) improvement in median KGE from 0.38 to 0.61 as basin

452 size increased from order 4 to order 6, which is observed across all experiments. NSE, however, was

453 relatively constant across orders, with a noticeable increase in the interquartile range (IQR) for the

454 largest order with ten stations. When we compared similar spatial orders across the three

455 experiments (columns in Figure 5) - at-station, lumped, and distributed experiments - we observe an

456 improvement in both NSE and KGE scores as orders increase and more information is added to

the data modeling process. Consider Figures 5(I), (V), and (IX), KGE improved from 0.38 to 0.56 in the fourth order, 0.34 to 0.46 in the fifth order, and 0.61 to 0.69 in the sixth order, from at station to distributed experiments respectively. Likewise, we observe an equivalent improvement in NSE, i.e., Figures 5(II), (VI), and (X) from 0.42 to 0.48 in the fourth order, 0.34 to 0.47 in the fifth order, and 0.29 to 0.60 in the sixth order. Additionally, these skill gains are accompanied by consistently unbiased predictions with negligible relative bias (RBias $\approx$ 0.0) across all models and orders. When we compare the performance of literature models on an order level basis (Figure S1), we observe a much more substantial improvement in performance as the number of sub-basins increases. The RADR model (Feng et al., 2021) had the most noticeable improvement in skill scores, with median KGE improving from 0.63 in the fourth order to 0.77 in the sixth order, while median NSE improved from 0.47 to 0.58 in the corresponding orders. On the other hand, Kratzert et al. (2019) demonstrated an improvement in KGE from 0.68 in the fourth order to 0.72 in the sixth order but a decline in NSE scores from 0.72 in the fourth order to 0.56 in the sixth order. We compare the results of the distributed experiment against model predictions of both a reimplementation of an ML model proposed by Kratzert et al. (2019) with minor modification and off-the-shelf results of a remote sensing data assimilation over the same basin and time from Feng et al. (2021), i.e., Figure 4(III)-(IV). Performance across all three methods was largely similar but with noticeable differences in 'good' and 'bad' regions of skill, which is more pronounced with the KGE metric (that rewards correlation per Eq. 1). The distributed modeling approach has 13% of all NSE values and 3% of all KGE values as negative predictions across the entire experiment, the Kratzert et al. model has 22% of all NSE values and 7% of KGE values as negative predictions across all orders, and the Feng et al. model has 28% of all NSE values and 13% of all KGE values as negative predictions across all Strahler river orders. Thus, the distributed LSTM we propose here produces fewer 'bad' hydrographs that are worse than the mean compared to the other two methods. However, when all models perform well, the two literature models outperform our LSTM, although performance is quite similar (p > 0.05).
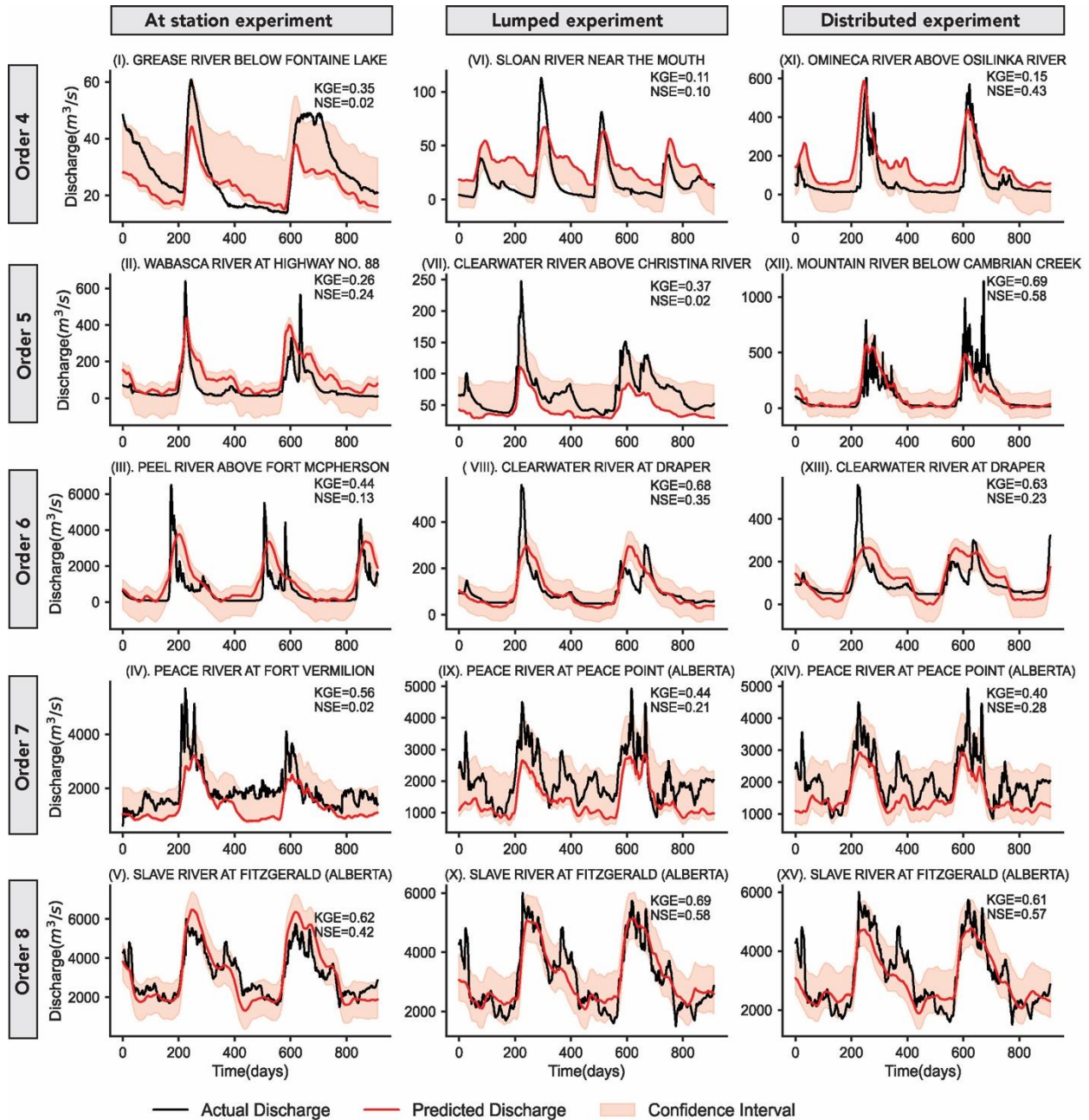
Figure 6: Representative hydrographs showing randomly selected models with 0.0 < NSE ≤ 0.6 in each of the experiments: At-station (left), lumped (middle), and distributed (right) experiments across the defined orders, i.e., from order 4 (top) to order 8 (bottom). Here, we plot hydrographs for the first 2.5 years.

Figure 6 shows hydrographs of randomly selected ML models in orders 4 to 8 whose NSE scores lie between 0.0 and 0.6. Here, we use 0.0 < NSE ≤ 0.6 as a representative average performance range across the prediction distribution. Across individual experiments, the models' confidence to re-create discharge increases as sub-basins increase. For example, absolute relative bias (|RBIAS|) improves from 0.24 to 0.007 in the station experiment, 0.80 to 0.002 in the lumped experiment, and

492   0.82 to 0.06 in the distributed experiments, as the number of sub-basins increases (i.e., from fourth

493   to eight order). Note that as relative bias approaches zero, model predictions become increasingly

494   unbiased and reliable, thereby enhancing the confidence and reliability with which they can inform

495   impactful water management decisions. Nevertheless, notable differences in hydrographs remain

496   across the defined experiments. Consider the fourth order across the three experiments, normalized

497   root mean squared error (NRMSE) reduces from 0.17 in the at-station experiment to 0.09 in the

498   distributed experiment, indicating an improvement in model performance in response to additional

