

1 **Influence of Boulders on Channel Width and Slope: Field Data and Theory**

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11 **Abstract**

12 Large boulders with a diameter of up to several tens of meters are globally observed in mountainous bedrock
13 channel environments. Recent theories suggest that high concentrations of boulders are associated with
14 changes in channel morphology. However, data are scarce and ambiguous, and process-related studies are
15 limited. Here we present data from the Liwu River, Taiwan, showing that channel width and slope increase
16 with boulder concentration. We apply two mass balance principles of bedrock erosion and sediment
17 transport and develop a theory to explain the steepening and widening trends. Five mechanisms are
18 considered and compared to the field data. The cover effect by immobile boulders is found to have no
19 influence on channel width. Channel width can partially be explained by boulder control on the tools effect
20 and on the partitioning of the flow shear stress. However, none of the mechanisms we explored can
21 adequately explain the scattered width data, potentially indicating a long-timescale adjustment of channel
22 width to boulder input. Steepening can be best described by assuming a reduction of sediment transport
23 efficiency with boulder concentration. We find that boulders represent a significant perturbation to the
24 fluvial landscape. Channels tend to adjust to this perturbation leading to a new morphology that differs
25 from boulder-free channels. The general approach presented here can be further expanded to explore the
26 role of other boulder-related processes.

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33 **Key Points**

- 34 • Reach-scale bedrock channel width and sediment-bed slope increase with boulder-concentration in
35 the Liwu River, Taiwan.
- 36 • Reduction of transport efficiency due to boulders best explains the increase in slope in boulder-bed
37 channels.
- 38 • Models incompatibility to account for scattered width data could imply long adjustment timescale
39 to boulder input.

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43 **Plain Language Summary**

44 Boulders are significant features in mountainous landscapes and can be found on hillslopes and river beds.
45 The Liwu River, Taiwan, exhibits boulders with sizes of tens of meters, which are probably rarely mobile
46 during floods. Channel segments that host large concentrations of boulders are generally wider and steeper,
47 offering an opportunity to examine the roles of boulders in shaping the geometry of the channel. Here we
48 use two fundamental principles related to the mass balance of (1) the riverbed rock eroded by pebble
49 impacts and (2) pebble transport downstream during floods to develop a set of equations that predict the
50 slope and width behavior as a result of boulder presence. The increase of slope with more boulders can be
51 explained by assuming that high concentrations of boulders inhibit the rate of the transported pebbles by
52 causing them to, for example, take longer paths. A fraction of the scattered width data can be accounted for
53 by increasing friction forces between the water flow and boulders and by increasing the rate of sediment
54 impact between boulders due to a reduction in the free riverbed space. This work demonstrates the
55 significant role of boulders in shaping landscapes.

56 1. Introduction

57 Boulders are ubiquitous in mountainous landscapes responding to large magnitude tectonic
58 perturbations and extreme variability of climatic conditions (Shobe et al., 2021). Boulders with a wide range
59 of diameters, between tens of centimeters and a few tens of meters, can be found on hillslopes (e.g., Bennett
60 et al., 2016; Finnegan et al., 2019; Shobe et al., 2020) and in rivers (e.g., Bathurst, 1996; Pagliara and
61 Chiavaccini, 2006)(Fig. 1). While the definition of a boulder varies among different studies, here boulders
62 are defined as the largest and least mobile grains in a landscape (Shobe et al., 2021). Much focus has been
63 given to the effects of small to intermediate size boulders, with diameters of tens of centimeters to few
64 meters, on channel hydraulics, channel geometry, and sediment transport (e.g., Carling et al., 2002; Nitsche
65 et al., 2011). Small to intermediate size boulders are commonly found in steep alluvial channels such as
66 cascades and step-pools (Montgomery and Buffington, 1997) and in mountainous torrents, where they are
67 thought to play a significant role in modifying bedload transport rates and patterns (Yager et al., 2007;
68 Nitsche et al., 2011; Rickenmann and Recking, 2011), flow structure and velocity (Canovaro et al., 2007;
69 Nitsche et al., 2012) and channel bed roughness (e.g., Schneider et al., 2015; Johnson, 2017).

70 A series of recent studies explored the morphological effects of larger boulders, a few meters and more
71 in diameter, which are more common in bedrock rivers (Cook et al., 2018; Shobe et al., 2020, 2021). Such
72 large boulders have been argued to be immobile for prolonged durations with expected substantial impacts
73 on channel hydraulics and channel geometry and long-term geomorphic functionality (Haviv, 2007; Huber
74 et al., 2020; Shobe et al., 2021). The emplacement of large boulders is associated with glacial lake outburst
75 floods (Cook et al., 2018), rockfalls, debris flows, landslides, and glacial erratics (e.g., Jouvét et al., 2017;
76 Polvi, 2021). In addition to their hypothesized effects on landscape evolution (e.g., Shobe et al., 2016), the
77 role of boulders as geohazards (Kean et al., 2019; Dini et al., 2021; Shobe et al., 2021) has recently been
78 recognized. Like changes in tectonics and climate, boulder emplacement in rivers can be regarded as a
79 disturbance to the fluvial system, forcing its geometry to adjust in response to the new hydraulic conditions
80 set by the large boulders. Boulders may affect the scaling relations between channel steepness and
81 catchment-scale erosion rate (Shobe et al., 2018) in comparison to those expected for boulder-free channels
82 (e.g., Lague et al., 2005; DiBiase et al., 2010; DiBiase and Whipple, 2011). Despite these recent insights,
83 the effects of large immobile boulders on channel geometry, especially channel width, have not been
84 systematically studied, and the processes involved in channel geometrical modifications in response to large
85 boulders emplacement have mostly remained unexplored.

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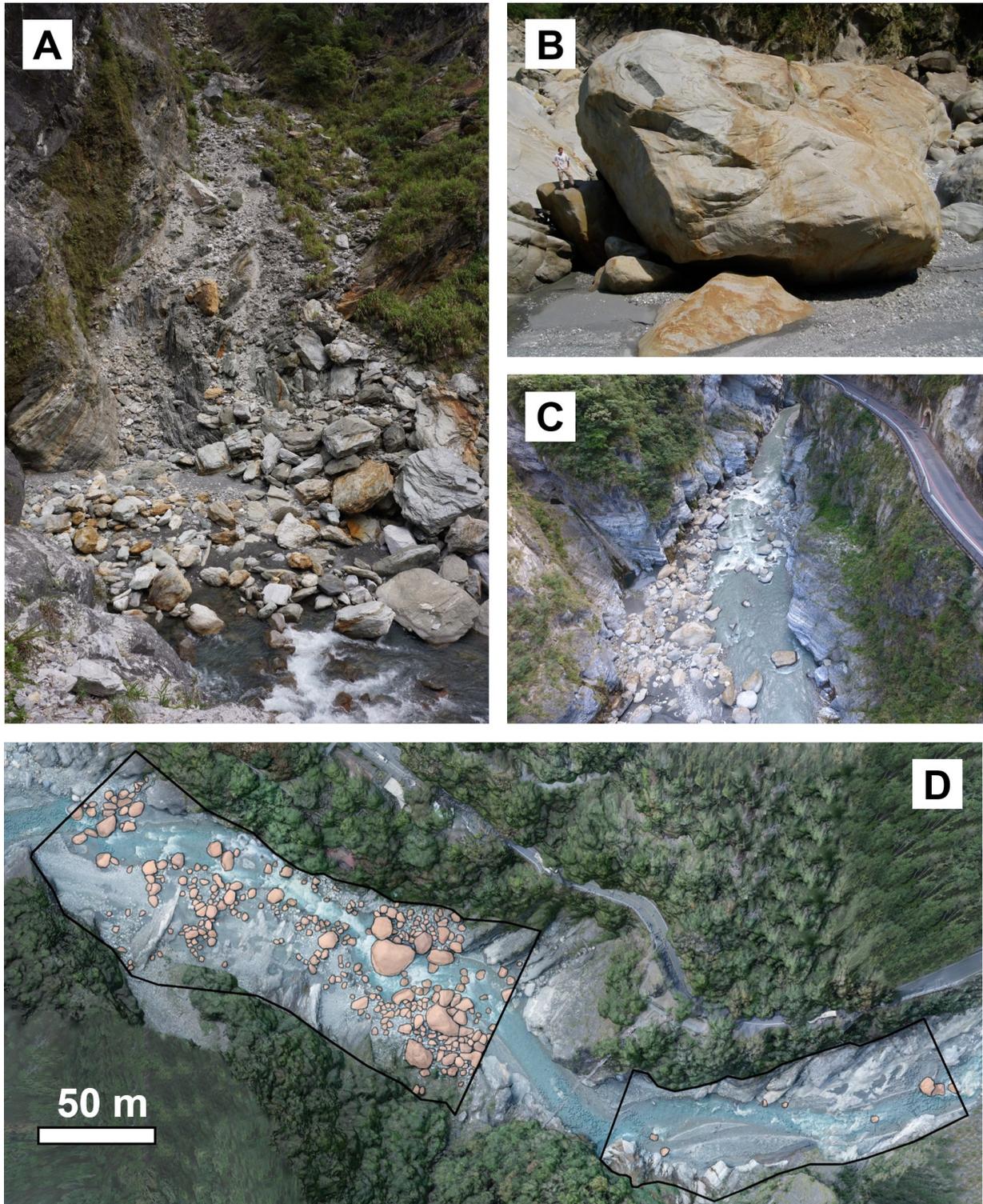


Figure 1: Field photographs from the Liwu River, Taiwan, showing different bed morphologies associated with large boulders. (A) Boulders placed on a hillslope debris channel in the Liwu, indicating an adjacent source of boulders. (B) A large (~15–20 m) sized boulder downstream of the Marble gorge. Note the person on the left for scale. (Photograph courtesy: Andrew Wilson). (C) Field evidence for variation in channel width and the relation to boulders in the Taroko Marble gorge. Moving downstream (towards the upper part of the picture), the gorge narrows as boulder concentration decreases. (D) Two neighboring channel reaches with the same drainage area but differing in width and boulder-concentration. The black line delineates the channel reach (as the black line in Fig. 2) and the red polygons are boulders with a diameter larger than 2 m.

89 Here, we explore the hypothesis that increasing boulder concentration can cause channels to widen and
90 steepen. We collected field data of channel geometry, morphology, and boulder characteristics. The data
91 are based on field and remote sensing observations from the Liwu River in Taiwan, where boulders with
92 diameters of up to 25 meters are ubiquitous on the channel bed along various river reaches, differing in
93 drainage area and geometry. Our goals are to (1) study the relationship between channel slope, width, and
94 boulder concentration and (2) theoretically identify the processes linking these variables. To achieve the
95 second goal, we focus on the influence of boulders on bedrock erosion and sediment transport and describe
96 their effects using conceptual arguments and empirical relations. We establish a suite of mechanisms that
97 relate immobile boulders to bedrock channels' steady-state width and slope. We treat each mechanism
98 independently, discuss the trends it predicts, and compare them against field observations. In the following,
99 we review the literature concerning flow hydraulics induced by boulders, the effects of boulders on
100 sediment transport processes, and the state-of-the-art regarding the channel adjustments in the presence of
101 large boulders.

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103 **2. Background for Boulder Control on Channel Geometry**

104 **2.1. Boulder Effects on Hydraulics and Sediment Transport**

105 Boulders are macro-roughness elements, which enhance flow resistance and alter the flow structure
106 (Nitsche et al., 2011). For example, in mountain streams with relatively shallow flows, boulders exert drag
107 forces on the flow, violating the classic view of a logarithmic velocity profile (e.g., Wiberg and Smith,
108 1991; Canovaro et al., 2007). Due to the complex three-dimensional flow structure, the spatial distribution
109 of shear stresses significantly varies in the vicinity of boulders, causing local variations in sediment
110 transport (Papanicolaou et al., 2012; Papanicolaou and Tsakiris, 2017). Boulders modify flow patterns
111 around them, such as turbulence intensity, and promote flow accelerations and decelerations (e.g., Tsakiris
112 et al., 2014). In high relative submergence flows, where the water depth is much greater than the boulder
113 diameter, the near-wake zone of a boulder becomes a zone of flow reversals and decelerations (e.g., Dey et
114 al., 2011). It is, thus, expected that such flow regimes favor sediment deposition and clustering downstream
115 of boulders (e.g., Papanicolaou and Kramer, 2006).

116 Boulders and large clasts are thought to reduce the available shear stress for sediment motion (e.g.,
117 Buffington and Montgomery, 1997). Coupling theory and flume experiments, Yager et al. (2007) suggested
118 that the drag exerted by immobile boulders could explain why traditional transport equations overpredict
119 bedload fluxes by orders of magnitude. Canovaro et al. (2007) designed flume experiments with different
120 portions of boulder concentrations, demonstrating a humped relationship between the percentage of drag
121 and total shear stress versus boulder concentration. For small boulder concentration values, the drag force
122 increased logarithmically until it peaked. The drag force decreased linearly with a further boulder
123 concentration increase until it dropped to zero when boulders fully covered the bed. With the strong
124 dependence of bedload transport on the available shear stress (e.g., Nitsche et al., 2011), these results
125 strengthen the contention that bedload flux is reduced in boulder-bed channels.

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127 **2.2. Boulder-bed Bedrock Channels and Relationships with Channel Slope and Width**

128 Various studies reported links between boulders and channel morphology (e.g., Montgomery and
129 Buffington, 1997; Lenzi, 2001; Turowski et al., 2009b; Thaler and Covington, 2016; Cook et al., 2018;
130 Shobe et al., 2018, 2020). Recent investigations identified a positive relationship between boulders and
131 channel steepness (Thaler and Covington, 2016) and slope (Shobe et al., 2020) in bedrock channels. Steady-
132 state bedrock channel morphology is assumed to control long-term river bedrock erosion adjustment to the
133 long-term uplift rate (e.g., Whipple and Tucker, 1999). When the uplift rate changes, the erosion rate
134 responds by adjusting the river profile (e.g., Whipple, 2004; Lague et al., 2005) and cross-section geometry
135 (e.g., Turowski et al., 2009a; Yanites, 2018; Turowski, 2020). Assuming immobility of large boulders,

136 Shobe et al. (2020) exploited this notion to argue that boulders hinder erosion by protecting the bedrock
137 channel bed. Their model predicts that a boulder-bed channel would consequently steepen to compensate
138 for the reduced erosion. Immobile boulders were also argued to be consequential for changes in bedrock
139 channel width. Shobe et al. (2020) tested the influence of the proximity of the boulder delivery point (e.g.,
140 landslides scars) on the width coefficient, i.e., width normalized by drainage area (e.g., Lague, 2014) and
141 found contrasting results. Accordingly, conclusive data and a general theory of boulder influence on
142 bedrock channel width are still missing.

143 Understanding how boulders influence channel morphology in bedrock rivers requires insights into the
144 process of bedrock erosion and sediment transport. The slope of bedrock channels has been argued to adjust
145 to both bedrock erosion requirement and the mobilization of upstream sediment supply (e.g., Sklar and
146 Dietrich, 2006). However, the degree to which slope adjusts to each of these components remains unclear
147 (Johnson et al., 2009). While channel slope is commonly considered to be the consequence of bedrock
148 erosion and reshaping of the long profile (e.g., Royden and Perron, 2013), recent studies suggest that
149 equilibrium of bedrock channels could be attained by a modification of the slope of sediment overlying the
150 bedrock (Phillips and Jerolmack, 2016; Turowski, 2020, 2021). As in alluvial channels, rearrangement of
151 the bed to form a new sediment-bed slope can be achieved via selective deposition and entrainment
152 processes during floods (Mackin, 1948; Schumm and Parker, 1973; Schneider et al., 2015b; Turowski and
153 Hodge, 2017), which relates to sediment transport processes. Furthermore, adjusting sediment-bed slope
154 can be achieved within a timescale of a single flood, significantly faster than the timescale associated with
155 bedrock erosion and the formation of a new bedrock slope (Turowski, 2020).

156 In abrasion-dominated channels, erosion of the bedrock bed and banks are thought to occur during flood
157 events and are driven by impacts of sediment grains, which travel as bedload (e.g., Sklar and Dietrich, 2004;
158 Cook et al., 2013; Auel et al., 2017). Channel widening occurs by lateral erosion, which is thought to be a
159 consequence of sediment particles deflected to the sides following encounters with bed roughness elements
160 (e.g., Li et al., 2020). A field study from a bedrock channel gorge in Switzerland showed that wall erosion
161 increases in proximity to roughness elements (Beer et al., 2017). Although recent studies proposed a
162 positive relationship between channel roughness and lateral erosion (Fuller et al., 2016; Turowski, 2018;
163 Li et al., 2020; He et al., 2021) the precise nature of this relationship remains to be explored (Turowski,
164 2020).

165 In the light of the above review, adjustment of channel width and slope to perturbations caused by
166 immobile boulders can be expected to be controlled by bedrock erosion and sediment transport processes.
167 Changing channel slope could occur by eroding the bedrock bed and altering sediment cover and depth by
168 sediment deposition and entrainment. In contrast, existing models and observations indicate that widening
169 the channel is only possible by lateral erosion. Due to the estimated long timescales of width adjustment

170 (see below)(Turowski, 2020), a link between steady-state width and boulder concentration can be
171 established if we consider at least one of the following conditions. First, the timescale of bedrock channel
172 width adjustment to boulder input is shorter than the residence time of boulders within a river. Theoretically,
173 the widening of bedrock channels such as the Liwu River is expected to extend to periods of up to thousands
174 of years. Second, boulder supply and boulder degradation balance each other to keep the concentration of
175 boulders steady over the required time scale for width adjustment. These assumptions will be reviewed in
176 the discussion.

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182 **3. Boulders and Channel Morphology in the Liwu River: Methods and Empirical** 183 **Data**

184 The Liwu River, Taiwan, exhibits numerous fluvial bedrock reaches hosting huge boulders. This section
185 describes the methods applied for data collection in the Liwu River (Section 2.1) and empirical relations of
186 boulder concentration and channel slope and width based on these data (Section 2.2).

187 **3.1. Data Collection**

188 We documented 20 fluvial reaches along the Liwu River. Field data were collected in field campaigns
189 during the low flow seasons of 2018 and 2019. We selected different fluvial reaches with variable drainage
190 areas and local relief, representing various portions of the drainage basin. Our primary focus was on reaches
191 with a substantial number of boulders, but we also collected data from reaches with lower boulder
192 concentrations. We avoided fluvial reaches with incoming tributaries to ensure a minimal difference in
193 drainage area within a given reach. To avoid lithology differences, we used a geological map of Taiwan to
194 verify that the lithology does not change within the selected reaches. We avoided reaches exhibiting a large
195 spatial variability in channel width. In each channel reach, a drone was used to document the channel at 80
196 - 120 m above the channel, constrained by the complexity of the topography and the pilot's location. The
197 channel bed and banks were photographed primarily at vertical and various other angles, with ~80%
198 overlapping area. Due to the steep topography of many bedrock canyon sections, most of the reaches were
199 inaccessible by foot, thus prohibiting emplacement of Ground Control Points (GCPs). We generated point
200 clouds from the photos by using the AGISOFT METASHAPE commercial software. We created
201 orthophotos and DEMs at 5 - 25 cm/pixel horizontal spatial resolutions, depending on the site and data
202 quality. To account for the elevation uncertainty associated with the output models, we assume an elevation
203 error of ± 0.5 m for the DEM.

204 The reach area A_{tot} was manually delineated using a digitization process in ArcGIS. First, the upstream
205 and downstream channel reach boundaries were chosen and delineated with straight lines, bounding what
206 we observed as a continuous distribution of boulders (Fig. 2). Second, the channel bank boundaries were
207 identified and tracked by following distinctive bedrock-vegetation contacts. To evaluate the boulder-
208 concentration in the channel reach, we manually digitized the map-view area of all of the visible boulders
209 with an average diameter ≥ 2 m (Fig. 2B). A boulder was commonly recognized by observing that it
210 protrudes from either water or a gravel bar. Boulder-concentration was calculated using the relation $\Gamma =$
211 A_b/A_{tot} , where A_b is the sum of the areas of all of the boulders and can range between zero and one. To
212 extract boulder diameters from the delineated map-view polygons, we assumed that boulders are circles.
213 Reach-averaged channel width W_b was calculated using two methods: (1) by dividing the reach area by the
214 thalweg length L , the assumed streamwise distance that follows the curvature of the map-view channel

215 banks, and we consider a 5 m uncertainty on the measurement of L . (2) By manually measuring ten bank-
216 to-bank lengths, perpendicular to channel banks, along the reach and using the average as a representative.
217 We calculated the Root Mean Square Error (RMSE) value between the two methods to be 3.4 m (5% of the
218 average reach width measurements in all reaches). The standard deviation (STD) of each ten measurements
219 was used as an error on channel width measurements. To calculate reach-scale channel slope S_b in a boulder-
220 bed channel, the cross-sections that define the upstream and downstream boundaries of the reach area
221 (Fig. 2) were extracted from the DEM. The minimum elevation point of each cross-section was subtracted
222 and divided by L . Because a substantial fraction of the bedrock bed is occupied with fine sediments, the
223 slope represents a sediment-bed slope, which might differ from the bedrock-bed slope.

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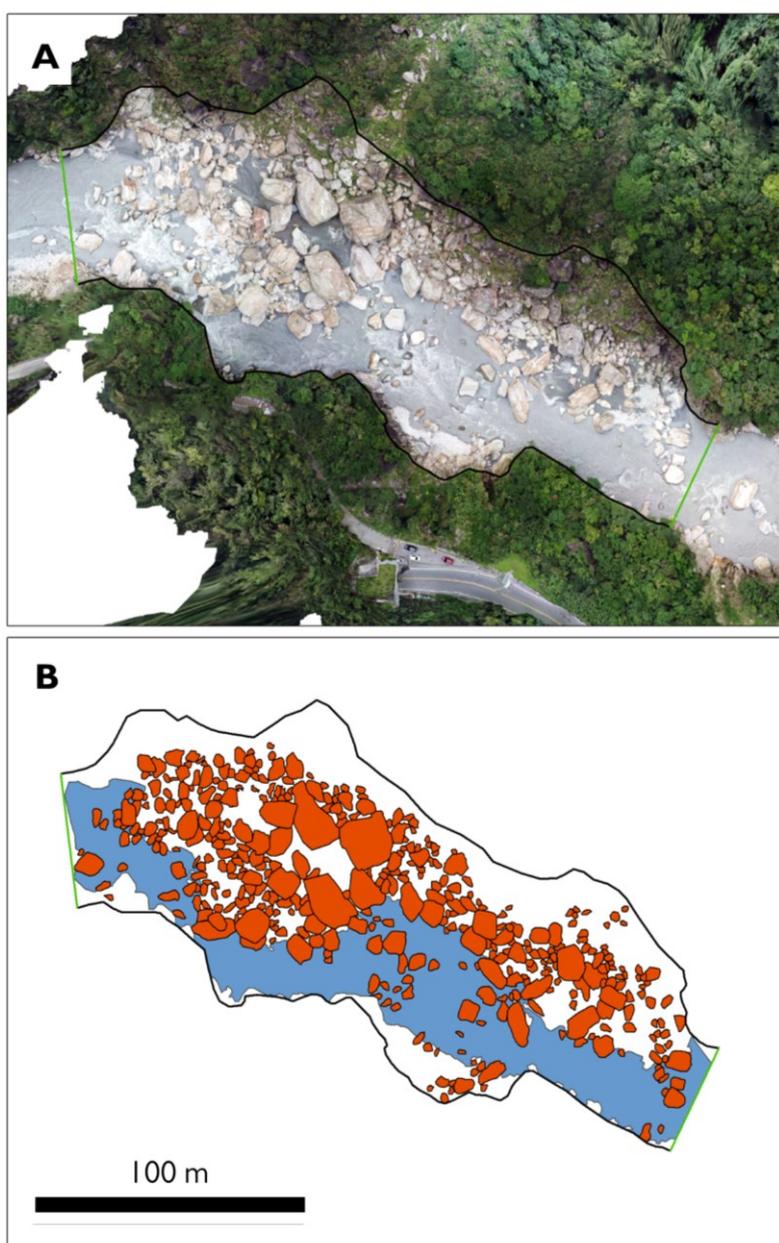


Figure 2: An example of boulder digitization. (A) A 3D model-derived orthophoto. The channel reach boundaries are marked (outer black and green lines). (B) The observed boulders are manually digitized (red polygons). Boulder concentration was calculated using the sum of all boulder area divided by the reach area. For the calculations, we accounted only for boulders with a diameter > 2 m. Flow direction is from left to right. Green lines in the upstream and downstream reach margins are the locations where cross-sections were used to estimate the reach-scale channel slope. For illustration, the water flow distribution is shown in blue.

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232 Theory and global observations show that to first order and in the absence of other perturbations,
233 channel width increases (e.g., Montgomery and Gran, 2001; Whitbread et al., 2015) and slope decreases
234 (e.g., Wobus et al., 2006) with drainage area. Consequently, to isolate the effects of boulders, the impact of
235 the drainage area needs to be removed. We use a dimensionless width ratio W_b/W , defined as the average
236 width ratio of paired reaches located immediately upstream or downstream from one another, presumably
237 without tributaries joining between them. W_b refers to the measured width of a boulder-bed channel, and W
238 refers to the width of a boulder-free channel. Similarly, we define a slope ratio S_b/S . Each selected pair of
239 reaches shares a similar drainage area and lithology. Calculations of boulder-free width W were performed
240 using two approaches. First, the average of ten measurements exploiting Google-Earth imagery, and
241 second, utilizing a basin-wide scaling relationship between width and drainage area for boulder-free
242 channels (Fig. S2). The first approach can test local width anomalies compared to the standard width
243 derived using the second approach. Data points that show significant difference between the two methods
244 are suspected of experiencing a local effect on width. Channel reaches with a large discrepancy between
245 the two measurements are marked differently in plots. The boulder-free slope S was determined by a power-
246 law regression between channel slope versus drainage area (Fig. S3) based on data of channels with minor
247 boulder presence.

248

249 3.2. Empirical Relations

250 The collected data include channel reaches with widths ranging between 30 and 120 m, slopes ranging from
251 0.01 to over 0.08, and boulder concentrations that range between ~ 0 and 0.34 (Table 1; Fig. 3). We observe
252 that both channel width (Fig. 3A; $R^2 = 0.29$) and slope (Fig. 3B; $R^2 = 0.51$) tend to increase with boulder
253 concentration Γ . The two approaches for evaluating boulder-free width W are compared (Fig. S2) and yield
254 relatively similar width ratios; among 20 data points, only two lie outside a 50% error. A comparison
255 between the methods yields a Root Mean Square Error (RMSE) value of 0.46, or 0.22 if the two outliers
256 are excluded. The width ratio W_b/W (Fig. 3D; $R^2 = 0.42$) and slope ratio, S_b/S ($R^2 = 0.71$) increase with
257 boulder concentration. In both cases, normalization by using the paired boulder-free reach improves the
258 relationship with Γ , as indicated by an increase of the R^2 (Fig. 3). Although the width ratio exhibits scatter
259 for a given Γ , W_b/W is always larger than one for $\Gamma > 0.05$. Over a range of 35% variability in boulder-
260 concentration, the slope ratio increases from about unity to > 4 .