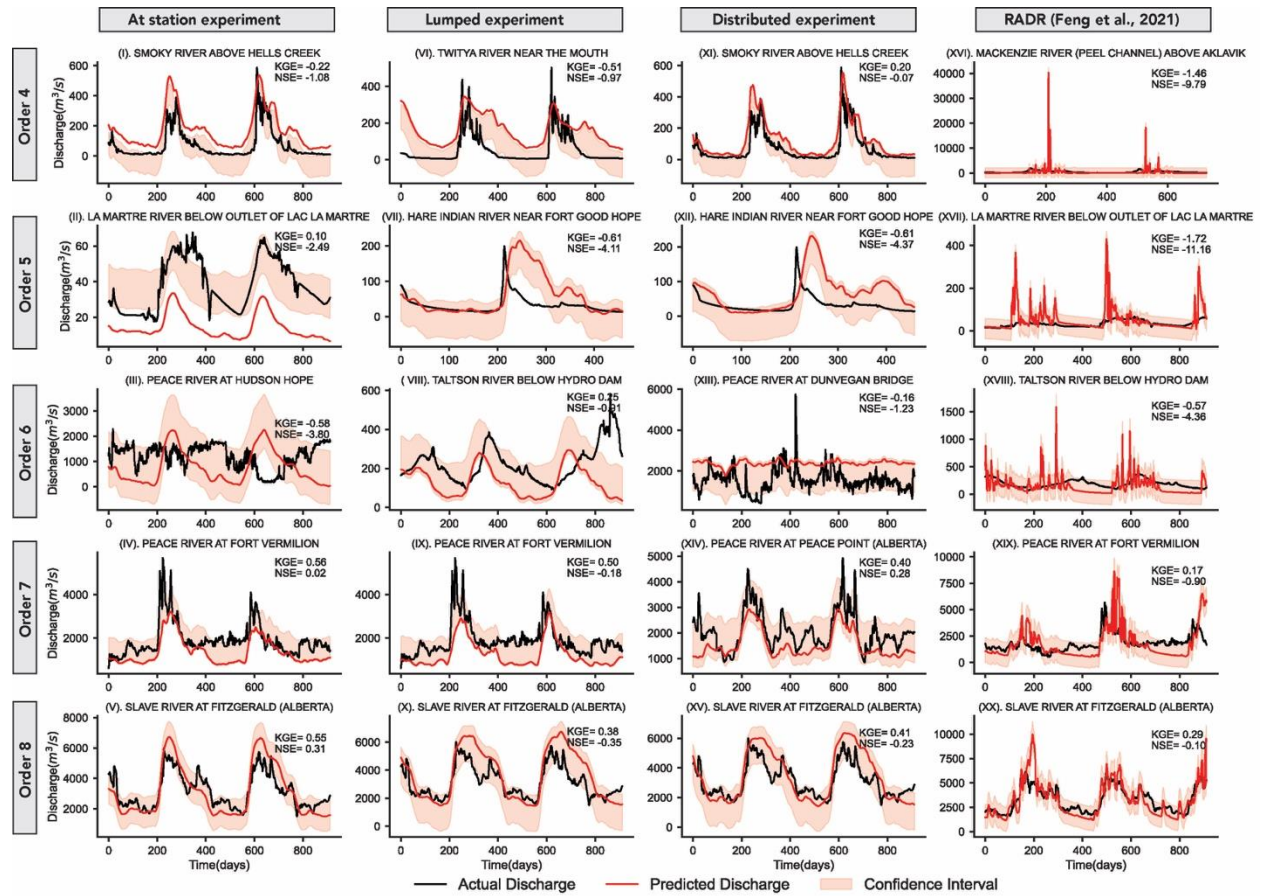499   hydrological information in the training data.

Figure 7: Left to right: Representative hydrographs showing the worst performing ML models in each of the experiments and the non-ML literature model; At station experiment, lumped experiment, distributed experiment, and RADR model (Feng et al., 2021) across the defined orders, i.e., from order 4 (top) to order 8 (bottom). The RADR model overestimates peak flows and underestimates base flows in lower orders. Here, we plot hydrographs for the first 2.5 years.

505   Figure 7 represents hydrographs of worst-performing models with NSE scores below 0.0 (-∞ <NSE

506   <0.0) across orders 4 to 8. This NSE range encompasses the entirety of potentially bad model

507   predictions within the predicted discharge distribution, providing a comprehensive view of model

508 shortcomings across the defined experiments. We observed that across all experiments, models
509 within orders 4 and 5 demonstrated a significant difficulty in precisely reproducing discharge
510 hydrographs, indicated by a high uncertainty in model predictions. Interestingly, higher-order
511 models, specifically those of orders 7 and 8, exhibited a consistent ability to capture the underlying
512 trend of the actual discharge despite persisting uncertainty in the finer details. The underwhelming
513 performance of RADR models reinforces the observation in Figure 4: process-based models, while
514 valuable for capturing established physical and hydrologic laws, often struggle to adapt to real-world
515 scenarios marked by significant, unpredictable fluctuations; that is, their inflexible structure hinders
516 their ability to adapt to these deviations, leading to less accurate discharge predictions.
517 Different geographical and climatic regions have dominant physical processes at different temporal-
518 spatial scales. Results in section 3.1 showed that integrating this knowledge of temporal-spatial
519 variations (distributed modeling) improved the discharge prediction of ML models.
520 Earlier studies (e.g., Kahraman et al., 2021; Dey & Fuentes, 2020) showed that longer lookback
521 windows with a longer 'memory' of past hydrologic conditions improve model performance.
522 However, this performance improvement comes with increased computational power and time. To
523 further evaluate the impact of the lookback window on model performance, we repeat experiments
524 defined in section 2.3.1 with varying lookback window sizes of 30, 90, 180, and 270 days. Pairwise
525 comparisons of distributions for both at-station and lumped experiments indicate that the size of the
526 lookback window has no impact on model performance (P-value > .05). However, there is a
527 significant difference between distributions of results for lookback pairs (30, 90), (30, 270) days of
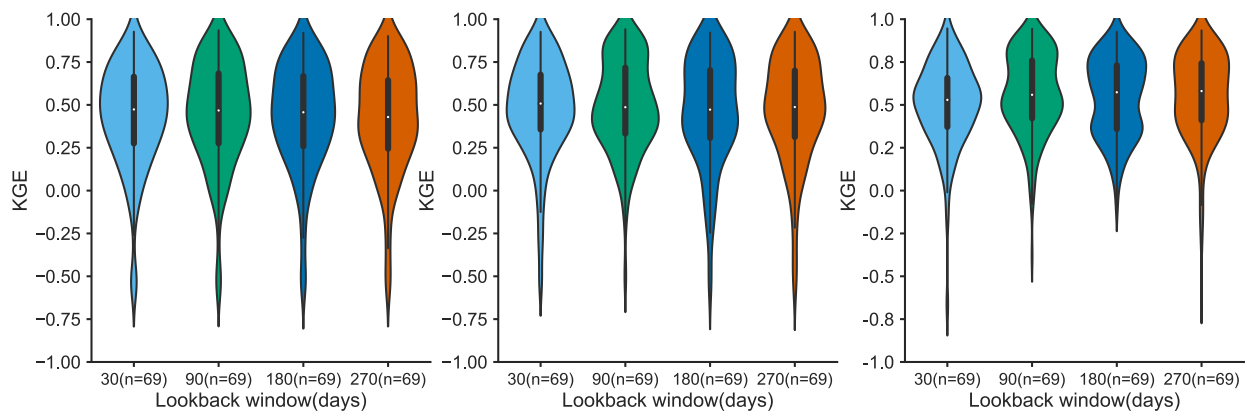528 the distributed experiment (P-value ≤ .05).

Figure 8: Left to right: Pairwise comparison of KGE distributions with varying lookback window sizes and corresponding statistical significance tests across the three experiments. Inter-experiment comparisons show that distributions of lookback for at-station and lumped experiments are similar. At the same time, there is an observable difference in the distributions of lookback windows of the distributed experiment.

4. Discussion

We confirm our hypothesis that distributed modeling outperforms lumped modeling for our architecture, but that by Kratzert et al's (2019) lumped LSTM has superior performance to our distributed model when all models predict well. Our model outperformed the literature models when all models produced poor hydrographs (Figure 4, 7), and our skill scores have a much higher 'floor' than the literature models. However, we have a lower 'ceiling' as well - the literature models' performance exceeds ours when all models perform well, although the difference between this study and the literature is much more pronounced at lower skill (where our results improve skill). We attribute the superior performance of the Feng et al. RADR product at the high skill areas to three factors. First, RADR was calibrated on remotely sensed data drawn from the same distribution (independent and identically distributed data). Second, the model was assimilated on heterogeneous data from the entire Arctic region (as compared to our models trained on data from only the Mackenzie basin). Finally, the superior performance of process-based models can be attributed to their deep-rooted understanding of hydrologic, geomorphologic, and hydrometeorological processes. This comprehensive knowledge enables process-based models to effectively simulate the complex and interconnected interactions between various processes within a river basin. This theoretical foundation grounded in the principles of hydrology and river system dynamics not only enhances their predictive accuracy but also ensures the physical consistency and interpretability of the results. We attribute the Kratzert et al. model's better performance to a different training strategy as compared to the distributed experiment. Whereas models in the distributed experiment were trained and validated on order-specific training data, the Kratzert et al. model used a k-fold validation strategy and trained on the entire spectrum of data (all 69 gauge stations), following the original model implementation proposed by the authors. This strategy ensured the model was trained on more diverse data, enhancing its generalization to previously unseen data. This also offers the advantage of enabling flow prediction for all rivers within the basin. However, in our study, we didn't follow Kratzert et al. because our distributed experiment exhibits two notable advantages: first, when all models performed poorly (Figure 6), models in the distributed experiment still performed better than literature models. In general, we attribute poor performance (poor generalization) to limited training data, a reality for much of the world where training data are rare, nonexistent, or proprietary (Gleason & Smith, 2014). Second, acknowledging the influence of physical processes on the hydrologic cycle, the existence of these processes at different spatial resolutions, and their varying dominance across different geographical regions, order-specific models

566 in the distributed experiment firmly integrate this hydrological knowledge in the data modeling
567 process as compared to the literature models. One possible explanation of why models in the
568 distributed experiment perform better when all models have low skill scores is that despite limited
569 training data, these models are better than literature models at leveraging the high correlation
570 between temporal-spatial variability and physical processes to extract meaningful patterns in the
571 training data. This capability is particularly relevant when considering discharge estimation on a
572 global scale, where well-hydrologically mapped regions are scarce.
573 We also observe that while RADR has the highest skill score when all models perform well, it also
574 has the lowest skill scores when all models generally perform poorly (Figures 4(III) and (IV)). One
575 possible explanation is that process-based models, which rely heavily on established physical and
576 hydrological principles, often struggle to adapt to poorly understood scenarios or environments with
577 significant uncertainties. This limitation is further compounded by their potential inability to capture
578 emergent phenomena and human impacts - complex interactions or patterns that arise
579 spontaneously and are not yet fully understood or integrated into existing hydrologic theories. Thus,
580 the scientific robustness of process-based models, while grounded in established principles, can
581 inadvertently narrow their score, hindering their ability to dynamically adapt to and accurately model
582 these evolving and multifaceted riverine environments. Thus, while each model possesses unique
583 advantages, a distributed data modeling approach offers a more applicable and scalable solution for
584 global-scale discharge estimation.
585 Further, we observed that even the best-performing models in the at-station experiment (Figure S2)
586 fail to recreate medium to high peak discharges by a considerable margin in the lower orders. This is
587 not surprising, given that peak discharges are a function of events in the upstream basin, e.g., after
588 maximum rain intensity or melting of accumulated snow (Volpi et al., 2018; Jones, 2000; Furey &
589 Gupta, 2005; Kabeja et al., 2020), information that is not included in the training data. Indeed, the
590 impact of the knowledge of events in the upstream basin becomes more prevalent as more
591 information is added to the training data. This is visible in the hydrographs of both the lumped and
592 distributed experiments in Figure 6 (average-performing) and Figure S2 (best-performing), in which
593 models recreate most of the peak discharges (or miss them by a small margin). To verify this, we
594 aggregated the top 10 peak flows of each station. We observed that the mean error of the best-
595 performing models across each experiment (defined as the average of the top 10 peaks in each
596 order) reduced from 2901.58 m^3s^{-1} in the lumped experiment to 2518.74 m^3s^{-1} in the distributed
597 experiment and observed a similar pattern between the same orders across the two experiments.

598 We attribute the high correlation between pairs of lookback windows for both the at-station and

599 lumped experiments to the fact that both experiments ignore spatial variations of events in the

600 upstream basin (physical processes). On the other hand, we attributed the differences across the

601 lookback window pairs of the distributed experiment to the integration of knowledge of both

602 temporal and spatial variations of physical processes in the data modeling process, indicating that the

603 impact of dominant physical processes on model performance is prevalent at different temporal-

604 spatial scales. We found that at various temporal scales (with similar spatial scales), a lookback of as

605 little as 90 days was enough to capture temporal information encoded in the training data. As such,

606 we saw no additional value in longer lookback windows, although this could be different for

607 different geographical regions and data.

608 We do not report individual skill scores of the seventh and eighth orders (Figure 5) due to the

609 limited number of gauge stations (Table 1). Further, data availability limits the minimum number of

610 gauge stations (x) to include in each subset, which reduces data heterogeneity for each order-specific

611 model. For instance, on order 8, x=3 represents 75% of the data as training, while on order 4, x=3

612 represents only 12% (Table 1). We chose to keep x constant instead of a constant train/test ratio

613 because this allows sharing model hyper-parameters (and structure) and makes it easier to compare

614 the results of models trained on the same number of gauge stations (x) across different orders of the

615 same experiment. Finally, randomly selecting 24 subsets from all possible combinations for spatial

616 resolutions with many gauge stations (Table 1) is not the best representation of complete data

617 heterogeneity. However, we experimented with up to 100 validation sets and observed no substantial

618 change in model performance. Future work could explore all possible combinations of training and

619 testing and/or vary x to learn the effect of increasing the training sample.

620 ML has demonstrated encouraging results in global river discharge predictions and holds the

621 potential to address many existing challenges in hydrology (Shen, 2018; Nearing et al., 2021).

622 However, these advancements have primarily relied on lumped data modeling techniques, which

623 overlook the temporal-spatial variations of physical processes that govern the hydrologic cycle. We

624 have demonstrated that incorporating this knowledge into training data modeling (via our

625 distributed experiments) can further improve the performance of ML models, particularly for

626 predictions in ungauged basins. Further, we have shown that even with limited data, a distributed

627 modeling strategy could provide improved predictions (especially in ungauged basins) than any of

628 the existing benchmarked models. We acknowledge that literature models from ML and hydrologic

629 modeling represented by Kratzert et al. (2019) and Feng et al. (2021) offer unique advantages that

630 can deepen our understanding of global discharge as a proxy for assessing the cascading impacts of

631 climate change on water resources. Therefore, leveraging distributed modeling could further

632 improve the performance of other ML approaches.

633 **5. Conclusion**

634 In this work, we have demonstrated the importance of distributed data modeling in improving the

635 performance of ML models for discharge prediction in ungauged basins. Further, we leverage

636 topologically guided river hierarchies as a proxy for understanding the impact of temporal resolution

637 (lag window) on model performance, specifically examining how much historical context is

638 necessary to improve model performance. We showed that as spatial resolution increases, model

639 performance improves in response to granular hydrological information. This makes our proposed

640 method more applicable for predicting discharge for most global river basins with limited to no data.

641 Our experiments and results demonstrate the importance of integrating hydrological and

642 geographical differences in the data modeling process, a notion that has, until now, been largely

643 ignored when building data-driven hydrology models. With the recent launch of the SWOT mission

644 that will provide more consistent and granular hydrological information on global rivers, our

645 proposed approach has the potential to improve methods for predicting river discharge on a global

646 scale and, as a result, explore the complex, cascading, and often hidden ways that climate change

647 alters global water systems. However, while we did not specifically identify which physical processes

648 are dominant at varying spatial scales, this opens up questions in future work on quantifying the

649 temporal-spatial contribution of distinct features towards model performance and overall

650 interpretability and explainability of ML models in hydrology and physical sciences in general.

651

Data and Code Availability Statement

Code related to this study can be found online at https://github.com/amuhebwa/rivers_ML . Data used in this study is available at https://zenodo.org/record/6604724 . Data for the RADR model is available at (https://zenodo.org/record/5604980)

References

Agostinelli, F., Hoffman, M., Sadowski, P., & Baldi, P. (2014). Learning activation functions to improve deep neural networks. arXiv preprint arXiv:1412.6830.

Akbari Asanjan, A., Yang, T., Hsu, K., Sorooshian, S., Lin, J., & Peng, Q. (2018). Short-term precipitation forecast based on the PERSIANN system and LSTM recurrent neural networks. Journal of Geophysical Research: Atmospheres, 123(22), 12-543.

Andreadis, K. M., Brinkerhoff, C. B., & Gleason, C. J. (2020). Constraining the assimilation of SWOT observations with hydraulic geometry relations. Water Resources Research, 56(5), e2019WR026611.

Arsenault, R., & Brissette, F. P. (2014). Continuous streamflow prediction in ungauged basins: The effects of equifinality and parameter set selection on uncertainty in regionalization approaches. Water Resources Research, 50(7), 6135-6153.

Aziz, O. I. A., & Burn, D. H. (2006). Trends and variability in the hydrological regime of the Mackenzie River Basin. Journal of hydrology, 319(1-4), 282-294.

Baroni, G., Schalge, B., Rakovec, O., Kumar, R., Schüler, L., Samaniego, L., ... & Attinger, S. (2019). A comprehensive distributed hydrological modelling intercomparison to support process representation and data collection strategies. Water Resources Research, 55(2), 990-1010.

Bengio, Y., & Gingras, F. (1995). Recurrent neural networks for missing or asynchronous data. Advances in neural information processing systems, 8.

Berrar, D. (2019). Cross-Validation.

Basijokaite, R., & Kelleher, C. (2021). Time-Varying Sensitivity Analysis Reveals Relationships Between Watershed Climate and Variations in Annual Parameter Importance in Regions With Strong Interannual Variability. Water Resources Research, 57(1), e2020WR028544.

Beaudoing, H. and M. Rodell, NASA/GSFC/HSL (2019), GLDAS Noah Land Surface Model L4 3 hourly 0.25 x 0.25 degree V2.0, Greenbelt, Maryland, USA, Goddard Earth Sciences Data and Information Services Center (GES DISC) Accessed: Aug, 2021

Belvederesi, C., Zaghloul, M. S., Achari, G., Gupta, A., & Hassan, Q. K. (2022). Modelling river flow in cold and ungauged regions: a review of the purposes, methods, and challenges. Environmental Reviews, 99(999), 1-15.