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266 **Table 1:** Liwu River data

	^a Channel reach name	Drainage area, A [km ²]	^b Width factor (using BSR) W_b/W	^c Width factor (using GE) W_b/W	^d Slope factor S_b/S	Boulder-concentration, Γ	Mean boulder size D_{mean} [m]	Maximal boulder size D_{max} [m]
1	Baiyang downstream	59	1.21	1.27	0.33	0.05	2.9	6.2
2	Baiyang upstream	59	0.89	2.22	0.78	0.10	4.0	7.5
3	Bouluwan downstream	507	1.07	1.00	1.28	0.04	3.3	12.2
4	Bouluwan upstream	507	1.37	1.44	3.01	0.34	4.4	19.5
5	Dasha park	186	1.03	1.30	1.61	0.17	4.0	15.4
6	Dasha red-bridge downstream	183	1.37	2.38	0.96	0.07	2.0	9.1
7	Dasha red-bridge upstream	183	1.23	1.52	1.63	0.09	2.6	7.9
8	Dasha tunnel downstream	179	1.57	1.58	2.72	0.29	4.1	15.2
9	Dasha tunnel upstream	179	0.99	NA	1.06	0.03	3.4	5.5
10	East baiyang (near the parking)	188	0.89	NA	1.27	0.05	1.7	10.4
11	Heliu camp Downstream	431	0.87	NA	1.02	0.02	3.4	7.1
12	Heliu camp upstream	431	1.33	1.53	1.96	0.24	2.6	17.2
13	Lushui	450	1.54	1.48	1.53	0.22	4.4	23.4
14	Lushui Downstream	431	1.94	1.94	1.85	0.15	3.3	12.4
15	Lushui Upstream	431	1.05	NA	0.55	0.01	2.2	3.6
16	Ning an Upstream	523	2.21	1.65	1.30	0.16	3.5	23.2
17	Sinuous reach	523	1.83	1.48	3.59	0.29	3.0	19.1
18	Sinuous upstream	514	1.50	1.29	0.94	0.10	2.1	12.2
19	Tianxiang construction	431	1.26	1.18	2.59	0.20	3.3	17.3
20	Tianxiang hotel	258	1.13	1.12	1.85	0.16	2.5	19.2

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^aBoulder-bed reach locations are indicated in Fig. (S1).

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^bBSR stands for Basin Scale Relationship, and denotes the width calculated using the relation $W = 0.48A^{0.24}$ for channels without boulders (Fig. S3).

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^cGE stands for Google Earth, and denotes the average of 10 width measurements.

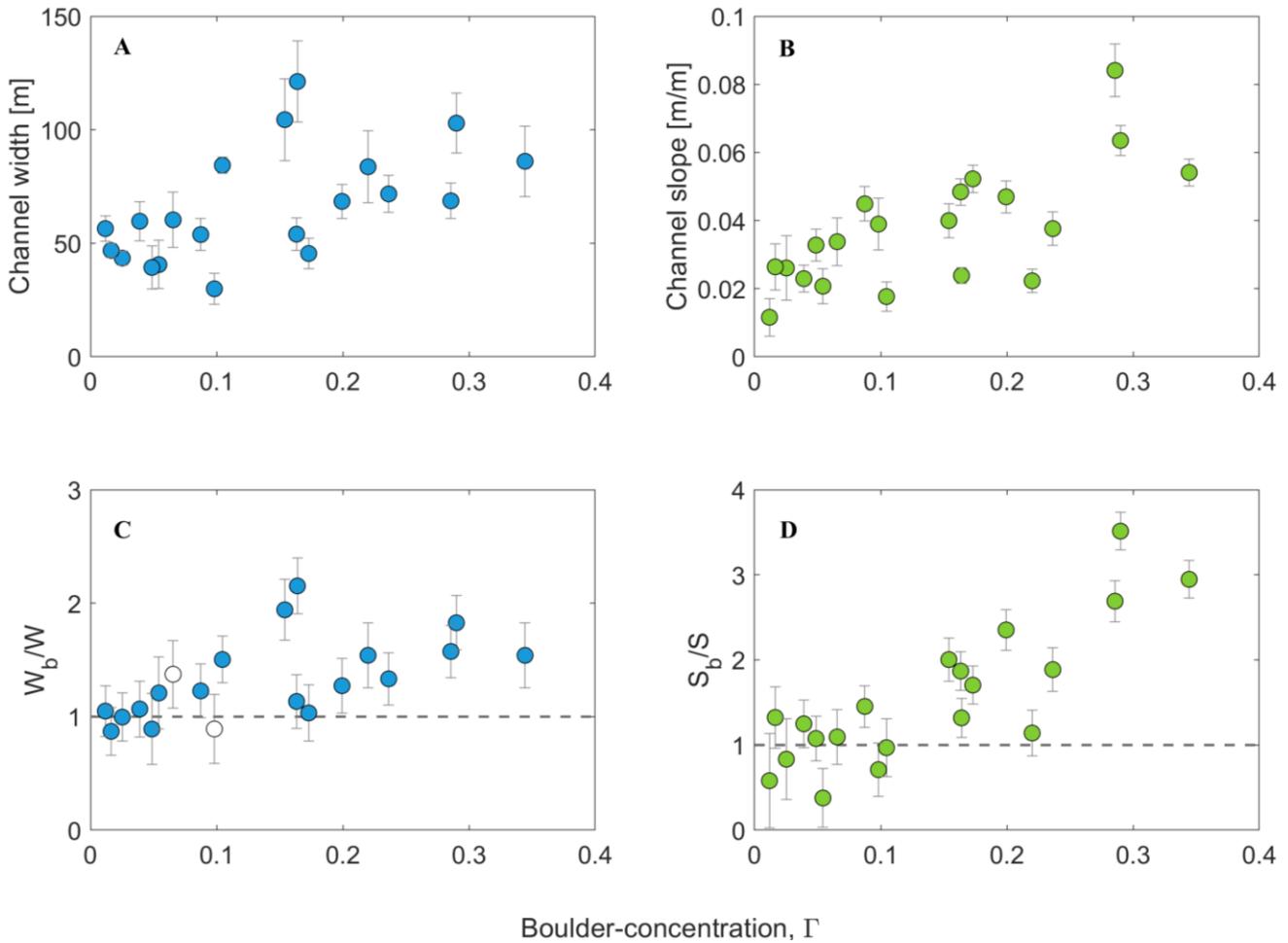
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^dChannel slope was calculated using the relation $S = 505.4A^{-0.51}$ for channels without boulders (Fig. S3).

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For information about the errors associated with calculations of W_b/W and S_b/S see supporting information.

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Figure 3: Channel morphology versus boulder concentration in the Liwu River. **(A)** Channel width increases with boulder-concentration ($R^2 = 0.29$). Error bars represent one STD from the mean of ten measurements. **(B)** Channel slope increases with boulder-concentration ($R^2 = 0.51$). Error bars represent uncertainties in elevation (0.5 m) and in thalweg length (5 m). **(C)** The width ratio W_b/W increases with Γ ($R^2 = 0.42$). White circles represent data points in which width ratio measured using two distinct methods is different by over 50% (Fig. S2; section 2.2.). **(D)** The slope ratio S_b/S increases with Γ ($R^2 = 0.71$). The fits improve in both cases where slope and width are normalized by the value of the paired boulder-free reach (compare C and D to A and B). For information about the errors associated with calculations of W_b/W and S_b/S see supporting information.

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275 4. Theoretical framework

276 In this section, we develop a theoretical framework that yields steady-state analytic solutions that predict
277 the width ratio W_b/W and the slope ratio S_b/S as functions of boulder-concentration, Γ . The geometrical
278 adjustment of a boulder-bed bedrock channel is associated with two aspects of its mass balance. First,
279 Bedrock Rivers evolve by matching their erosion rates to the applied uplift rates. Second, like alluvial rivers
280 (e.g., Mackin, 1948), it has been argued that bedrock rivers evolve to achieve a graded state (Turowski,
281 2020), related to the mass balance of river sediments. Aggradation of the bed occurs if the flow is unable
282 to carry the supplied sediments from upstream. Conversely, degradation of the bed arises when the flow's
283 ability to mobilize sediments is larger than the sediment supply. When the channel geometry reflects a
284 condition where the power of the channel to mobilize sediments exactly equals upstream sediment supply,
285 the channel is considered graded. When boulders disturb a bedrock channel, the channel responds by
286 altering its geometry until an erosion-uplift balance and grade are met again. As is shown below, the
287 solutions developed under the erosional balance assumption predict W_b/W as a function of Γ , while
288 predictions derived from the grade assumption yield solutions involve both W_b/W and S_b/S .

289

290 4.1. Influence of Boulders on Bedrock Erosion

291 The erosion rate in abrasion-dominated bedrock rivers is thought to be physically driven by the impacts
292 of moving sediment grains during floods (e.g., Sklar and Dietrich, 1998, 2004; Turowski et al., 2007).
293 When sediment flux increases, more sediments are available to impact the channel bed, causing erosion
294 and contributing to the so-called 'tools effect' (e.g., Cook et al., 2013). In contrast, when sediment flux
295 further increases, the bed becomes shielded to impacts by sediments, consequently inhibiting erosion by
296 the 'cover effect' (e.g., Johnson et al., 2010; Turowski and Hodge, 2017). Bedrock erosion is thus modulated
297 by the tools effect, approximated by sediment flux per unit width Q_s/W [$\text{kg}^1\text{s}^{-1}\text{m}^{-1}$], the cover effect, and
298 the rock erodibility k [m^2kg^{-1}], the latter determining the susceptibility of the rock to erosion and the eroded
299 volume per sediment impact for given forcing factors. Sediment flux-dependent vertical erosion rate E_v ,
300 [ms^{-1}] is given by the product of these three terms (Sklar and Dietrich, 2004; Auel et al., 2017; Turowski,
301 2018)

$$302 \quad E_v = k \frac{Q_s}{W} (1 - C_f) \quad (1)$$

303 To account for the effect of immobile boulders in Eq. (1), C_f is defined as the sediment cover due to mobile
304 fine grains only and does not include the cover by large immobile boulders. The fine cover C_f can be
305 calculated from a cross-sectional perspective, by dividing the width which is not covered by sediments
306 ('uncovered width'), with the total width W . To predict steady-state channel width using Eq. (1) we need an

307 assumption about the cover C_f at steady-state. Turowski (2018) suggested that steady-state width can be
 308 related to a length scale d [m], which indicates the distance in which a sediment particle is deflected to the
 309 side after impacting a roughness element, thereby causing bedrock wall erosion. Bedload deflected towards
 310 the sidewalls can cause wall erosion if d is larger than the cover-free channel width. In contrast, no wall
 311 erosion occurs when d is smaller than the cover-free width. At some point, the channel width adjusts such
 312 that particles almost arrive at the channel wall but do not cause erosion (Turowski, 2018, 2020). In this
 313 specific steady-state, d is equal to the uncovered width

$$314 \quad C_f = \frac{W-d}{W} = 1 - \frac{d}{W} \quad (2)$$

315 Substituting (2) into (1) and solving for the width, the model predicts steady-state width to be:

$$316 \quad W = \sqrt{\frac{kdQ_s}{E_v}} \quad (3)$$

317 The sideward deflection length d is expected to vary in space and time and can expected to depend on
 318 channel hydraulics, roughness, and sediment supply (Fuller et al., 2016a; Beer et al., 2017; Turowski, 2018,
 319 2020b; Li et al., 2020; He et al., 2021).

320 We explore five potential effects of the influence of immobile boulders on steady-state channel width.
 321 For each effect, we develop an analytical expression that predicts a boulder-bed channel width $W_{b,m}$ and
 322 then use Eq. (3) to normalize it by the steady-state width of a boulder-free equivalent reach. This process
 323 leads to terms of the form $W_{b,m}/W$, where the subscript b stands for a boulder-reach, and subscript m denotes
 324 the specific effect. When normalizing, we assume that vertical erosion in the boulder-bed channel $E_{v,b}$
 325 equals the erosion E_v in the nearby boulder-free channel. Likewise, the erodibility (Eqs. 1 and 3) is assumed
 326 similar in both reaches. Consequently, both the erosion and the erodibility terms are canceled.

327

328 4.1.1 The Cover Effect

329 Immobile boulders hinder fluvial bedrock erosion by shielding the bed (Shobe et al., 2016, 2018). However,
 330 most models that solve Eq. (1) do not consider the presence of immobile boulders with residence times
 331 larger than those of fine grains. Here, we assume a cross-section configuration with an immobile boulder
 332 in the center and a patch of fine cover that hugs one of the banks (Fig. 4). In contrast to previous works
 333 (e.g., Sklar and Dietrich, 2004), we define the riverbed fraction covered by mobile sediments as $C_f = A_f /$
 334 $(A_{tot} - A_b)$, where A_{tot} is the reach area, and A_f and A_b are the areas covered by fine sediments, and boulders,
 335 respectively. The total cover C_{tot} of the mobile sediments and immobile boulders is then written as

336

337
$$C_{tot} = 1 - (1 - C_f)(1 - \Gamma) \quad (4)$$

338

339 Equation (4) can be combined with the equation of vertical erosion rate (1) by replacing $(1 - C_f)$ with $(1 -$
 340 $C_{tot})$, where both C_f and Γ ranges between zero and one. To illustrate this choice, when Γ is 0.5, half of the
 341 channel reach area is covered by boulders, and half is free to accommodate non-stationary, finer sediments.
 342 Then, C_f may be adjusted according to the remaining proportion, e.g., $C_f = 1$ means that the fine sediments
 343 cover the remaining bed area, half of the total reach area. In this case, the fine steady-state cover can be
 344 described using the definition for the fine sediment cover C_f

345
$$C_f = \frac{W_{cf}}{W_b - W_{cb}} = \frac{W_b - (d_b + W_{cb})}{W_b - W_{cb}} = 1 - \frac{d_b}{W_b(1 - \Gamma)} \quad (5)$$

346

347 Here, d_b is the deflection length scale in the boulder-bed channel. Assigning Eqs. (5) and (4) into (1),
 348 solving for steady-state boulder width W_b and dividing by Eq. (3) leads to:

349
$$\frac{W_{bcover}}{W} = \sqrt{\frac{d_b}{d}} \quad (6)$$

350 Equation (6) predicts that the width ratio due to the cover mechanism by boulders is independent of boulder
 351 concentration and only depends on the square root of the ratio of channel deflection length. This
 352 independence on Γ derives from two opposing effects. First, vertical erosion decreases due to boulder
 353 covering the bed according to $(1 - \Gamma)$ (substitute Eq. (4) with (1)). Second, in the bed areas which are not
 354 covered, vertical erosion increases according to $1/(1 - \Gamma)$ (Eq. 5).

355

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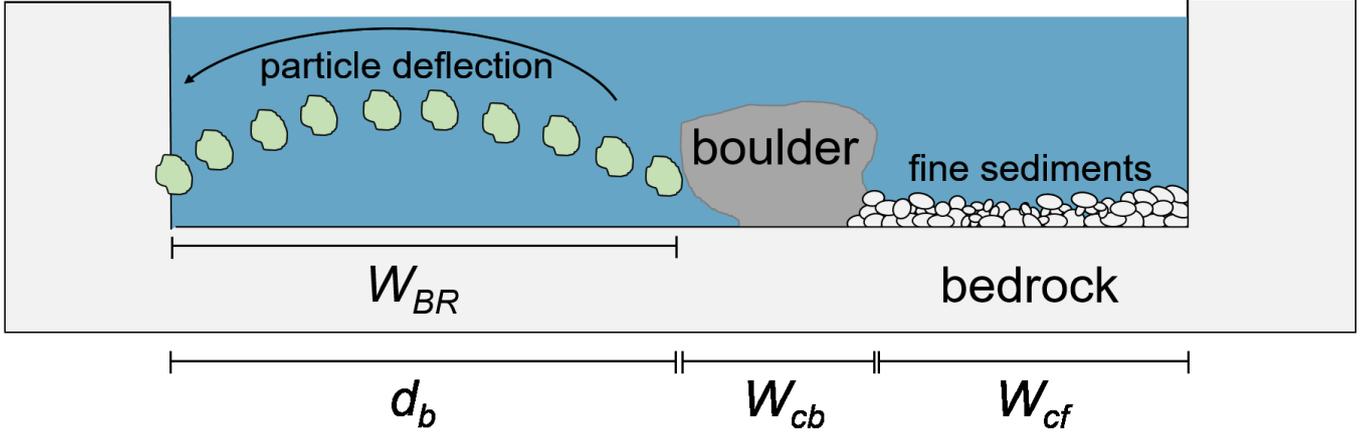


Figure 4: Schematic channel cross-section setting. The total boulder-bed channel width W_b is the sum of the different width portions, including boulders (W_{cb}), exposed bedrock (W_{BR}), fine cover (W_{cf}). Here we assume that the particle deflection d_b equals the exposed bedrock.

4.1.2 The Tools Effect

In a boulder-bed channel reach, immobile boulders occupy a fraction of the total bed area, thus reducing the bed area exposed to erosion. We assume that impacting sediments acting as erosion tools can concentrate on such reduced exposed bedrock patches. Consequently, for a given cross-sectional geometry, the existence of immobile boulders increases bedload flux per unit exposed (or reduced) width. The presence of the boulders causes mobile sediments to impact on a reduced width, defined here as the effective width W_{eff} . This assumption is somewhat similar to the approach of Yager et al. (2007) and Papanicolaou et al. (2012), who assumed a reduced area for sediment transport. The resultant average effective width is the reach area free of boulders ($A_{tot} - A_b$) divided by the total reach length L

$$W_{eff} = W(1 - \Gamma)^\alpha \quad (7)$$

Equation (7) is derived using the relations $A_{tot} = WL$ and $A_b = A_{tot}\Gamma$. The power α controls the magnitude of this effect. The condition $\alpha = 1$ applies that sediment only moves over the part of the bed without boulders, and $\alpha = 0$ applies that sediments are also transported over the top of the boulders. Eq. (1) becomes $E_V = k \frac{Q_s}{W_{eff}} (1 - C_f)$. Inserting Eq. (7) into the modified (1) and solving for steady-state boulder width and dividing by (3):

$$\frac{W_{btools}}{W} = \sqrt{\frac{d_b}{d}} (1 - \Gamma)^{\frac{-(\alpha+1)}{2}} \quad (8)$$

380 According to Eq. (8), for $d_b/d = 1$, boulder-bed width increases with boulder-concentration due to the tools
 381 effect. The combination of both tools and cover effects into a single model yields

$$382 \quad \frac{W_{bTAC}}{W} = \sqrt{\frac{d_b}{d}} (1 - \Gamma)^{-\frac{\alpha}{2}} \quad (9)$$

383 In this case, the solution collapses to Eq. (6), for $\alpha = 0$, or indicates an increase of width with boulder-
 384 concentration for $\alpha > 0$.

385

386 4.1.3 The Multi-Channel Effect

387 Immobile boulders are obstacles in the channel, which are hypothesized to form small independent
 388 channels ('in-channels') between boulders as well as between boulders and the channel banks (Fig. 5). A
 389 channel reach can have two or more in-channels; the minimum set of in-channels occurs when one large
 390 boulder occupies the center of a cross-section. Consider a fluvial reach with a width W_b and a length L .
 391 There, boulders form n_b island-like columns parallel to the flow direction (Fig. 5). The total reach number
 392 of-in channels n_{ic} equals $n_b + 1$. Assuming cubic-shaped boulders (Fig. 5) with a diameter D_B , the number
 393 of in-channels is given by

$$394 \quad n_{ic} = 1 + \frac{\Gamma W_b}{c D_B} \quad (10)$$

395 Here, $c D_B$ [m] is the length of a typical pile of clustered boulders (Fig. 5), and $c (> 1)$ is a dimensionless
 396 parameter, assumed to equal the number of boulders constituting the boulder-island in the cross-section
 397 direction. Bedload is considered to be evenly distributed between the in-channels, such that in each of them,
 398 the average bedload flux $\overline{Q_{s,ic}}$ is given by

$$399 \quad \overline{Q_{s,ic}} = \frac{Q_s}{n_{ic}} = \frac{Q_s}{1 + \Gamma \frac{W_b}{c D_B}} \quad (11)$$

400 We assume that steady-state cover adjusts within each in-channel independently so that deflected sediments
 401 arrive precisely at the boulder or channel bank but do not cause lateral erosion. In this case, each in-channel
 402 width W_{ic} can be approximated using a form of Eq. (3)

$$403 \quad W_{ic} = \sqrt{\frac{k d \overline{Q_{s,ic}}}{E_v}} = \sqrt{\frac{k d Q_s}{E_v}} \left(1 + \Gamma \frac{W_b}{c D_B}\right)^{-0.5} \quad (12)$$

404 The total reach width W_{bMCE} is the sum of all in-channel widths $W_{ic} \overline{n_{ic}}$ and the width occupied by boulders
 405 $(\overline{n_b} - 1) c D_B$ (i.e., the number of boulders times their size)

$$406 \quad W_{bMCE} = W_{ic} n_{ic} + (n_{ic} - 1) c D_B \quad (13)$$

407 Assigning Eqs. (10)-(12) into (13), and solving for W_{bMCE} , we reach a quadratic equation with only one
 408 physically meaningful solution:

409
$$\frac{W_{bMCE}}{W} = \frac{1}{2(1-\Gamma)^2} \left(\frac{W\Gamma}{cD_B} + \sqrt{\left(\frac{W\Gamma}{cD_B}\right)^2 + 4(1-\Gamma)^2} \right) \quad (14)$$

410
 411 where D_B is the boulder diameter. Equation (14) predicts that a boulder-channel width increases with
 412 boulder-concentration for a given D_B . Equation (14) is implicit for W , and to solve it, information on the
 413 boulder-free width, W , is needed.

414

415

416 **Natural settings**

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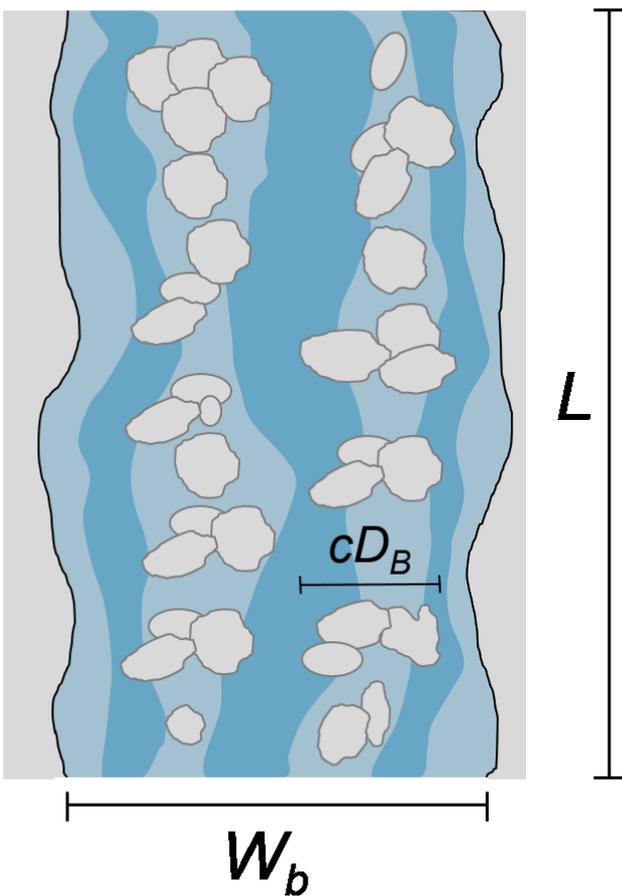
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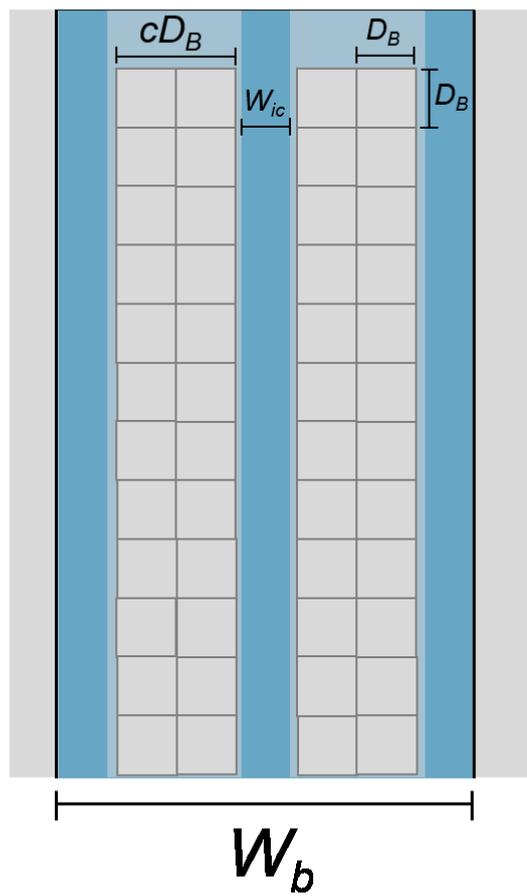
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Model



428

429

430 **Figure 5:** The model geometry used in the multi-channel effect. The model describes an L long W_b wide fluvial
 431 reach hosting square shaped boulder piles with a diameter D_B . The parameter c denotes the number of boulders
 432 in a pile (two in this example) and each formed in-channel is assumed to be W_{ic} wide. The right hand side
 433 delineates a repeat geometry pattern parallel to the flow direction.

434 4.2. Influence on Sediment Transport

435 The concept of grade (Gilbert, 1877; Davis, 1902; Mackin, 1948) stipulates that a channel removed
 436 from equilibrium adjusts its system variables to restore the ability to transport the same sediment supplied
 437 from upstream. A central paradigm is that channel slope adjusts to achieve grade (e.g., Mackin, 1948; Lane,
 438 1955; Bolla Pittaluga et al., 2014; Blom et al., 2016, 2017). Various models have been developed for
 439 equilibrated channel profiles but assumed fixed channel width (e.g., Parker, 1978, 1979; Bolla Pittaluga et
 440 al., 2014; Blom et al., 2016). The graded state depends on the sediment mass balance of a river. An
 441 evolutionary mass balance representation of the sediment-bed elevation h_s is described by the Exner equation
 442 (e.g., Paola and Voller, 2005; Ancey, 2010)

$$443 \quad \frac{\partial h_s}{\partial t} = -\frac{1}{\rho_s(1-p)} \frac{\partial q_s}{\partial x}, \quad (15)$$

444 which states that the rate of change of the sediment-bed elevation h_s with respect to time t is proportional
 445 to the divergence of sediment mass flux per unit width q_s . Here, the coordinate x denotes the streamwise
 446 direction, p is sediment porosity, and ρ_s is the sediment density. A situation where a channel is in grade
 447 implies that the derivative on the left-hand side of (15) equals zero, implying that $\frac{\partial q_s}{\partial x} = 0$, and sediment flux
 448 is constant along the channel (e.g., Zhou et al., 2017).