Bergstra, J., & Bengio, Y. (2012). Random search for hyper-parameter optimization. Journal of machine learning research, 13(2).

Bickel, P. J., Li, B., Tsybakov, A. B., van de Geer, S. A., Yu, B., Valdés, T., ... & van der Vaart, A. (2006). Regularization in statistics. Test, 15(2), 271-344.

695 Birhanu, D., Kim, H., & Jang, C. (2019). Effectiveness of introducing crop coefficient and leaf area index to
696   enhance evapotranspiration simulations in hydrologic models. Hydrological Processes, 33(16), 2206-2226.

697 Brinkerhoff, C. B., Gleason, C. J., & Ostendorf, D. W. (2019). Reconciling at-a-station and at-many-stations
698   hydraulic geometry through river-wide geomorphology. Geophysical Research Letters, 46(16), 9637-9647.

699 Brinkerhoff, C., Gleason, C., Feng, D., & Lin, P. (2020). Constraining remote river discharge estimation using reach-
700   scale geomorphology. Water Resources Research, 56(11), e2020WR027949.

701 Buck, S. F. (1960). A method of estimation of missing values in multivariate data suitable for use with an electronic
702   computer. Journal of the Royal Statistical Society: Series B (Methodological), 22(2), 302-306.

703 Che, Z., Purushotham, S., Cho, K., Sontag, D., & Liu, Y. (2018). Recurrent neural networks for multivariate time
704   series with missing values. Scientific reports, 8(1), 1-12.

705 Chung, J., Gulcehre, C., Cho, K., & Bengio, Y. (2014). Empirical evaluation of gated recurrent neural networks on
706   sequence modelling. arXiv preprint arXiv:1412.3555.

707 Claesen, M., & De Moor, B. (2015). Hyperparameter search in machine learning. arXiv preprint arXiv:1502.02127.

708 Clark, M. P., Rupp, D. E., Woods, R. A., Zheng, X., Ibbitt, R. P., Slater, A. G., ... & Uddstrom, M. J. (2008).
709   Hydrological data assimilation with the ensemble Kalman filter: Use of streamflow observations to update
710   states in a distributed hydrological model. Advances in water resources, 31(10), 1309-1324.

711 Clark, M. P., Nijssen, B., Lundquist, J. D., Kavetski, D., Rupp, D. E., Woods, R. A., ... & Rasmussen, R. M. (2015).
712   A unified approach for process-based hydrologic modelling: 1. Modelling concept. Water Resources Research,
713   51(4), 2498-2514.

714 Clark, M. P., Nijssen, B., Lundquist, J. D., Kavetski, D., Rupp, D. E., Woods, R. A., ... & Marks, D. G. (2015). A
715   unified approach for process-based hydrologic modelling: 2. Model implementation and case studies. Water
716   Resources Research, 51(4), 2515-2542.

717 Clark, M. P., Schaefli, B., Schymanski, S. J., Samaniego, L., Luce, C. H., Jackson, B. M., ... & Ceola, S. (2016).
718   Improving the theoretical underpinnings of process-based hydrologic models. Water Resources Research,
719   52(3), 2350-2365.

720 Cramer, W., Guiot, J., Fader, M., Garrabou, J., Gattuso, J. P., Iglesias, A., ... & Xoplaki, E. (2018). Climate change
721   and interconnected risks to sustainable development in the Mediterranean. Nature Climate Change, 8(11),
722   972-980.

723 Cui, X., Guo, X., Wang, Y., Wang, X., Zhu, W., Shi, J., ... & Gao, X. (2019). Application of remote sensing to water
724   environmental processes under a changing climate. Journal of Hydrology, 574, 892-902.

725 Zamir, A. R., Sax, A., Shen, W., Guibas, L. J., Malik, J., & Savarese, S. (2018). Taskonomy: Disentangling task
726   transfer learning. In Proceedings of the IEEE conference on computer vision and pattern recognition (pp.
727   3712-3722).

728 D'Amour, A., Heller, K., Moldovan, D., Adlam, B., Alipanahi, B., Beutel, A., ... & Sculley, D. (2020).
729   Underspecification presents challenges for credibility in modern machine learning. arXiv preprint
730   arXiv:2011.03395.

731 Dey, S., & Fuentes, O. (2020). Predicting solar x-ray flux using deep learning techniques. In 2020 international
732   joint conference on neural networks (ijcnn) (pp. 1–7).

733 Dembélé, M., Hrachowitz, M., Savenije, H. H., Mariéthoz, G., & Schaefli, B. (2020). Improving the predictive
734   skill of a distributed hydrological model by calibration on spatial patterns with multiple satellite data sets.
735   Water resources research, 56(1), e2019WR026085.

736 Dickey, D. A., & Pantula, S. G. (1987). Determining the order of differencing in autoregressive processes.
737   Journal of Business & Economic Statistics, 5(4), 455-461.

738 Dimitriadis, P., Koutsoyiannis, D., Iliopoulou, T., & Papanicolaou, P. (2021). A global-scale investigation of
739   stochastic similarities in marginal distribution and dependence structure of key hydrological-cycle processes.
740   Hydrology, 8(2), 59.

741 Durand, M., Gleason, C. J., Garambois, P. A., Bjerklie, D., Smith, L. C., Roux, H., ... & Vilmin, L. (2016). An
742   intercomparison of remote sensing river discharge estimation algorithms from measurements of river height,
743   width, and slope. Water Resources Research, 52(6), 4527-4549.

744 Durand, M., Chen, C., de Moraes Frasson, R. P., Pavelsky, T. M., Williams, B., Yang, X., & Fore, A. (2020). How
745   will radar layover impact SWOT measurements of water surface elevation and slope, and estimates of river
746   discharge?. Remote Sensing of Environment, 247, 111883.

747 Eck, D., & Schmidhuber, J. (2002). A first look at music composition using lstm recurrent neural networks. Istituto
748   Dalle Molle Di Studi Sull Intelligenza Artificiale, 103, 48.

749 Feng, D., Fang, K., & Shen, C. (2020). Enhancing streamflow forecast and extracting insights using long-short
750   term memory networks with data integration at continental scales. Water Resources Research, 56(9),
751   e2019WR026793.

752 Feng, D., Lawson, K., & Shen, C. (2021). Mitigating prediction error of deep learning streamflow models in large
753   data-sparse regions with ensemble modelling and soft data. Geophysical Research Letters, 48(14),
754   e2021GL092999.

755 Feng, D., Gleason, C. J., Yang, X., Allen, G. H., & Pavelsky, T. M. (2022). How have global river widths changed
756   over time?. Water Resources Research, 58(8), e2021WR031712.

757 Feng, D., Gleason, C. J., Lin, P., Yang, X., Pan, M., & Ishitsuka, Y. (2021). Recent changes to arctic river discharge.
758   Nature communications, 12(1), 1–9.

759 Feng, D., Gleason, C. J., Yang, X., & Pavelsky, T. M. (2019). Comparing discharge estimates made via the bam
760   algorithm in high-order arctic rivers derived solely from optical cubesat, landsat, and sentinel-2 data. Water
761   Resources Research, 55(9), 7753–7771.

762 Fraiwan, L., & Alkhodari, M. (2020). Investigating the use of uni-directional and bi-directional long short-term
763   memory models for automatic sleep stage scoring. Informatics in medicine unlocked, 20, 100370.

764 Frasson, R. P. D. M., Pavelsky, T. M., Fonstad, M. A., Durand, M. T., Allen, G. H., Schumann, G., ... & Yang, X.
765   (2019). Global relationships between river width, slope, catchment area, meander wavelength, sinuosity, and
766   discharge. Geophysical Research Letters, 46(6), 3252-3262.

767 Fry, T. J., & Maxwell, R. M. (2018). Using a distributed hydrologic model to improve the green infrastructure
768   parameterization used in a lumped model. Water, 10(12), 1756.

769 Fu, M., Fan, T., Ding, Z. A., Salih, S. Q., Al-Ansari, N., & Yaseen, Z. M. (2020). Deep learning data-intelligence
770   model based on adjusted forecasting window scale: application in daily streamflow simulation. IEEE Access,
771   8, 32632-32651.

772 Fujita, Koji. "Effect of precipitation seasonality on climatic sensitivity of glacier mass balance." Earth and Planetary
773   Science Letters 276.1-2 (2008): 14-19.

774 Furey, P. R., & Gupta, V. K. (2005). Effects of excess rainfall on the temporal variability of observed peak-discharge
775   power laws. Advances in Water Resources, 28(11), 1240-1253.

776 Ghojogh, B., & Crowley, M. (2019). The theory behind overfitting, cross validation, regularization, bagging, and
777   boosting: tutorial. arXiv preprint arXiv:1905.12787.

778 Gleason, C. J., & Hamdan, A. N. (2017). Crossing the (watershed) divide: satellite data and the changing politics of
779   international river basins. The Geographical Journal, 183, 2-15.