449 Based on the above concept, we assume that boulder-bed channels adjust their geometry (i.e., width
 450 and slope) to accommodate a change in sediment transport due to boulder emplacement. A new equilibrium
 451 is reached when the sediment flux within the boulder-bed channel $Q_{s,b}$ matches the sediment flux in the
 452 nearby boulder-free channel Q_s . Thus, for equilibrated boulder-bed channels, we can write

$$453 \quad Q_{s,b} = Q_s \quad (16)$$

454 To derive the steady-state form of the adjusted boulder-bed channels, we first define a general bedload
 455 transport equation (e.g., Meyer-Peter and Müller, 1948; Fernandez Luque and Van Beek, 1976)

$$456 \quad \frac{Q_s}{W} = \gamma \left(g \left(\frac{\rho_s}{\rho} - 1 \right) D^3 \right)^{0.5} (\tau^* - \tau_c^*)^{3/2} \quad (17)$$

457 Here, $\tau^* = \frac{\rho H S}{(\rho_s - \rho) D}$ is the Shields number, H is flow depth [m], τ_c^* is the critical Shields stress for bedload
 458 incipient motion, D [m] is bedload grain size, g [9.81 ms⁻²] is the acceleration due to gravity, and γ is a non-
 459 dimensional constant larger than one (Fernandez Luque and Van Beek, 1976; Wong and Parker, 2006).
 460 Equation (17) can be replaced by a discharge-based equation for sediment transport (Rickenmann, 2001),
 461 which takes the form of (e.g., Turowski, 2021)

$$462 \quad \frac{Q_s}{W^q} = K_{BL} Q^m S^n \quad (18)$$

463 Here, Q is water discharge, and K_{BL} is a constant describing transport efficiency. The exponent m typically
464 takes values between 1 and 4 (Barry et al., 2004), while n ranges between 1.5 to 2 (Rickenmann, 2001).
465 The exponent q sets the dependence of bedload transport on channel width and is often assumed to be equal
466 to zero (e.g., Rickenmann, 2001). However, given the unsteady nature of bedload transport and along-
467 stream variations in channel width (Cook et al., 2020), the parameter q may differ from zero. Analytically
468 derived end-member approximations have been discussed by Turowski (2021), which give values for q of
469 zero, 0.1, or 2.5.

470 The influence of boulders on sediment transport can be considered via the boulder effects on the various
471 parameters in equations (17) and (18) (Shobe et al., 2021). A reduction in the effective shear-stress
472 ($\tau^* - \tau_c^*$) is associated with two different hypothesized effects (Schneider et al., 2015a): (i) a reduction in
473 τ^* due to fluid friction forces (e.g., Canovaro et al., 2007; Yager et al., 2007; Nitsche et al., 2011) and (ii)
474 an increase in the threshold of motion τ_c^* with channel slope (Lamb et al., 2008; Prancevic and Lamb, 2015),
475 which is thought to increase with boulder-concentration (Nitsche et al., 2011; Thaler and Covington, 2016;
476 Shobe et al., 2020). Similarly, there might be a reduction in the bedload transport efficiency for a given
477 shear-stress (Rickenmann, 2001; Nitsche et al., 2011) due to particles either taking longer pathways or
478 being transported slower due to boulder-influenced hydrodynamic effects (Papanicolaou et al., 2018).
479 Based on these effects, we establish two theoretical models that predict the relation between the width and
480 slope ratios. We begin in section 4.2.1 with analytical solutions assuming a reduction in the coefficient of
481 transport efficiency and continue in section 4.2.2 by considering a reduction in the Shields-number due to
482 fluid friction forces on boulders. Additional potential effects of an increase in the threshold of motion τ_c^*
483 due to boulders, and a reduction in the energy slope for bedload transport (e.g., Chiari et al., 2010) are
484 acknowledged, but are not treated in this paper.

485

486 **4.2.1 Reduction in Bedload Transport Efficiency**

487 A boulder placed into a steady-state channel is expected to change the river's ability to carry bedload
488 sediments. A reduction in the transport efficiency is expected because, during a transport event, sediments
489 can (i) be deposited in the wake-zones of boulders due to flow reversals (e.g., Papanicolaou and Tsakiris,
490 2017; Papanicolaou et al., 2018), thus delaying their overall movement downstream, (ii) lose momentum
491 due to direct encounters with boulder-influenced zones, and (iii) take longer pathways relative to a similar
492 boulder-free channel (e.g., Seizilles et al., 2014). The new condition adjusts the channel geometry to a new
493 state where transport capacity equals the sediment supply. This can be achieved via changing slope, width,
494 or both (Eq. 18). Rickenmann (2001) showed for flume and field bedload transport data that transport
495 efficiency decreases with relative roughness (ratio of flow depth to grain size) by up to five orders of
496 magnitudes. Nitsche et al. (2011) studied flow and bedload transport characteristics in 13 Swiss streams.

497 They showed that fractional transport efficiency K'_{BL}/K_{BL} , where K'_{BL} is the reduced transport efficiency
 498 coefficient due to roughness, decreases with boulder-concentration. Using digitization of their bedload data
 499 (their Fig. 8e), we fitted the relation between K'_{BL}/K_{BL} and Γ with:

$$500 \quad \frac{K'_{BL}}{K_{BL}} = \frac{1}{1+(\theta-1)\Gamma^\nu} \quad (19)$$

501 Equation (19) is an empirical function with a factor θ and a power ν . Substituting Eq. (18) into (16) leads
 502 to:

$$503 \quad K'_{BL} Q^m W_{b_{STE}}^q S_{b_{STE}}^n = K_{BL} Q^m W^q S^n \quad (20)$$

504 And solving for the slope ratio using (19)

$$505 \quad \frac{S_{b_{STE}}}{S} = \left(\frac{W_{b_{STE}}}{W} \right)^{-q/n} (1 + (\theta - 1)\Gamma^\nu)^{1/n} \quad (21)$$

506 Here, $S_{b_{STE}}/S$ and $W_{b_{STE}}/W$ are dependent variables, whereas Γ is independent and q , n , θ , and ν are empirical
 507 parameters. Closing equation (21) requires that the width ratio is substituted with either one of the models
 508 derived in section 3.1 or supplied with field data.

509

510 4.2.2 The effect of Shear-Stress Partitioning

511 The total shear stress acting on a channel boundary is commonly used as a first-order parameter for
 512 prediction of bedload fluxes (e.g., eq. 18; Einstein, 1950; Fernandez Luque and Van Beek, 1976;
 513 Rickenmann, 2001). However, many bedload transport equations were derived based on flume experiments,
 514 where the geometry is simplified and roughness is considered to be steady. Natural bedrock channels often
 515 exhibit bedforms and large grains, which act as obstacles to the flow, altering water velocity gradients and
 516 associated shear stresses. Mainly, roughness elements bear a fraction of the total available shear-stress τ ,
 517 thus decreasing the available shear stress for entrainment of bedload τ_m . Einstein and Banks (1950)
 518 suggested that the total resistance to roughness elements equals the sum of the resistance of each of the
 519 individual components. This partitioning approach for transport predictions was further developed for
 520 immobile boulders (Yager et al., 2007). We adopt this approach to predict channel width and slope in
 521 boulder-bed channels, acknowledging that boulders are roughness elements. Following Yager et al. (2007),
 522 we partition the channel bed into a fine-grained, mobile bedload fraction (denoted by the subscript m) with
 523 a characteristic grain size D and immobile boulders with a diameter of D_B . Shear-stresses are not additive,
 524 i.e., the total shear-stress τ does not equal the sum of all stresses. Instead, forces are additive; hence we can
 525 assume a fluid force balance between the driving forces F_{tot} and the resisting forces F_d and F_m

$$526 \quad \tau A_{tot} = \tau_d A_d + \tau_m A_m \quad (22)$$

527 Here, $F_m = \tau_m A_m$ is the resisting force due to the roughness of the channel bed without boulders, which
 528 encompasses both skin friction and drag (Dey, 2014), $F_d = \tau_d A_d$ is the resisting force due to drag on boulders,
 529 and A_{tot} , A_d and A_m are the channel areas upon which the forces are applied, respectively. The skin friction
 530 component due to boulders F_s is assumed to be negligible. To facilitate area calculations, we can divide Eq.
 531 (22) by the total reach area A_{tot} to obtain

$$532 \quad \tau = \tau_d \frac{A_d}{A_{tot}} + \tau_m \frac{A_m}{A_{tot}} \quad (23)$$

533 In a large flood, the entire bed is submerged, and the mobile area A_m upon which drag applies is proportional
 534 to the overhead projection area without boulders, i.e., $A_m/A_{tot} = (1-\Gamma)$. However, boulders extend into the
 535 flow; thus, drag forces act mostly on their upstream sides and $A_d = nD_B^2$, with n being the number of
 536 boulders in the reach. Using the definitions for boulder-concentration $\Gamma = nD_B^2/WL$ and for the reach area
 537 $A_{tot} = WL$, we introduce $A_d/A_{tot} = \Gamma$. Thus, (23) can be rewritten as:

$$538 \quad \tau = \tau_d \Gamma + \tau_m (1 - \Gamma) \quad (24)$$

539 Considering that boulders reduce the total shear stress, we aim to find an expression for the reduced shear
 540 stress, τ_m/τ , which we assume is responsible for fine sediment transport. First, the fractional boulder-drag
 541 stress τ_d/τ can be evaluated using a general empirical log-linear model based on experimental results from
 542 Canovaro et al. (2007):

$$543 \quad \frac{\tau_d}{\tau} = \beta \Gamma \left[1 - \ln \left(\frac{\Gamma}{\Gamma_{max}} \right) \right]; \quad 0 < \Gamma \leq e \Gamma_{max} \quad (25)$$

544 Here, Γ_{max} is the boulder-concentration for which τ_d/τ is maximal, β is a scaling factor, and e is the natural
 545 base logarithm constant. The maximal τ_d/τ value can be derived by applying $\Gamma = \Gamma_{max}$, which in that case
 546 $(\tau_d/\tau)_{max} = \beta \Gamma_{max}$. The random-boulder setting experiments of Canovaro et al. (2007) show that Γ_{max} is
 547 relatively limited and ranges from ~ 0.2 to 0.4 . The condition $\Gamma \leq e \Gamma_{max}$ verifies that τ_d/τ do not yield
 548 negative, unrealistic values. Substituting Eqs. (24) and (25) into (22) and solving for τ_m/τ

$$549 \quad \frac{\tau_m}{\tau} = \frac{1}{1-\Gamma} \left[1 - \beta \Gamma \left[1 - \ln \left(\frac{\Gamma}{\Gamma_{max}} \right) \right] \right] \quad (26)$$

550 If only the effect of shear stress partitioning is considered, then the combination of (16) and (17) implies

$$551 \quad W_{bSSP} \tau_m^*{}^{3/2} \sim W \tau^*{}^{3/2} \quad (27)$$

552 Rearranging (27) and solving for W_b/W using the definition for the Shield-stress $\tau^* = \frac{\tau}{gD(\rho_s - \rho)}$ and $\tau_m^* =$
 553 $\frac{\tau_m}{gD(\rho_s - \rho)}$ and Eq. (26)

$$554 \quad \frac{W_{bSSP}}{W} = \left(\frac{\tau_m}{\tau} \right)^{-3/2} = \left[\frac{1}{1-\Gamma} \left(1 - \beta \Gamma \left(1 - \ln \left(\frac{\Gamma}{\Gamma_{max}} \right) \right) \right) \right]^{-3/2} \quad (28)$$

555 The effect of shear-stress partitioning can alternatively be expressed in terms of the slope ratio (Appendix
556 A)

$$557 \quad \frac{S_{bSSP}}{S} = \left(\frac{1}{1-\Gamma} \left[1 - \beta\Gamma \left[1 - \ln \left(\frac{\Gamma}{\Gamma_{max}} \right) \right] \right] \right)^{\frac{\delta-0.5}{\delta+0.5}} \quad (29)$$

558 Where δ is an exponent relating water velocity to the hydraulic radius R_h and equals $\frac{1}{2}$ for a Darcy-
559 Weisbach relation or $\frac{2}{3}$ for a Manning-Strickler relation. For δ equals $\frac{1}{2}$, the right-hand side of (29) equals
560 one, and the boulder-bed channel slope S_b equals the boulder-free channel slope, whereas when δ equals
561 $\frac{2}{3}$, the slope ratio S_b/S depends on the expression on the right-hand side of (29) to the power of $1/7$. With
562 such a low exponent, the effect of shear-stress partitioning on the slope ratio is expected to be small and is
563 not likely to reproduce the data.

564
565 **Table 2:** Models performances of the width and slope ratios.

Assumption	Mechanism	Prediction	^a Parameters	^b RMSE
Erosional balance: bedrock erosion matches between boulder-bed and boulder-free channels	Cover	$\frac{W_{bcover}}{W} = \sqrt{\frac{d_b}{d}}$	$d_b = d$	0.48
	Tools	$\frac{W_{btools}}{W} = \sqrt{\frac{d_b}{d}} (1-\Gamma)^{-\frac{(\alpha+1)}{2}}$	$\alpha = 0$	0.40
			$\alpha = 1$	0.33
	Tools and Cover	$\frac{W_{bTAC}}{W} = \sqrt{\frac{d_b}{d}} (1-\Gamma)^{-\frac{\alpha}{2}}$	$\alpha = 0$	0.48
			$\alpha = 1$	0.40
	Multi-channel Effect	$\frac{W_{bMCE}}{W} = \frac{1}{2(1-\Gamma)^2} \left(\frac{W\Gamma}{c} + \sqrt{\left(\frac{W\Gamma}{cD_B} \right)^2 + 4(1-\Gamma)^2} \right)$	$c = D_{max}/D_{mean}$	0.51
Grade: sediment flux between boulder-bed and boulder-free channels equals	Reduction in Sediment Transport Efficiency	$\frac{S_{bSTE}}{S} = \left(\frac{W_b}{W} \right)^{-q/n} (1 + (\theta - 1)\Gamma^v)^{1/n}$	$q = 0$	0.43
			$q = 0.1$	0.44
			$q = 1$	0.76
	Shear-stress Partitioning	$\frac{W_{bSSP}}{W} = \left[\frac{1}{1-\Gamma} \left(1 - \beta\Gamma \left[1 - \ln \left(\frac{\Gamma}{\Gamma_{max}} \right) \right] \right) \right]^{-3/2}$	$\beta = 1.38$ $\Gamma_{max} = 0.30$	0.32
		$\frac{S_{bSSP}}{S} = \left(\frac{1}{1-\Gamma} \left[1 - \beta\Gamma \left[1 - \ln \left(\frac{\Gamma}{\Gamma_{max}} \right) \right] \right] \right)^{\frac{\delta-0.5}{\delta+0.5}}$	$\beta = 1.38$ $\Gamma_{max} = 0.30$	0.50

566 ^aThe parameter values used to examine the models against the Liwu data.
567 ^bRoot Mean Square Error calculated between the Liwu data and the examined model.
568

569
570

571 **5. Model Evaluation using the Liwu River Data**

572 The mechanisms introduced in Section 4 yield five equations for the width and two for the slope ratio (Table
573 2). These can be tested against the Liwu River data (Fig. 3). Each model contains various parameters, some
574 of which could not be independently constrained. Due to the scatter in the width ratio versus boulder-
575 concentration (Fig. 3C), we do not expect a single set of parameters to predict the entire width ratio dataset.
576 Moreover, plotting a single model with specific parameter values requires calibration against field data,
577 which will bias the model towards good performance. Instead, we analyze slope and width ratio sensitivity
578 to parameter changes within the different models by plotting model results for different parameter scenarios
579 while holding other parameters constant.

580

581 **5.1 The Tools, Cover, 'Tools and Cover,' and Multi-Channel Effect Models**

582 The cover (Eq. 6), the tools (Eq. 8), and the combined 'tools and cover' (Eq. 9) effects can be solved
583 explicitly and can therefore be directly compared to the field data. We first note that the cover model is
584 independent of boulder concentration (Fig. 6). Its prediction does not follow the trend observed in the field
585 data and is equivalent to a case where $W_b = W$. This trivial model yields an RMSE value of 0.48, which
586 forms a benchmark error to which the various width models are compared (Table 2).

587 The tools and the 'tools and cover' effects contain one free parameter, α , which could vary between zero
588 and one, and $d_b/d = 1$ is assumed throughout the analysis. In the case of $\alpha = 0$, both models yield the trivial
589 result of $W_b = W$. Therefore, we turn to present the results of the two models using $\alpha = 1$. The tools effect
590 predicts an increase in the width ratio with boulder-concentration (Fig. 6), with a model-data RMSE of 0.40
591 (Table 2). Although a lower RMSE value than the trivial model, the tools effect underpredicts most of the
592 data. The 'tools and cover' model predicts an increase in the width ratio similar to the tools model. Still, it
593 predicts an even smaller exponent and underpredicts the field data, yielding an RMSE value of 0.40.

594 The multi-channel effect, Eq. (14), is implicit for the boulder-free width W , which also appears on the right-
595 hand side of the equation. Therefore, to compare the model to data, we assign the measured values of
596 boulder-free width W (using the Google-Earth derived channel width; see Fig. S2), mean boulder diameter
597 D_B , and boulder-concentration for each data point. The parameter c can be interpreted as the number of
598 boulders constituting a boulder pile along the cross-section (Fig. 5). Here, to represent the uncertainty in c ,
599 we assume that it takes values between 1 and 4. The multi-channel model plots relatively close to the field
600 data (Fig. 7A). Considering the error on W_b/W and the uncertainty in c , the model accounts for 75% of the
601 Liwu width ratio data. The RMSE between the field and best-fit model width ratios is 0.51, which is larger
602 than the prediction for $W_b = W$.

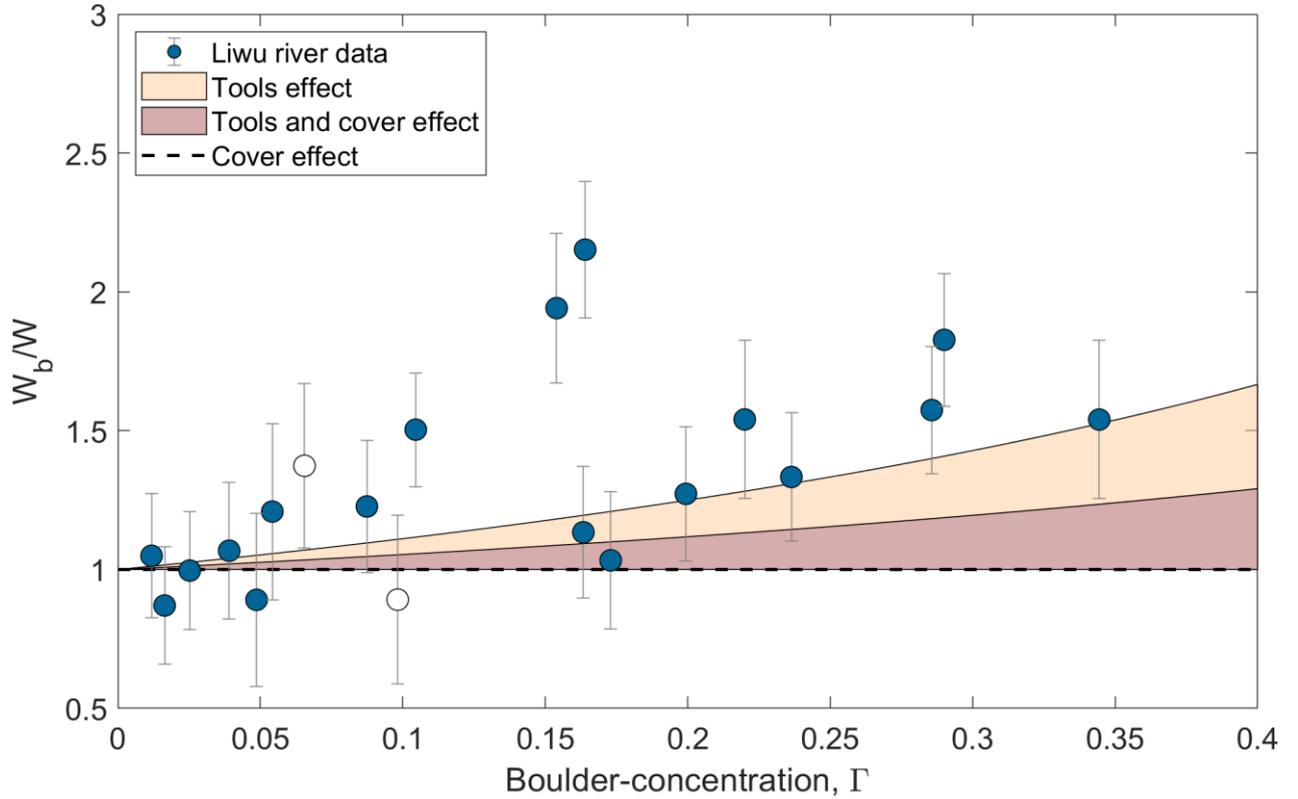


Figure 6: The width ratio W_b/W versus boulder-concentration (Γ) compared between the Liwu River field data (blue circles) and three models: (I) the tools effect (Eq. (8); orange shaded area depicts the model output range when the parameter α is varied between zero and one), (II) the ‘tools and cover’ effect (Eq. 9; red shaded area, using the same range for α range as in the tools effect), and (III) the cover effect (Eq. 6; black dashed line). The tools and the ‘tools and cover’ models predict that the width ratio to increase as a response to an increase in boulder-concentration, while the cover effect is constant. All models are plotted using $d_b/d = 1$. The notation for the white circles is given in the caption of Fig. 3.

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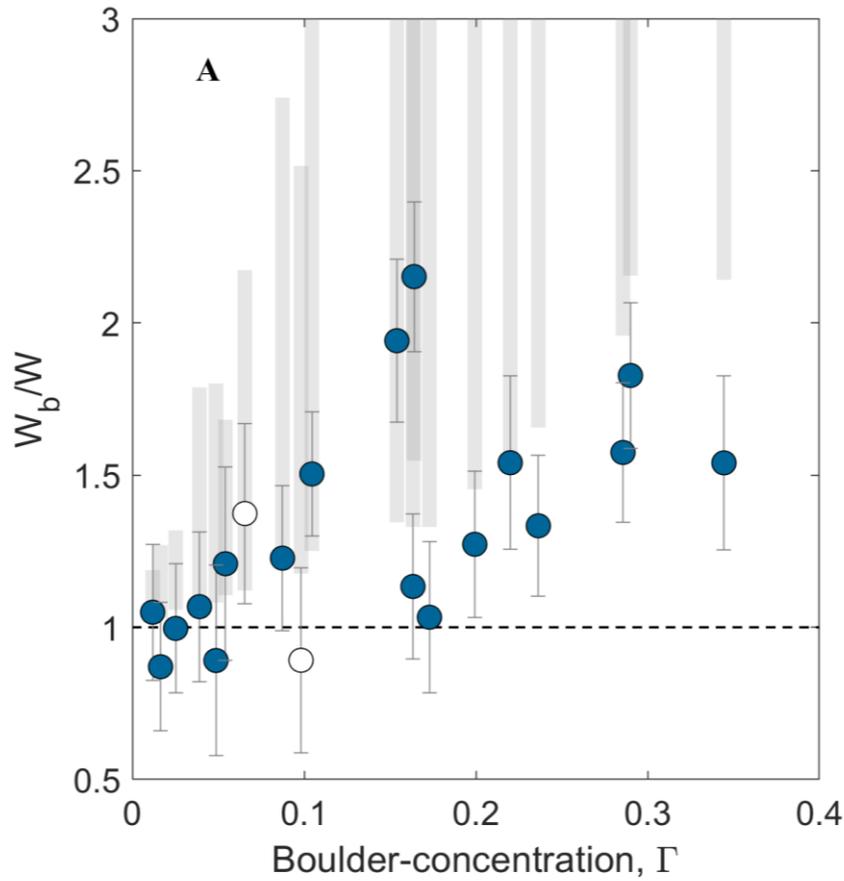


Figure 7: The width ratio W_b/W versus boulder-concentration Γ compared between the Liwu river field data and the multi-channel effect model. The width ratio data is plotted versus boulder concentration (blue and white circles). Each gray bar represents the application of the model (Eq. 14) on a single field data point by using the specific boulder-free width of that boulder-bed channel reach. The vertical range of the gray bar represents uncertainty in the parameter c , which is varied between 1 and 4. The notation for the white circles is given in the caption of Fig. 3.

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5.2 Reduction in Sediment Transport Efficiency

629 The reduction of sediment transport efficiency model, equation (21), combines both the width and
 630 slope ratios and therefore requires a second equation or independent data to close the system. Furthermore,
 631 to solve equation (21), the parameters q , n , θ , and ν need to be constrained. The parameter q was shown to
 632 take end-member values of 0, 0.1, 1, and $5/2$ (Section 4.2.1). We study the behavior of q on the model since
 633 its appearance in Eq. (21) implies a covariant effect of channel width and channel slope. For each q value
 634 explored, we iterated and chose random values of the remaining unknown parameters: n , θ , and ν from a
 635 specified range of values and selected those that minimized the RMSE value between the model output and

636 the Liwu data. Using the tools model to replace W_b/W and $\alpha = 1$, when q is low (i.e., equals zero or 0.1),
 637 the model captures the increase in S_b/S with Γ (Fig. 8). In contrast, for larger values of q , the model deviates
 638 significantly from the data. The model performs best (lowest RMSE) when q is close to or set to zero (Table
 639 2), which corresponds to a case where the slope ratio S_b/S is independent of the width ratio W_b/W .

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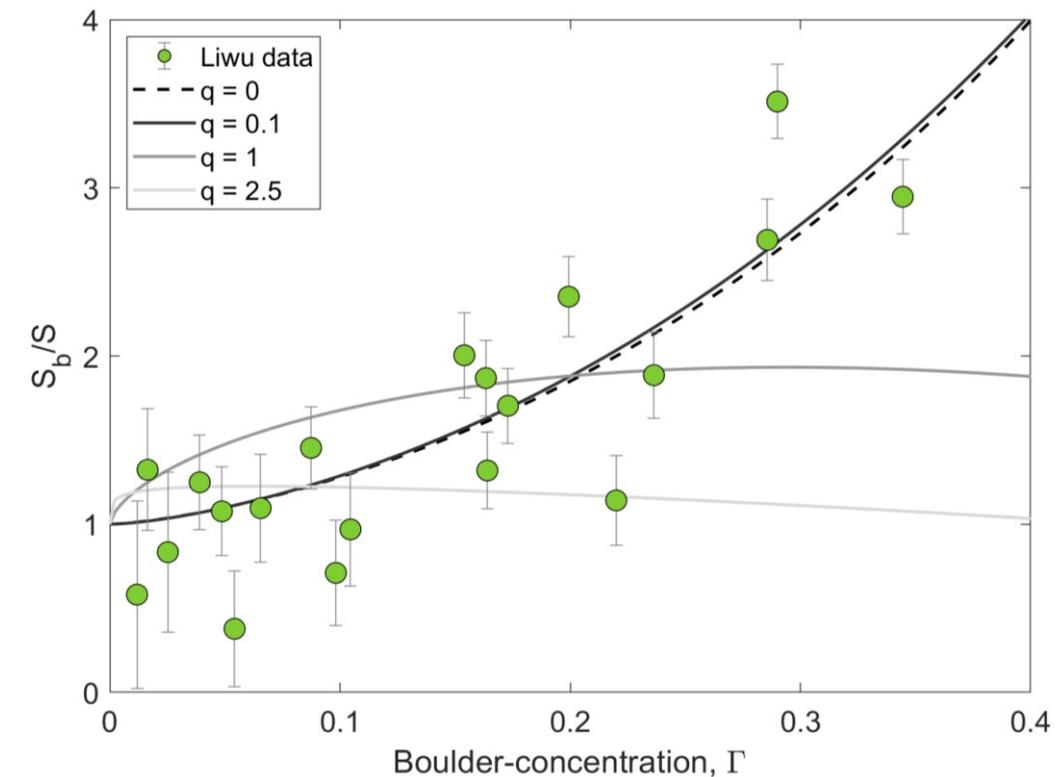
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Figure 8: Influence of the parameter q (Eq. 22) on the ‘reduction in sediment transport efficiency’ model behavior. For each selected q value (see legend), we varied n , θ , and ν and documented the resultant RMSE value between the model and Liwu slope ratio S_b/S . The plotted curves are model simulations of which the RMSE values were lowest. Note the deviation of the model from the data for larger q values (i.e., for q values of 1 and 2.5).