780 Gleason, C. J., & Smith, L. C. (2014). Toward global mapping of river discharge using satellite images and at-
781   many-stations hydraulic geometry. Proceedings of the National Academy of Sciences, 111(13), 4788–4791.

782 Gleason, C. J., & Durand, M. T. (2020). Remote sensing of river discharge: a review and a framing for the
783   discipline. Remote Sensing, 12(7), 1107.

784 Ghosh, S., Vinyals, O., Strope, B., Roy, S., Dean, T., & Heck, L. (2016). Contextual lstm (clstm) models for large
785   scale nlp tasks. arXiv preprint arXiv:1602.06291.

786 Goodfellow, I., Bengio, Y., & Courville, A. (2016). Deep learning. MIT press. (pp. 373-416)

787 Goldstein, R. (1995). Atmospheric limitations to repeat-track radar interferometry. Geophysical research letters,
788   22(18), 2517-2520.

789 Graves, A., & Schmidhuber, J. (2005). Framewise phoneme classification with bidirectional LSTM and other neural
790   network architectures. Neural networks, 18(5-6), 602-610.

791 Gorelick, N., Hancher, M., Dixon, M., Ilyushchenko, S., Thau, D., & Moore, R. (2017). Google Earth Engine:
792   Planetary-scale geospatial analysis for everyone. Remote sensing of Environment, 202, 18-27.

793 Gupta, H. V., & Kling, H. (2011). On typical range, sensitivity, and normalization of Mean Squared Error and Nash-
794   Sutcliffe Efficiency type metrics. Water Resources Research, 47(10).

795 Hagemann, M. W., Gleason, C. J., & Durand, M. T. (2017). BAM: Bayesian AMHG-Manning inference of discharge
796   using remotely sensed stream width, slope, and height. Water Resources Research, 53(11), 9692-9707.

797 Hinton, G. E., Srivastava, N., Krizhevsky, A., Sutskever, I., & Salakhutdinov, R. R. (2012). Improving neural
798   networks by preventing co-adaptation of feature detectors. arXiv preprint arXiv:1207.0580.

799 Hirpa, F. A., Gebremichael, M., Hopson, T. M., Wojick, R., & Lee, H. (2014). Assimilation of satellite soil moisture
800   retrievals into a hydrologic model for improving river discharge. Remote sensing of the terrestrial water cycle,
801   206, 319.

802 Hochreiter, S., & Schmidhuber, J. (1997). Long short-term memory. Neural computation, 9(8), 1735–1780.

803 Hosking, J. R. (1984). Modelling persistence in hydrological time series using fractional differencing. Water resources
804   research, 20(12), 1898-1908.

805 Hu, C., Wu, Q., Li, H., Jian, S., Li, N., & Lou, Z. (2018). Deep learning with a long short-term memory networks
806   approach for rainfall-runoff simulation. Water, 10(11), 1543.

807 Huang, Q., Long, D., Du, M., Han, Z., & Han, P. (2020). Daily continuous river discharge estimation for
808   ungauged basins using a hydrologic model calibrated by satellite altimetry: Implications for the SWOT
809   mission. Water Resources Research, 56(7), e2020WR027309.

810 Hsu, K.-l., Gupta, H. V., & Sorooshian, S. (1995). Artificial neural network modelling of the rainfall-runoff
811   process. Water resources research, 31(10), 2517– 2530.

812 Hu, Y., Huber, A., Anumula, J., & Liu, S. C. (2018). Overcoming the vanishing gradient problem in plain
813   recurrent networks. arXiv preprint arXiv:1801.06105.

814 Hunink, Eekhout, J., Vente, J., Contreras, S., Droogers, P., & Baille, A. (2017). Hydrological Modelling using
815   Satellite-Based Crop Coefficients: A Comparison of Methods at the Basin Scale. Remote Sensing, 9(2),
816   174. https://doi.org/10.3390/rs9020174

817 Immerzeel, W. W., Van Beek, L. P., & Bierkens, M. F. (2010). Climate change will affect the Asian water towers.
818   science, 328(5984), 1382-1385.

819 Ishitsuka, Y., Gleason, C. J., Hagemann, M. W., Beighley, E., Allen, G. H., Feng, D., ... & Pavelsky, T. M. (2021).
820   Combining optical remote sensing, McFLI discharge estimation, global hydrologic modelling, and data
821   assimilation to improve daily discharge estimates across an entire large watershed. Water Resources
822   Research, 57(3), e2020WR027794.

823 Jamshidian, M., & Mata, M. (2007). Advances in analysis of mean and covariance structure when data are
824   incomplete. In Handbook of latent variable and related models (pp. 21-44). North-Holland.

825 Jiang, D., & Wang, K. (2019). The role of satellite-based remote sensing in improving simulated streamflow: A
826   review. Water, 11(8), 1615.

827 Jones, J. A. (2000). Hydrologic processes and peak discharge response to forest removal, regrowth, and roads in
828   10 small experimental basins, western Cascades, Oregon. Water Resources Research, 36(9), 2621-2642.

829 Kahraman, A., Hou, P., Yang, G., & Yang, Z. (2021). Comparison of the effect of regularization techniques and
830   lookback window length on deep learning models in short term load forecasting. In 2021 international
831   top-level forum on engineering science and technology development strategy: 6th purple mountain forum
832   on smart grid protection and control.

833 Kabeja, C., Li, R., Guo, J., Rwatangabo, D. E. R., Manyifika, M., Gao, Z., ... & Zhang, Y. (2020). The impact of
834   reforestation induced land cover change (1990–2017) on flood peak discharge using HEC-HMS
835   hydrological model and satellite observations: a study in two mountain basins, China. Water, 12(5), 1347.

836 Kirchner, J. W. (2006). Getting the right answers for the right reasons: Linking measurements, analyses, and
837   models to advance the science of hydrology. Water Resources Research, 42(3).

838 Kittel, C. M., Arildsen, A. L., Dybkjær, S., Hansen, E. R., Linde, I., Slott, E., ... & Bauer-Gottwein, P. (2020).
839   Informing hydrological models of poorly gauged river catchments–a parameter regionalization and
840   calibration approach. Journal of Hydrology, 587, 124999.

841 Kompas, T., Pham, V. H., & Che, T. N. (2018). The effects of climate change on gdp by country and the global
842   economic gains from complying with the paris climate accord. Earth's Future, 6(8), 1153–1173.

843 Kratzert, F., Klotz, D., Herrnegger, M., Sampson, A. K., Hochreiter, S., & Nearing, G. S. (2019). Toward
844   improved predictions in ungauged basins: Exploiting the power of machine learning. Water Resources
845   Research, 55(12), 11344–11354.

846 Knoben, W. J. M., Freer, J. E., & Woods, R. A. (2019). Technical note: inherent benchmark or not? Comparing
847   Nash–Sutcliffe and Kling–Gupta efficiency scores. Hydrol Earth Syst Sc 23: 4323–4331.

848 Kratzert, F., Klotz, D., Shalev, G., Klambauer, G., Hochreiter, S., & Nearing, G.
849   (2019).Towards learning universal, regional, and local hydrological behaviors via machine learning applied to
850   large-sample datasets. Hydrology and Earth System Sciences, 23(12), 5089–5110.

851 Larnier, K., & Monnier, J. (2020). Hybrid Neural Network–Variational Data Assimilation algorithm to infer river
852 discharges from SWOT-like data. Nonlinear Processes in Geophysics Discussions, 1-30.

853 Lehner, F., Wood, A. W., Llewellyn, D., Blatchford, D. B., Goodbody, A. G., & Pappenberger, F. (2017). Mitigating
854 the impacts of climate nonstationarity on seasonal streamflow predictability in the US Southwest. Geophysical
855 Research Letters, 44(24), 12-208.

856 Lees, T., Reece, S., Kratzert, F., Klotz, D., Gauch, M., De Bruijn, J., ... & Dadson, S. (2021). Hydrological concept
857 formation inside long short-term memory (LSTM) networks. Hydrology and Earth System Sciences Discussions,
858 2021, 1-37.

859 Lin, P., Pan, M., Beck, H. E., Yang, Y., Yamazaki, D., Frasson, R., ... others (2019). Global reconstruction of
860   naturalized river flows at 2.94 million reaches. Water resources research, 55(8), 6499–6516.

861 Lim, S., Kim, S. J., Park, Y., & Kwon, N. (2021). A deep learning-based time series model with missing value
862   handling techniques to predict various types of liquid cargo traffic. Expert Systems with Applications, 184,
863   115532.

864 Long, M., Zhu, H., Wang, J., & Jordan, M. I. (2017, July). Deep transfer learning with joint adaptation networks.
865   In International conference on machine learning (pp. 2208-2217). PMLR.

866 Lundberg, S. M., & Lee, S. I. (2017). A unified approach to interpreting model predictions. Advances in neural
867   information processing systems, 30.

868 Lundberg, S. M., Erion, G., Chen, H., DeGrave, A., Prutkin, J. M., Nair, B., ... & Lee, S. I. (2020). From local
869   explanations to global understanding with explainable AI for trees. Nature machine intelligence, 2(1), 56-
870   67.

871 M. Hrachowitz, H.H.G. Savenije, G. Blöschl, J.J. McDonnell, M. Sivapalan, J.W. Pomeroy, B. Arheimer, T.
872   Blume, M.P. Clark, U. Ehret, F. Fenicia, J.E. Freer, A. Gelfan, H.V. Gupta, D.A. Hughes, R.W. Hut, A.
873   Montanari, S. Pande, D. Tetzlaff, P.A. Troch, S. Uhlenbrook, T. Wagener, H.C. Winsemius, R.A. Woods,
874   E. Zehe & C. Cudennec (2013) A decade of Predictions in Ungauged Basins (PUB)—a review,
875   Hydrological Sciences Journal, 58:6, 1198-1255, DOI: 10.1080/02626667.2013.803183

876 Ma, K., Feng, D., Lawson, K., Tsai, W. P., Liang, C., Huang, X., ... & Shen, C. (2021). Transferring hydrologic
877   data across continents–leveraging data-rich regions to improve hydrologic prediction in data-sparse
878   regions. Water Resources Research, 57(5), e2020WR028600.

879 Mai, J., Craig, J. R., Tolson, B. A., & Arsenault, R. (2022). The sensitivity of simulated streamflow to individual
880   hydrologic processes across North America. Nature Communications, 13(1), 1-11.

881   Marcinkevičs, R., & Vogt, J. E. (2020). Interpretability and explainability: A machine learning zoo mini-tour.
882   arXiv preprint arXiv:2012.01805.

883   Marshall, L., Nott, D., & Sharma, A. (2005). Hydrological model selection: A Bayesian alternative. Water
884   resources research, 41(10).

885   Mastorakis, G. (2018). Human-like machine learning: limitations and suggestions. arXiv preprint
886   arXiv:1811.06052.

887   McLaughlin, D. (1995). Recent developments in hydrologic data assimilation. Reviews of Geophysics, 33(S2),
888   977-984.

889   Mhaskar, H. N., & Micchelli, C. A. (1993). How to choose an activation function. Advances in neural
890   information processing systems, 6.

891   Moore, I. D., Grayson, R. B., & Ladson, A. R. (1991). Digital terrain modelling: a review of hydrological,
892   geomorphological, and biological applications. Hydrological processes, 5(1), 3-30.}

893   Montanari, A., & Koutsoyiannis, D. (2012). A blueprint for process-based modelling of uncertain hydrological
894   systems. Water Resources Research, 48(9).

895   Muhammad, A., Evenson, G. R., Stadnyk, T. A., Boluwade, A., Jha, S. K., & Coulibaly, P. (2019). Impact of
896   model structure on the accuracy of hydrological modelling of a Canadian Prairie watershed. Journal of
897   Hydrology: Regional Studies, 21, 40-56.

898   Muhebwa, A., Wi, S., Gleason, C. J., & Taneja, J. (2021). Towards improved global river discharge prediction in
899   ungauged basins using machine learning and satellite observations.

900   Nash, J. E., & Sutcliffe, J. V. (1970). River flow forecasting through conceptual models part i—a discussion of
901   principles. Journal of hydrology, 10(3), 282– 290.

902   Nearing, G. S., Kratzert, F., Sampson, A. K., Pelissier, C. S., Klotz, D., Frame, J. M., ... & Gupta, H. V. (2021).
903   What role does hydrological science play in the age of machine learning?. Water Resources Research,
904   57(3), e2020WR028091.

905   Nepal, S., Flügel, W. A., & Shrestha, A. B. (2014). Upstream-downstream linkages of hydrological processes in
906   the Himalayan region. Ecological Processes, 3(1), 1-16.

907   Ntegeka, V., Baguis, P., Roulin, E., & Willems, P. (2014). Developing tailored climate change scenarios for
908   hydrological impact assessments. Journal of Hydrology, 508, 307-321.

909   Ortiz-Bobea, A., Ault, T. R., Carrillo, C. M., Chambers, R. G., & Lobell, D. B. (2021). Anthropogenic climate
910   change has slowed global agricultural productivity growth. Nature Climate Change, 11(4), 306-312.

911   Oubanas, H., Gejadze, I., Malaterre, P. O., Durand, M., Wei, R., Frasson, R. P., & Domeneghetti, A. (2018).
912   Discharge estimation in ungauged basins through variational data assimilation: The potential of the
913   SWOT mission. Water Resources Research, 54(3), 2405-2423.

914   Oubanas, H., Gejadze, I., Malaterre, P. O., & Mercier, F. (2018). River discharge estimation from synthetic
915   SWOT-type observations using variational data assimilation and the full Saint-Venant hydraulic model.
916   Journal of Hydrology, 559, 638-647.

917   Oudin, L., Andréassian, V., Perrin, C., Michel, C., & Le Moine, N. (2008). Spatial proximity, physical similarity,
918   regression and ungaged catchments: A comparison of regionalization approaches based on 913 French
919   catchments. Water Resources Research, 44(3).

920   Ouyang, W., Lawson, K., Feng, D., Ye, L., Zhang, C., & Shen, C. (2021). Continental-scale streamflow
921   modelling of basins with reservoirs: Towards a coherent deep-learning-based strategy. Journal of
922   Hydrology, 599, 126455.

923   Pagliero, L., Bouraoui, F., Diels, J., Willems, P., & McIntyre, N. (2019). Investigating regionalization techniques
924   for large-scale hydrological modelling. Journal of hydrology, 570, 220-235.

925   Pant, N., Semwal, P., Khobragade, S. D., Rai, S. P., Kumar, S., Dubey, R. K., ... & Ahluwalia, R. S. (2021). Tracing
926   the isotopic signatures of cryospheric water and establishing the altitude effect in Central Himalayas: A tool
927   for cryospheric water partitioning. Journal of Hydrology, 595, 125983.

928   Pokhrel, Y., Shin, S., Lin, Z., Yamazaki, D., & Qi, J. (2018). potential disruption of flood dynamics in the Lower
929   Mekong River basin due to upstream flow regulation. Scientific reports, 8(1), 1-13.

930   Pool, S., & Seibert, J. (2021). Gauging ungauged catchments–Active learning for the timing of point discharge
931   observations in combination with continuous water level measurements. Journal of Hydrology, 598, 126448.

932   Patz, J. A., Campbell-Lendrum, D., Holloway, T., & Foley, J. A. (2005). Impact of regional climate change on
933   human health. Nature, 438(7066), 310-317.

934   Pilz, T., Francke, T., Baroni, G., & Bronstert, A. (2020). How to Tailor My Process-Based Hydrological Model?
935   Dynamic Identifiability Analysis of Flexible Model Structures. Water resources research, 56(8),
936   e2020WR028042.

937   Rácz, A., Bajusz, D., & Héberger, K. (2021). Effect of dataset size and train/test split ratios in QSAR/QSPR
938   multiclass classification. Molecules, 26(4), 1111.

939   Rao, R. B., Fung, G., & Rosales, R. (2008, April). On the dangers of cross-validation. An experimental evaluation. In
940   Proceedings of the 2008 SIAM international conference on data mining (pp. 588-596). Society for Industrial
941   and Applied Mathematics.

942   Ramachandran, P., Zoph, B., & Le, Q. V. (2017). Searching for activation functions. arXiv preprint
943   arXiv:1710.05941.

944   Refaeilzadeh, P., Tang, L., & Liu, H. (2009). Cross-validation. Encyclopedia of database systems, 5, 532-538.

945   Rodell, M., P.R. Houser, U. Jambor, J. Gottschalck, K. Mitchell, C. Meng, K. Arsenault, B. Cosgrove, J. Radakovich,
946   M. Bosilovich, J.K. Entin, J.P. Walker, D. Lohmann, and D. Toll, 2004: The Global Land Data Assimilation
947   System, Bull. Amer. Meteor. Soc., 85, 381-394

948   Royall, D. (2021). Land-use impacts on the hydrogeomorphology of small watersheds.

949   Scown, M. W. (2020). The sustainable development goals need geoscience. Nature Geoscience, 13(11), 714-715.

950   Seifert, A., & Rasp, S. (2020). Potential and limitations of machine learning for modelling warm-rain cloud
951   microphysical processes. Journal of Advances in Modelling Earth Systems, 12(12), e2020MS002301.

952   Sheffield, J., Wood, E. F., Pan, M., Beck, H., Coccia, G., Serrat-Capdevila, A., & Verbist, K. (2018). Satellite
953   remote sensing for water resources management: Potential for supporting sustainable development in data-
954   poor regions. Water Resources Research, 54(12), 9724-9758.

955   Shen, C. (2018). A transdisciplinary review of deep learning research and its relevance for water resources
956   scientists. Water Resources Research, 54(11), 8558-8593.