653

653 5.3 The Effect of Shear-stress Partitioning

654 Here we aim to examine whether the shear-stress partitioning model can independently explain the Liwu
 655 River width and slope ratios. To test the model, we changed either β or Γ_{max} , while treating the other as a
 656 constant (see below). The parameter β defines how fast the normalized drag stress increases with increasing
 657 Γ (Eq. 25). In contrast, Γ_{max} is the boulder concentration where the normalized drag stress reaches its
 658 maximum. We note that both parameters are only constrained from flume experiments (Canovaro et al.,
 659 2007). Digitizing Canovaro et al.'s (2007) data sets, β ranges between 1.8 and 4.2, while Γ_{max} varies from
 660 0.18 to 0.37. We tested Eq. (28) by first plotting model predictions using a constant $\Gamma_{max} = 0.3$ while

661 exploring a range of β values that fit the width ratio data. Then, $\beta = 1.25$ was held constant while Γ_{max} values
662 were varied to study their role in controlling model behavior.

663 Exploring the model, we find that it predicts a non-monotonic trend. At small boulder concentrations, the
664 width ratio is predicted to increase, then it reaches a maximum, after which it predicts a decrease in width
665 ratio with increasing boulder concentration (Fig. 10). For a given Γ_{max} , larger β shifts the width ratio maxima
666 and magnitude towards larger Γ values and larger W_b/W values, respectively (Fig. 9A). A similar behavior
667 is observed when increasing Γ_{max} (Fig.9B). A model with $\beta = 1.0$ captures 60% of the width ratio data
668 within one STD error, so does. To test whether the data set can be described by a non-monotonic model,
669 we evaluated Spearman's rank correlation coefficient between the width ratio and boulder-concentration. A
670 calculated value of 0.65 implies that the two variables are positively correlated (for comparison, the rank
671 correlation coefficient between the slope ratio and Γ is 0.76). However, a non-monotonic relationship
672 cannot be ruled out.

673 Considering the effect of the shear stress partitioning on the slope ratio, in section 3.2.2, we showed that
674 the slope ratio depends on boulder concentration to a maximum power of 1/7. Regardless of the choice of
675 the other free parameters, this produces only a weak dependency between the slope ratio and boulder
676 concentration, which makes the shear stress partitioning model inadequate to describe the Liwu slope ratio
677 data (Fig. 10).

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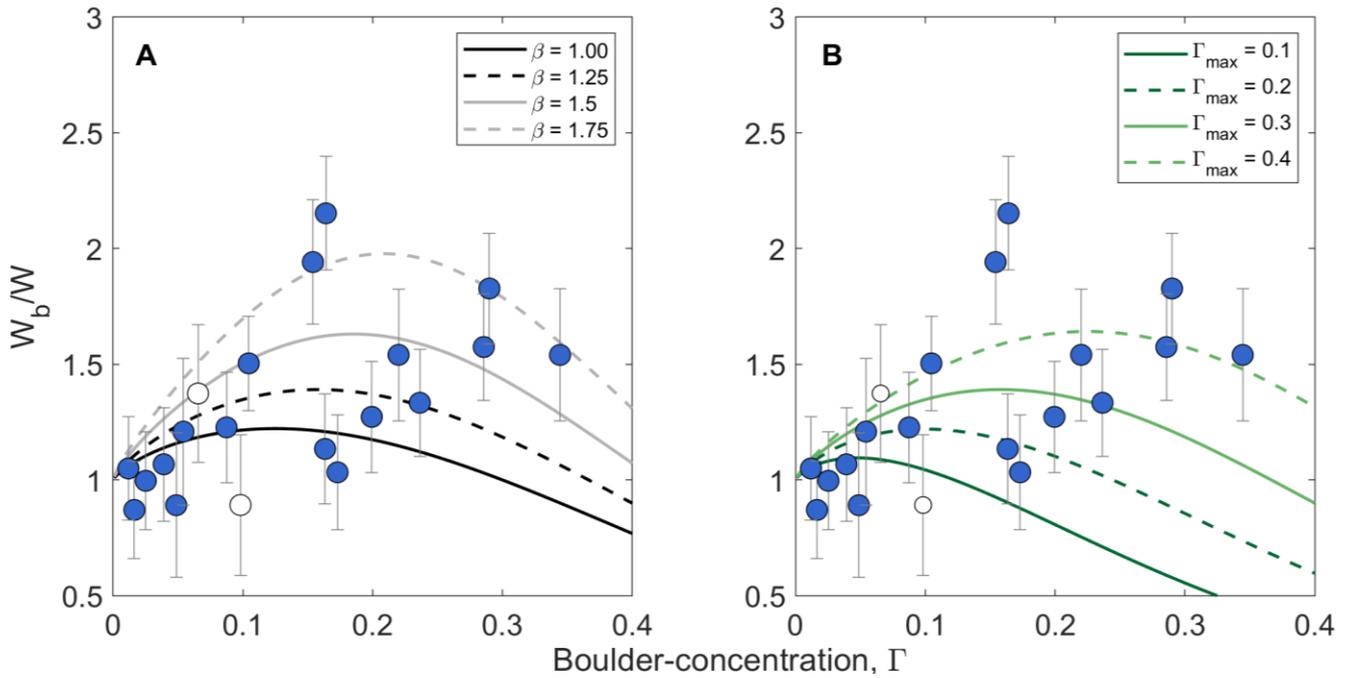


Figure 9: The width ratio W_b/W versus boulder-concentration Γ compared between the Liwu river field data (blue and white circles) and the ‘shear-stress partitioning’ model using different model parameters. (A) The parameter $\Gamma_{max} = 0.30$ is kept constant while β is varied between 1.00 and 1.75. Model scenarios (black and grey curves) show that the width ratio increases with boulder-concentration, but then reaches a maximum, after which it decreases. A fraction of 95% of the data is predicted using the specific range of β values (see legend). The maximum width ratio for each scenario increases with increasing β . (B) the parameter $\beta = 1.25$ is kept constant whereas Γ_{max} is varied between 0.1 and 0.4. As in (A), this figure indicates a humped relationship, with a maximum in width ratio that increase with Γ_{max} . The notation for the white circles is given in the caption of Fig. 3.

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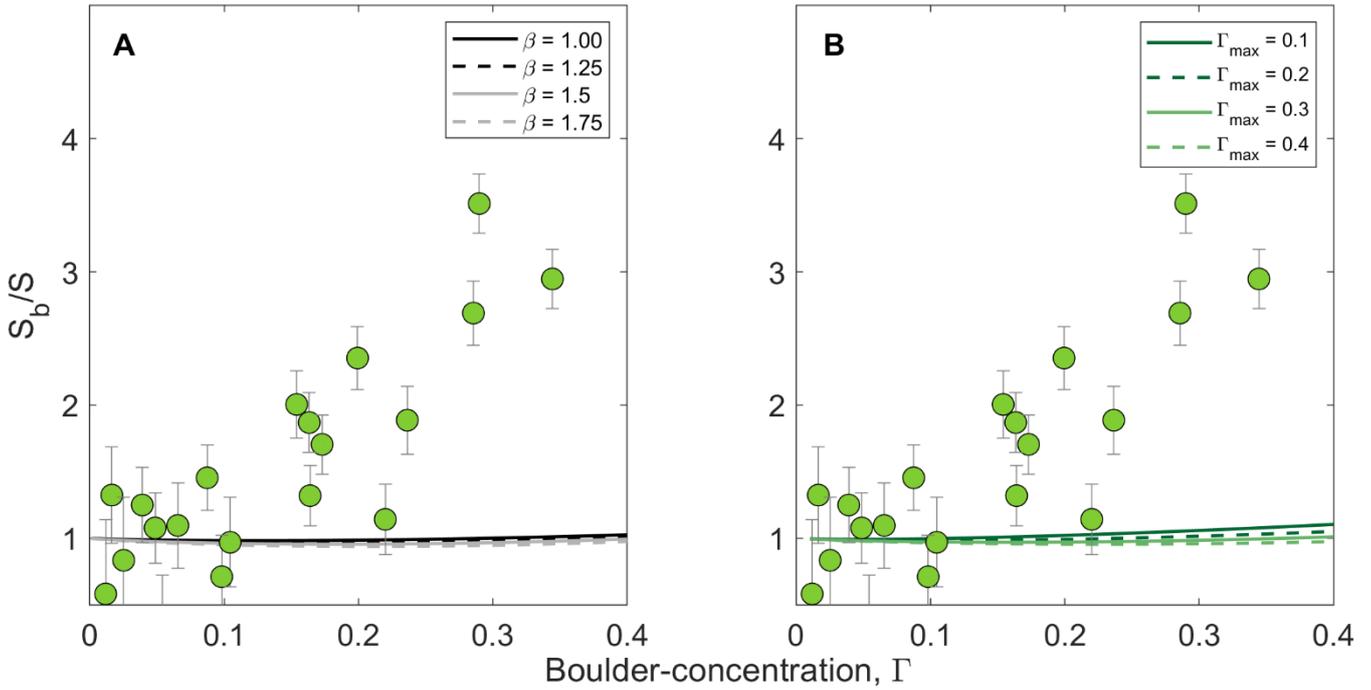


Figure 10: The width ratio S_b/S versus boulder-concentration Γ compared between the Liwu river field data (green circles) and the ‘shear-stress partitioning’ model (Eq. 29) using different model parameters, and $\delta = 2/3$ a constant. (A) The parameter $\Gamma_{max} = 0.30$ is kept constant while β is varied between 1.00 and 1.75. The model scenarios (black and grey curves) show that the slope ratio slightly increases with boulder-concentration, but do not capture the Liwu River slope ratio data. (B) the parameter $\beta = 1.25$ is kept constant whereas Γ_{max} is varied between 0.1 and 0.4. As in (A), slope ratio increases very subtly with Γ and cannot account for the slope ratio data.

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710 **6. Discussion**

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712 **6.1. Reviewing the Assumptions of Steady-States**

713 In our theoretical framework, we have assumed steady-state and tested the resulting equations using
714 field data from the Liwu River. Among the examined models, some have produced higher goodness-of-fit
715 values (e.g., the reduction of transport efficiency effect), while others showed a certain degree of
716 incompatibility compared to the data (Section 4; Table 2), thus requiring an assessment of the applicability
717 of the steady-state assumptions.

718 *Steady-State in the Erosional Balance Assumption*

719 Under the steady-state assumption in the erosional balance, we assume that (i) neighboring boulder-bed
720 and boulder-free reach incise at the same rate. A substantial difference in incision rates between two
721 adjacent channel reaches would promote a knickpoint between the two reaches. We have not observed any
722 such prominent knickpoint at any of the 20 studied sites. (ii) The channel width is at steady-state with
723 respect to erosion rate and fine cover (Turowski, 2018). This assumption is valid if boulders are present at
724 the same reach-averaged concentration at a particular location for a sufficiently long time. In numerous
725 reaches that we examined, there is direct evidence for a continuous supply of large boulders (Text S3).
726 Hillslopes nearby boulder-bed channels often exhibit scars typical of landslides and rockfalls. However,
727 whether those boulders were delivered to the Liwu tributaries recently or if they were placed a long time
728 ago requires further research. Field evidence from other tectonically active sites demonstrates that boulders
729 may last in rivers for periods of tens of thousands of years (Haviv, 2007; Huber et al., 2020). However, a
730 steady-state width configuration is also dependent on how fast the channel widens in response to boulder
731 input. Direct bedrock erosion measurements from the Liwu river reveal that locally, lateral bank erosion
732 can be as significant at tens of centimeters in a single flood season (Hartshorn et al., 2002; Turowski et al.,
733 2008). Hence, channel widening probably occurs much faster in the Liwu River than elsewhere. Ultimately,
734 boulder-bed channel width in the Liwu river may be at a steady-state with respect to uplift, sediment supply,
735 and discharge, but whether width has completely adjusted to boulder input requires further investigations
736 concerning the durability of boulders once they arrive into the river domain. It is also possible that we have
737 not considered different mechanisms responsible for the width anomaly in the Liwu River.

738 *Steady-State in the Grade Assumption*

739 Under the assumption of a grade steady state, we have assumed that sediment-flux in the boulder-bed
740 and boulder-free reaches are the same. This assumption does not require a continuous supply of boulders
741 into the channel but rather a fast response of the river to change the ability to transport sediment with the

742 same efficiency due to boulder-concentration. Specifically, according to Eq. (15), the 'grade' assumption
743 requires that sediment-bed elevation h_s above the bedrock is steady in the long term. Thus, for a channel
744 that has been recently supplied with large boulders, how rapidly can a river restore its sediment transport
745 capacity? We demonstrated that grade conditions could be achieved by adjusting the sediment thickness to
746 form a new channel slope. The rate at which new sediment bed slope forms depends on various hydrological
747 and morphological parameters, such as water discharge, shear stress, and the grain size of the mobile
748 sediment (e.g., Barry et al., 2004). The Liwu river may be a locality in which large variability in water
749 discharge (Lague et al., 2005) and magnitude are expected to promote more sediment transport events in a
750 given flood season (Hartshorn et al., 2002; Dadson et al., 2003). For example, observations from the Liwu
751 River show that the river can remove sediment a few meters in depth following a significant typhoon event
752 (Lague, 2010). Even if boulders disappear quickly once arriving in the fluvial system, the timescale of
753 bedload entrainment and deposition to form a new sediment slope in general and grade conditions, in
754 particular, may correspond to a single flood (Turowski, 2020). Field evidence from various bedrock
755 channels supports recognizing an equilibrium, or 'grade,' in many bedrock river environments (Phillips and
756 Jerolmack, 2016), reinforcing the plausible assumption that the Liwu river is at an approximate sediment
757 transport steady-state, or in grade, at nearly all times.

758

759 **6.1. Evaluation of the Theoretical Models**

760 Under the two steady-state assumptions described in sections 4.1 and 4.2, we formalized five
761 mechanisms presumably underlying the observations of both widening and steepening of boulder-bed
762 channels (Table 2). Below, we examine and discuss the performance of the models to describe the Liwu
763 data channel width and slope predictions using the erosional balance and grade-based mechanisms

764 Five models have been considered for testing the width ratio, W_b/W : the cover, the tools, the 'tools
765 and cover,' the multi-channel effect, and the shear-stress partitioning effect. The first three models are
766 dependent on the ratio of the square root of boulder-bed to boulder-free deflection lengths (Eqs. 6, 8, and
767 9), which we assumed to be one, i.e., $d_b = d$. The deflection length likely depends on grain size, hydraulic
768 parameters (Turowski, 2020), the contact angle of the boulder with the mobile particle (Fuller et al., 2016;
769 Beer et al., 2017; Li et al., 2020), bedload path relative to the location of a roughness zone (He et al., 2021),
770 and fluid shear stress (Li et al., 2020; Turowski, 2020). The influence of boulder concentration on sediment
771 deflection is currently unknown, but a positive correlation may account for channel widening for the above-
772 discussed models beyond the predictions with $d_b = d$.

773 The cover model predicts that W_b/W equals $\sqrt{d_b/d}$, meaning that as long as $d_b = d$, (I) the width
774 ratio does not independently depend on Γ , and (II) there is no boulder-bed widening with respect to a
775 boulder-free reach. Considering the above, although our theoretical framework of the cover effect does not
776 reproduce the Liwu width ratio data, future advances in our understanding of the relation between deflection
777 length and roughness elements could lead to a modified cover model for channel width that depends on Γ
778 as has been hypothesized for slope (Shobe et al., 2021).

779 The tools (Eq. 8) and the 'tools and cover' (Eq. 9) models predict an increase in the width ratio with
780 boulder-concentration (Fig. 6). The essential difference between the two models is in the exponent, which
781 depends on the parameter α , describing whether bedload particles are routed above boulders ($\alpha = 0$) or not
782 ($\alpha = 1$). At the process scale, large boulders protruding into the flow are thought to encourage sediment
783 deposition around them (e.g., Papanicolaou and Kramer, 2006; Tsakiris et al., 2014; Polvi, 2021), which
784 may lead to substantially different protrusion, causing bedload transport to alter significantly (Yager et al.,
785 2007). We thus hypothesize that boulder protrusion and hydraulic behavior near boulders have an essential
786 role in controlling α .

787 The multi-channel effect (Eq. 14) predicts an increase in the width ratio with boulder concentration
788 (Fig. 7). For a given boulder-bed channel, the model plots relatively close to the data but commonly
789 overpredicts it, especially for large boulder-concentration values. Given the overall over-prediction of the
790 data and the relatively large RMSE value, we propose that the model with its current assumptions is
791 unsuitable for boulder-bed channels in the Liwu River. We envision three major potential causes for the
792 model-data deviations.

793 The model was derived using three primary assumptions: (I) the channel reach follows a specific
794 geometry, including boulder arrangement (Fig. 5), (II) sediments are redistributed evenly between the in-
795 channels, and (III) the overall boulder-bed channel width independently reflects a steady-state configuration
796 for every in-channel. The Liwu boulder-bed channel reaches, however, exhibit a wide range of boulder
797 sizes and inner-reach distributions. Furthermore, at bankfull flows, when the entire bed is submerged,
798 sediments are expected to follow paths set by the flow hydrodynamics—rather than the configuration of
799 boulders—and not be evenly distributed. We believe that some of the scatter of the data concerning model
800 predictions are due to such discrepancies. To better capture the width ratio variability, specific treatments
801 of boulder distributions and sediment paths can be considered in future studies

802 The effect of shear-stress partitioning shows a humped relationship between width ratio and Γ ,
803 which can be explained by the non-monotonic log-linear model Eq. (25) used to derive the model. Although
804 the effect captures 60% of the data within the errors, we emphasize two reasons for the model's inadequacy
805 of the Liwu data. First, a simpler, linear model could also account for that fraction captured by the non-

806 monotonic model. Second, the parameters β and Γ_{max} need to be different between the different reaches, but
807 independent constraints on their values are missing. As a result, the shear-stress partitioning model cannot
808 predict well the width ratio. While the physical interpretation of β is unclear, we cannot evaluate the extent
809 to which this parameter should vary among the examined reaches. Differences between channel reaches
810 could emerge from contrasts in the boulder size distributions and the streamwise and cross-sectional
811 location distributions.

812 Although the tools and shear-stress partitioning models statistically performed best overall (Table
813 2), the role of multi-channels in shaping boulder-bed channel width cannot be ruled out. Furthermore,
814 additional investigations are awaiting to unravel the role of cover in the relationship between width and
815 boulder presence (e.g., Shobe et al., 2020). However, the overall inability of the models to account for the
816 width anomaly in the Liwu River, and the long timescale of width adjustment implied from the scatter in
817 our data all drive us to suspect that different reaches have adjusted to boulder input to various degrees.

818 Two models have been considered for testing the slope ratio, S_b/S : reduction in transport efficiency and
819 shear-stress partitioning. Both were developed under the assumption of grade. We first note that the shear-
820 stress partitioning effect cannot explain the slope ratio increase in the Liwu River (Fig. 10). Thus, this
821 model can be ruled out in explaining the increase in width ratio with boulder-concentration. The prediction
822 of the reduction in transport efficiency model could explain the trend observed in the data (Fig. 8) yet
823 requires calibration of four parameters. Although, according to this model, in the general case, the slope
824 ratio is a function of the width ratio, we find that the best-fit parameters are those that make the slope ratio
825 independent of the width ratio. This outcome points to a steepening effect that relies solely on sediment
826 entrainment and deposition to form a steeper bed and can occur very fast, probably within one or a few
827 floods. This mechanism differs from the one developed by Shobe et al. (2020), which relied on bedrock
828 erosion to accomplish the slope change, and would therefore have a much longer adjustment timescale. The
829 inferred independence of the slope ratio and the width ratio, manifested by the small q (power of the width
830 ratio), may be a consequence of the substantial difference in the adjustment timescales of bedrock width
831 and sediment-bed slope (Turowski, 2020). In other localities with much softer and erodible banks (e.g.,
832 Cook et al., 2014), the covariation of slope and width are hypothesized to be more significant. Whereas
833 standard models commonly assume that q is either zero or one, it is also possible that the dependence of
834 sediment flux on channel width is diminished in the long term, thus constraining q to be close to zero
835 (Rickenmann, 2001). Further research on the value q for different timescales of sediment transport is
836 needed. Given the good fit and the general agreement of the model with the data, we attribute most of the
837 steepening of the boulder-bed channel reaches to a necessity to mobilize the upstream sediment supply
838 despite the presence of boulders that inhibit sediment transport efficiency.

839 The reduction in transport efficiency model further predicts a monotonic steepening effect with
840 increasing boulder concentration. However, with increasing boulder concentration, we expect channel slope
841 response to potentially reduce as the channel self-organizes a new bed largely composed of boulders such
842 that boulders are no longer significant roughness elements on the bed. This situation is equivalent to the
843 role of boulder spacing, shown by flume experiments, to strongly influence grade conditions (McKie et al.,
844 2021). Each boulder generates a unique zone susceptible to flow reversals and enhanced turbulence
845 (Papanicolaou and Tsakiris, 2017). However, when the spacing is small, the different boulder-influenced
846 zones interact, causing an overall reduction in the total influence zone. Our developed equation does not
847 show this behavior because of the assumption that the transport efficiency reduces monotonically for the
848 entire range of Γ (Eq. 19).

849 **6.2. Causality Relations between Boulder Concentration and Channel Width**

850 The models proposed to explain the observed relation between boulder concentration and the width
851 ratio assume that channel width adjusts (and is, therefore, the dependent variable) to boulder concentration.
852 Notwithstanding, the causality between the two variables can also be presented inversely. Here we pose a
853 hypothesis for a potential dependence of boulder-concentration on channel width. Consider a case in which
854 boulders have an equal probability of arriving at a specific location within the river and assume an initial
855 natural variability in channel width along the river. In wider reaches, the fluid shear-stress deriving both
856 bedload transport, which is responsible for boulder abrasion (Wilson et al., 2013) and boulder
857 transportation, is smaller relative to a narrow channel with otherwise the same parameters. Since bedload
858 transport depends on discharge and erosion depends on bedload, boulders will both abrade and be
859 transported quicker in narrower channels. In such a case, observations would be of a positive scaling of
860 channel width with boulder concentration. However, we specify three reasons why such a case is probably
861 not valid for the Liwu River. First, we do not have direct evidence for initial width variability. Second, an
862 initial spatial variability in channel width between neighborhood reaches is less likely because our paired
863 approach of width normalization should also account for lithological and bank properties.

864 The unknown directionality between boulder-concentration and the channel width is a '*chicken or egg?*'
865 problem, where cause and causality between the two variables are potentially bi-directional. Ultimately, we
866 speculate that once boulders arrive into the channel, the effects outlined above interact to form a new steady-
867 state width configuration (Turowski, 2018). Nearby failure events can produce new boulders, which in turn
868 contribute to the adjustment of channel width.

869

870 7. Conclusions

871 We studied the controls of large immobile boulders on channel width and slope in bedrock channels.
872 Our data from the Liwu River, Taiwan, show that sediment-bed slope and bedrock width increase in
873 response to higher concentrations of boulders after width and slope are normalized for variations due to
874 drainage area. We invoked rock and sediment mass balance principles to explore possible mechanisms
875 responsible for the observed width and slope increase with boulder concentration. We combined them in a
876 theoretical framework for fluvial bedrock erosion and sediment transport. The theoretical framework yields
877 analytic predictions for the width and slope ratios as a function of boulder concentration.

878 Under the first principle of rock mass balance, we assumed that boulder-bed and boulder-free reaches
879 incise into bedrock at the same rate. We expanded this assumption by considering three effects that boulders
880 impose on the process of bedrock erosion: the cover, the tools, and the multi-channel effect. These models
881 yielded solutions to the width ratio. Under the second principle, we assumed that bedload flux in adjacent
882 boulder-bed and boulder-free reaches is identical under equilibrated grade conditions. Here, two underlying
883 mechanisms were examined for the effect of boulders on bedload transport: a reduction in the efficiency of
884 sediment mobilization and a reduction in the shear stress responsible for sediment mobilization. Both
885 mechanisms yielded solutions for the slope ratios, while the second mechanism provided an independent
886 solution to the width ratio.

887 The width ratio trend was best captured by the tools effect, yet this model underpredicted most of the
888 data. The shear-stress partitioning model can account for a fraction of the width data, but requires
889 knowledge on its numerous parameters, which are not constrained. Under the boulder cover effect, width
890 is insensitive to boulder concentration. Still, an emerging relationship between sediment deflection and the
891 existence of boulders is hypothesized to yield a link between width and boulder-concentration due to a
892 boulder cover effect. The multi-channel effect demonstrated an increase of width but predicted larger width
893 values than mostly seen in the Liwu data. We conclude that the scatter in the data points out to a long
894 timescale adjustment of channel width, and different reaches have adjusted to different extents.

895 The slope ratio was best captured by the effect of a reduction in sediment transport efficiency, with
896 little to no dependence on channel width. In contrast, a shear-stress partitioning effect cannot explain the
897 slope ratio.

898 The theoretical framework presented in this paper is a first attempt to examine and test various physical
899 mechanisms controlling the relationship between bedrock channel morphology and large boulders. We
900 acknowledge two primary key future research questions emerging from our work. First, we have
901 insufficient insights into the dynamics of bedload relating to sediment deflection in vicinity to boulders.
902 Many of our model predictions may improve when the controls on the deflection length scale are better

903 understood. Second, revealing the durability of boulders in bedrock channels is expected to promote
904 understanding of the processes operating in the presence of boulders and the consequence on channel
905 morphology.

906

907 **Author Contributions**

908 R.N., J.M.T. and L.G. conceived the study and developed the theory. R.N. collected the data, performed
909 the analysis, and wrote the manuscript with input from all authors.

910

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916

917 **Conflict of interests**

918 The authors declare that they have no competing interests.

919

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927

928 8. Appendix A: Slope Solution to the Shear-stress Partitioning effect

929 Here we solve the equation of shear-stress partitioning (Section 4.2.2) for the slope ratio. First, from
 930 geometry and continuity, it follows that (Turowski, 2021)

$$931 \quad 2Q \left(\frac{\tau}{\rho g} \right) = QSW - K_V W^2 S^{\frac{1}{2}-\delta} \left(\frac{\tau}{\rho g} \right)^{1+\delta} \quad (\text{A1})$$

932 For intermediate width, the term on the left-hand side of the equation can be neglected, and (A1) can be
 933 solved for channel width

$$934 \quad W = (\rho g)^{\delta+1} \frac{QS^{\delta+0.5}}{K_V} \tau^{-(\delta+1)} \quad (\text{A2})$$

935 For a boulder-bed channel, Eq. (A2) can be rewritten as

$$936 \quad W_b = (\rho g)^{\delta+1} \frac{QS_b^{\delta+0.5}}{K_V} \tau_m^{-(\delta+1)} \quad (\text{A3})$$

937 Dividing (A3) by (A2)

$$938 \quad \frac{W_b}{W} = \left(\frac{S_b}{S} \right)^{\delta+0.5} \left(\frac{\tau_m}{\tau} \right)^{-(\delta+1)} \quad (\text{A4})$$

939 From (27), it follows that

$$940 \quad \frac{W_b}{W} = \left(\frac{\tau_{red}^*}{\tau^*} \right)^{-3/2} \quad (\text{A5})$$

941

942 Equating equations (A4) and (A5) and solving for the slope ratio

$$943 \quad \frac{S_b}{S} = \left(\frac{\tau_m}{\tau} \right)^{\frac{\delta-0.5}{\delta+0.5}} \quad (\text{A6})$$

944 Finally, Eq. (26) is substituted into (A6) to yield a solution for the slope ratio as a function of boulder-
 945 concentration (Eq. 29).

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948 9. References

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