957   Shen, H., Tolson, B. A., & Mai, J. (2022). Time to Update the Split-Sample Approach in Hydrological Model
958   Calibration. Water Resources Research, e2021WR031523.

959   Siami-Namini, S., Tavakoli, N., & Namin, A. S. (2019, December). The performance of LSTM and BiLSTM in
960   forecasting time series. In 2019 IEEE International Conference on Big Data (Big Data) (pp. 3285-3292).
961   IEEE.

962   Sidle, R. C., Gomi, T., Usuga, J. C. L., & Jarihani, B. (2017). Hydrogeomorphic processes and scaling issues in the
963   continuum from soil pedons to catchments. Earth-Science Reviews, 175, 75-96.

964   Stone, M. (1978). Cross-validation: A review. Statistics: A Journal of Theoretical and Applied Statistics, 9(1), 127-
965   139.

966   Srivastava, N., Hinton, G., Krizhevsky, A., Sutskever, I., & Salakhutdinov, R. (2014). Dropout: a simple way to
967   prevent neural networks from overfitting. The journal of machine learning research, 15(1), 1929-1958.

968   Srivastava, N., Mansimov, E., & Salakhudinov, R. (2015, June). Unsupervised learning of video representations
969   using lstms. In International conference on machine learning (pp. 843-852). PMLR.

970   Sun, A. Y., Jiang, P., Mudunuru, M. K., & Chen, X. (2021). Explore Spatio-Temporal Learning of Large Sample
971   Hydrology Using Graph Neural Networks. Water Resources Research, 57(12), e2021WR030394.

972   Tan, C., Sun, F., Kong, T., Zhang, W., Yang, C., & Liu, C. (2018, October). A survey on deep transfer learning. In
973   International conference on artificial neural networks (pp. 270-279). Springer, Cham.

974   Thyer, M., Renard, B., Kavetski, D., Kuczera, G., Franks, S. W., & Srikanthan, S. (2009). Critical evaluation of
975   parameter consistency and predictive uncertainty in hydrological modelling: A case study using Bayesian
976   total error analysis. Water Resources Research, 45(12).

977   Tian, S., Tregoning, P., Renzullo, L. J., van Dijk, A. I., Walker, J. P., Pauwels, V. R., & Allgeyer, S. (2017).
978   Improved water balance component estimates through joint assimilation of GRACE water storage and
979   SMOS soil moisture retrievals. Water Resources Research, 53(3), 1820-1840.

980   Tran, Q. Q., De Niel, J., & Willems, P. (2018). Spatially distributed conceptual hydrological model building: A
981   generic top-down approach starting from lumped models. Water Resources Research, 54(10), 8064-8085.

982   Tsai, W. P., Feng, D., Pan, M., Beck, H., Lawson, K., Yang, Y., ... & Shen, C. (2021). From calibration to
983   parameter learning: Harnessing the scaling effects of big data in geoscientific modelling. Nature
984   communications, 12(1), 1-13.

985   Volpi, E., Di Lazzaro, M., Bertola, M., Viglione, A., & Fiori, A. (2018). Reservoir effects on flood peak discharge at
986   the catchment scale. Water Resources Research, 54(11), 9623-9636.

987   Wager, S., Wang, S., & Liang, P. S. (2013). Dropout training as adaptive regularization. Advances in neural
988   information processing systems, 26.

989 Wagener, T., & Montanari, A. (2011). Convergence of approaches toward reducing uncertainty in predictions in
990   ungauged basins. Water Resources Research, 47(6). Wu, X., Jeuland, M., & Whittington, D. (2016). Does
991   political uncertainty affect water resources development? the case of the eastern nile. Policy and Society, 35(2),
992   151–163.

993 Wang, H., Cao, L., & Feng, R. (2021). Hydrological Similarity-Based Parameter Regionalization under Different
994   Climate and Underlying Surfaces in Ungauged Basins. Water, 13(18), 2508.

995 Wang, H., Cheng, Q., Wang, T., Zhang, G., Wang, Y., Li, X., & Jiang, B. (2021). Layover Compensation Method for
996   Regional Spaceborne SAR Imagery Without GCPs. IEEE Transactions on Geoscience and Remote Sensing,
997   59(10), 8367-8381.

998 Wanner, J., Herm, L. V., & Janiesch, C. (2020). How much is the black box? The value of explainability in machine
999   learning models.

1000 Wu, H., & Prasad, S. (2017). Convolutional recurrent neural networks forhyperspectral data classification. Remote
1001   Sensing, 9(3), 298.

1002 Wu, W., May, R. J., Maier, H. R., & Dandy, G. C. (2013). A benchmarking approach for comparing data splitting
1003   methods for modelling water resources parameters using artificial neural networks. Water Resources
1004   Research, 49(11), 7598-7614.

1005 Xie, K., Liu, P., Zhang, J., Han, D., Wang, G., & Shen, C. (2021). Physics-guided deep learning for rainfall-runoff
1006   modelling by considering extreme events and monotonic relationships. Journal of Hydrology, 603, 127043.

1007 Yamazaki, D., Ikeshima, D., Sosa, J., Bates, P. D., Allen, G. H., & Pavelsky, T. M. (2019). MERIT Hydro: A high-
1008   resolution global hydrography map based on latest topography dataset. Water Resources Research, 55(6),
1009   5053-5073.

1010 Yang, X., Magnusson, J., Huang, S., Beldring, S., & Xu, C. Y. (2020). Dependence of regionalization methods on the
1011   complexity of hydrological models in multiple climatic regions. Journal of Hydrology, 582, 124357.

1012 Yin, W., Kann, K., Yu, M., & Schütze, H. (2017). Comparative study of CNN and RNN for natural language
1013   processing. arXiv preprint arXiv:1702.01923.

1014 Ying, X. (2019, February). An overview of overfitting and its solutions. In Journal of physics: Conference series
1015   (Vol. 1168, p. 022022). IOP Publishing.

1016 Yoshida, T., Hanasaki, N., Nishina, K., Boulange, J., Okada, M., & Troch, P. A. Inference of parameters for a global
1017   hydrological model: Identifiability and predictive uncertainties of climate-based parameters. Water Resources
1018   Research, e2021WR030660.

1019 Yu, T., & Zhu, H. (2020). Hyper-parameter optimization: A review of algorithms and applications. arXiv preprint
1020   arXiv:2003.05689.

1021 Yu, C., Li, Z., Penna, N. T., & Crippa, P. (2018). Generic atmospheric correction model for interferometric
1022   synthetic aperture radar observations. Journal of Geophysical Research: Solid Earth, 123(10), 9202-9222.

1023 Zhou, Z., Ren, J., He, X., & Liu, S. (2021). A comparative study of extensive machine learning models for predicting
1024   long-term monthly rainfall with an ensemble of climatic and meteorological predictors. Hydrological
1025   Processes, 35(11), e14424.

Zhuang, F., Qi, Z., Duan, K., Xi, D., Zhu, Y., Zhu, H., ... & He, Q. (2020). A comprehensive survey on transfer learning. Proceedings of the IEEE, 109(1), 43-76.

Zounemat-Kermani, M., Batelaan, O., Fadaee, M., & Hinkelmann, R. (2021). Ensemble machine learning paradigms in hydrology: A review. Journal of Hydrology, 598, 126266.

Ma, C., Dai, G., & Zhou, J. (2021). Short-term traffic flow prediction for urban road sections based on time series analysis and LSTM_BILSTM method. IEEE Transactions on Intelligent Transportation Systems, 23(6), 5615-5624.

Atef, S., & Eltawil, A. B. (2020). Assessment of stacked unidirectional and bidirectional long short-term memory networks for electricity load forecasting. Electric Power Systems Research, 187, 106489.

Althelaya, K. A., El-Alfy, E. S. M., & Mohammed, S. (2018, April). Evaluation of bidirectional LSTM for short-and long-term stock market prediction. In 2018 9th international conference on information and communication systems (ICICS) (pp. 151-156). IEEE.

Siami-Namini, S., Tavakoli, N., & Namin, A. S. (2019). A comparative analysis of forecasting financial time series using arima, lstm, and bilstm. arXiv preprint arXiv:1911.09512.

Shrestha, S., Bae, D. H., Hok, P., Ghimire, S., & Pokhrel, Y. (2021). Future hydrology and hydrological extremes under climate change in Asian river basins. Scientific reports, 11(1), 17089.

Leng, G., Tang, Q., & Rayburg, S. (2015). Climate change impacts on meteorological, agricultural and hydrological droughts in China. Global and Planetary Change, 126, 23-34.

Tabari, H. (2020). Climate change impact on flood and extreme precipitation increases with water availability. Scientific reports, 10(1), 13768.
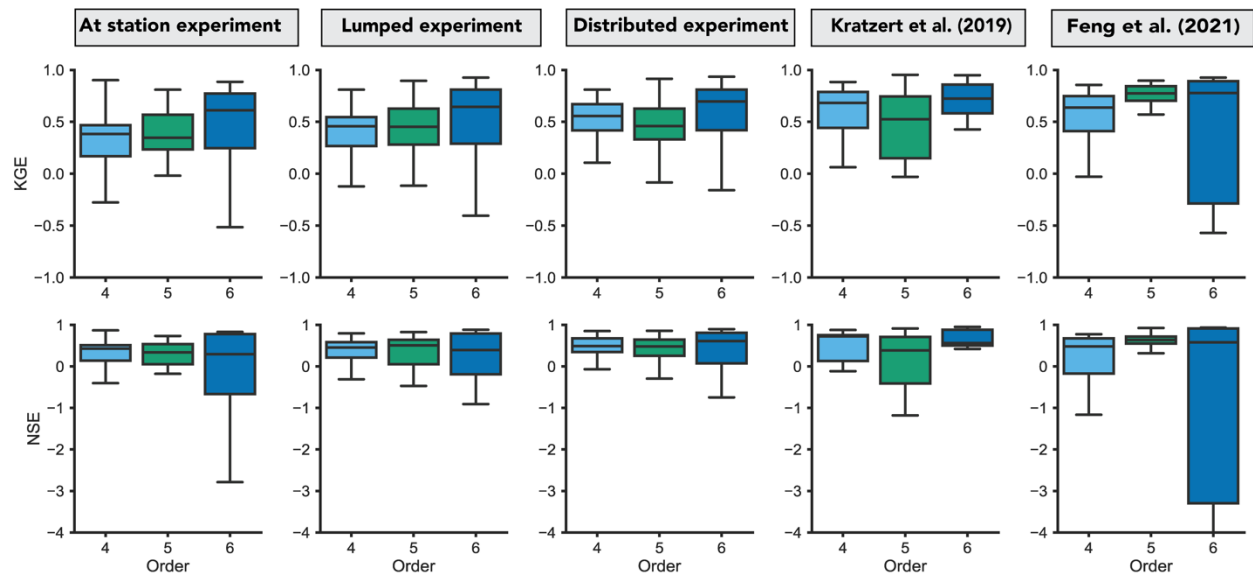
Appendix

Figure S1: Left to right: Distribution comparisons of selected metrics on held-out predictions for all experiments (i.e., at-station, lumped, and distributed experiments) and literature models: Kratzert et al. (2019) and Feng et al. (2021). Note that distributions for seventh and eighth orders are not included due to the limited gauge stations in the training set.
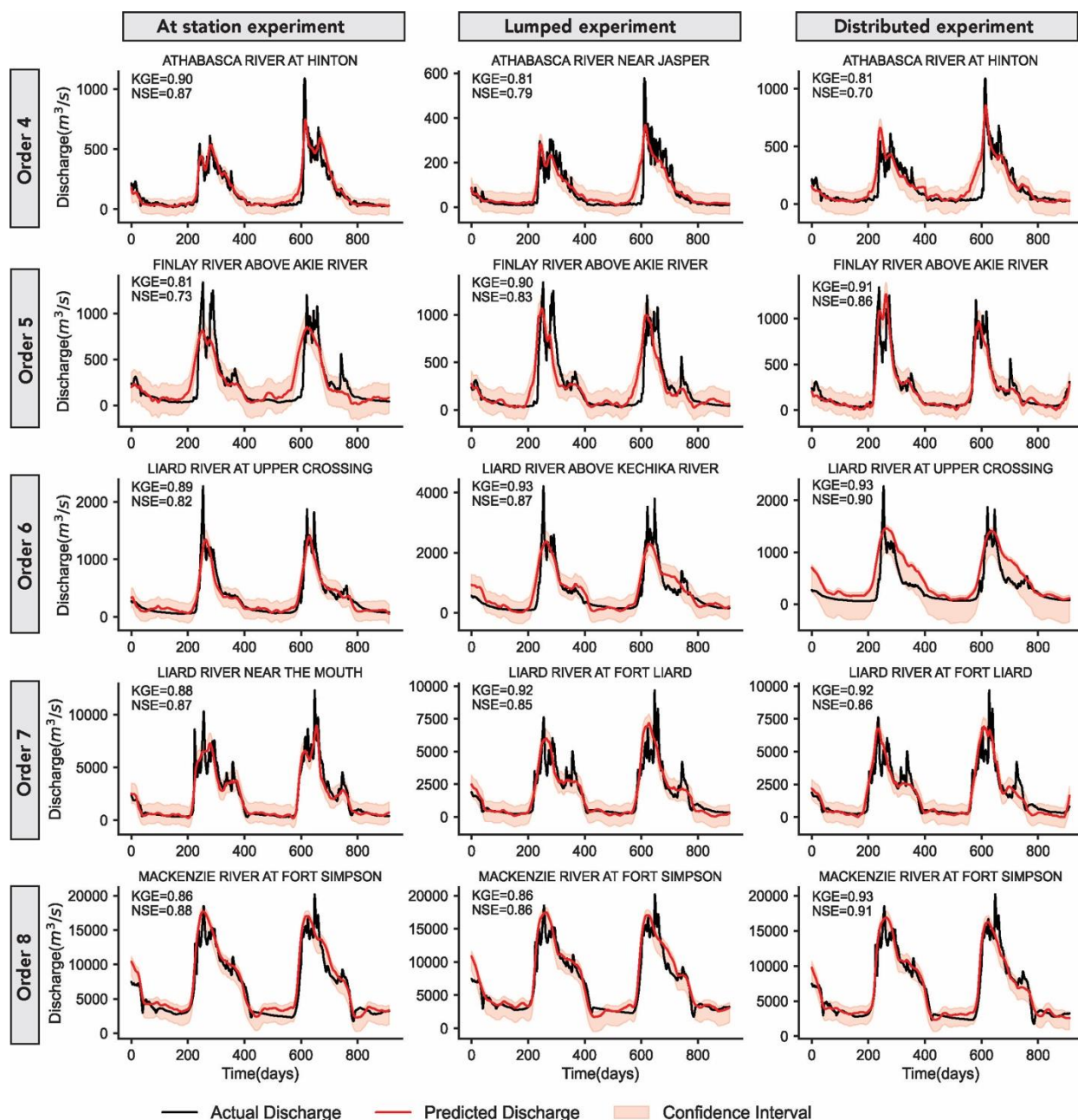
Figure S2: Left to right: Representative hydrographs showing the best performing models in each of the experiments; At-station (left), lumped (middle), and distributed (right) experiments across the defined orders, i.e., from order 4 (top) to order 8 (bottom). Here, we plot hydrographs for the first 2.5 years.

Table 2: Summary of variables used as input features to the LSTM model.

Variable name	Description	Unit
Discharge	In-situ daily river discharge at a gauge station	m^3s^{-1}
Albedo	Albedo	%
Avg_Skin_Temp	Average surface skin temperature	K

PlantCanopyWater	Plant canopy surface water	Kg/m²
CanopyWaterEvpn	Canopy water evaporation	W/m²
DirectEvonBareSoil	Direct evaporation free bare soil	W/m²
Evapotranspn	Evapotranspiration	Kg/m²//s
LngWaveRadFlux	Downward long-wave radiation flux	W/m²
NetRadFlux	Net long-wave radiation flux	W/m²
PotEvpnRate	Potential Evaporation rate	W/m²
Pressure	Pressure	Pa
SpecHmd	Specific humidity	kg/kg
HeatFlux	Heat flux	W/m²
Sen.HtFlux	Sensible heat net flux	W/m²
LtHeat	Latent heat net flux	W/m²
StmSurfRunoff	Storm surface runoff	kg/m²
BsGndWtrRunoff	Baseflow-groundwater runoff	kg/m²
SnowMelt	Snow melt	kg/m²
TotalPcpRate	Total precipitation rate	kg/m²/s
RainPcpRate	Rain precipitation rate	kg/m²/s
RootZoneSoilMstr	Root zone soil moisture	kg/m²
SnowDepthWtrEq	Snow depth water Equivalent	W/m²
DwdShtWvRadFlux	Downward short-wave radiation flux	m
SnowDepth	Snow depth	kg/m²/s
SnowPcpRate	Snow precipitation rate	kg/m²
SoilMst10	Soil moisture (0-10) cm	kg/m²
SoilMst40	Soil moisture (10-40) cm	kg/m²
SoilMst100	Soil moisture (40-100) cm	kg/m²
SoilMst200	Soil moisture (100-200) cm	kg/m²
SoilTmp10	Soil temperature (0-10) cm	K
SoilTmp40	Soil temperature (10-40) cm	K
SoilTmp100	Soil temperature (40-100) cm	K
SoilTmp200	Soil temperature (100-200) cm	K
NetShtWvRadFlux	Net short wave radiation flux	W/m²
AirTemp	Air temperature	K
Tspn	Transpiration	W/m²
WindSpd	Windspeed	m/s
	Reach width	
	Stream length	
	Bed slope	
	Sinuosity	
	Upstream Area	
	Length Dir	
	Stream Drop	

	Mean width	
	Max Width	

1059