

1 **Ionospheric Sluggishness: A Characteristic Time-Lag of the**  
2 **Ionospheric Response to Solar Flares**

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10 **Key Points:**

- 11 • The choice of ionospheric sounding techniques and reference solar irradiance  
12 wavebands affects the estimation of ionospheric sluggishness
- 13 • A simulation study shows that the D-region effective recombination coefficient  
14 varies by 4 – 5 orders of magnitude
- 15 • It is suggested that ionospheric sluggishness might be influenced by the ionic  
16 (negative and positive cluster ions) photochemistry

## 17 Abstract

18 The term “ionospheric sluggishness” is used to describe the time delay between  
19 maximum radio absorption in the ionosphere following the time of maximum irradiance  
20 during a solar flare. Sluggishness is one of the characteristic properties known to be  
21 maximized around D-region heights and can be used for studying lower ionospheric  
22 (D-region) and mesospheric chemistry. This article is our first attempt to estimate  
23 ionospheric sluggishness using high frequency (HF, 3 – 30 MHz) instruments.  
24 Specifically, we report on first estimates of sluggishness from riometer and  
25 SuperDARN observations following a solar flare and propose two new methods to  
26 estimate sluggishness. Sluggishness is shown to be anti-correlated with the peak solar  
27 X-ray flux and positively correlated with solar zenith angle and geographic latitude.  
28 The choice of instrument, method, and reference solar waveband effects the  
29 sluggishness estimation. A simulation study was performed to estimate the effective  
30 recombination coefficient, which was found to vary between 4 – 5 orders of magnitude.  
31 We suggest that the effective recombination coefficient is highly sensitive to D-region’s  
32 negative and positive ion chemistry.

## 33 Plain Language Summary

34 A systematic time delay between peak incoming solar radiation during a solar flare  
35 and peak electron density in the ionosphere is known as ionospheric sluggishness.  
36 Ionospheric sluggishness is known to be maximized around D-region heights (~60-90  
37 km altitude). This article is our first attempt to estimate ionospheric sluggishness using  
38 high frequency (3 – 30 MHz) instruments. In addition, we statistically characterize the  
39 observed sluggishness and provide an insight into D-region photochemical processes.  
40 In this article, we also demonstrate how to extract D-region’s recombination coefficient  
41 using a theoretical model and measured sluggishness.

## 42 1. Introduction

43 Solar EUV and X-rays radiations are primary sources for producing the ionosphere.  
 44 The characteristic ionospheric response to a sudden intense solar X-ray burst, or solar  
 45 flare, has been studied since the early 1900s (Dellinger, 1937). Flare-driven high  
 46 frequency (HF; 3-30 MHz) absorption, also known as shortwave-fadeout (SWF), is a  
 47 well-understood phenomenon (e.g., Mitra, 1974; Fiori et al., 2018). However, the initial  
 48 time delay of the ionospheric response following a solar flare, also known as  
 49 “sluggishness”, is not yet fully understood (Palit et al., 2015). E. V. Appleton first  
 50 defined the term sluggishness as the time delay between the peak ionospheric electron  
 51 density and peak electron-ion production rate at local solar noon (Appleton, 1953). We  
 52 now understand sluggishness as an inertial property of the ionosphere that is dependent  
 53 on latitude, longitude, and height of the ionosphere, as described in equation (1)  
 54 (Appleton, 1953).

$$55 \delta = \delta(\theta, \phi, h) = T_{n_e^{max}} - T_{q^{max}} \quad (1)$$

56 where:  $\theta, \phi, h, T_{n_e^{max}}$ , and  $T_{q^{max}}$  are latitude, longitude, altitude, times of peak electron  
 57 density, and peak electron-ion production rate, respectively. In addition, Appleton  
 58 found that  $\delta$  is inversely proportional to electron density and the effective  
 59 recombination coefficient ( $\alpha_{eff}$ ). Appleton and his contemporaries tried to measure  
 60 and characterize sluggishness in terms of the time delay between peak radio wave  
 61 absorption ( $\beta$ ) in the ionosphere and peak solar irradiance ( $I_{\infty}^{max}$ ) (Appleton, 1953;  
 62 Ellison, 1953), as described in equation (2).

$$63 \bar{\delta} = \bar{\delta}(\theta, \phi) = T_{\beta^{max}} - T_{I_{\infty}^{max}} \quad (2)$$

64 where:  $T_{\beta^{max}}$  and  $T_{I_{\infty}^{max}}$  are the times of peak HF absorption and peak solar irradiance,  
 65 respectively.

66 Consequently, ionospheric sluggishness is the time difference between the peak of  
 67 solar flux and ionospheric response. However, recent studies have shown that some HF  
 68 instruments undergo a saturation effect (a flat peak in the observation, see section 3.1  
 69 for details) due to substantial ionospheric HF absorption effect, in response to an X-  
 70 class solar flare (Chakraborty et al., 2018, 2019). Hence, the standard definition by  
 71 equation (2) will not provide an accurate measurement of sluggishness using  
 72 SuperDARN data. Hence, we propose two alternative definitions of sluggishness. First,  
 73 we define it as the time difference between the peak in the time derivative of  $\beta$  and the  
 74 peak in the time derivative of  $I_{\infty}$  (i.e.  $\bar{\delta}_s$  a name), as described in equation (3).  
 75  
 76  
 77

$$78 \bar{\delta}_s = \bar{\delta}_s(\theta, \phi) = T_{\dot{\beta}} - T_{\dot{I}_{\infty}} \quad (3)$$

79 where:  $T_{\dot{\beta}}$  and  $T_{\dot{I}_{\infty}}$  are the times of peak time derivative in absorption and peak time  
 80 derivative in solar irradiance, respectively. Second, we define the time shift ( $\tau$ ) in  $I_{\infty}$   
 81 that maximizes the correlation ( $\rho$ ) between  $\beta$  and  $I_{\infty}$ , as described in equation (4).  
 82

$$83 \bar{\delta}_c = \bar{\delta}_c(\theta, \phi) = \max_{\tau} \rho[\beta(t), I_{\infty}(t + \tau)] \quad (4)$$

84 Note that  $\bar{\delta}$ ,  $\bar{\delta}_s$ , and  $\bar{\delta}_c$  represent time delays between a change in solar irradiance  
 85 and an ionospheric response, whereas  $\delta$  represents the time delay between peak  
 86 photoionization rate and peak ionospheric electron density. Specifically,  $\bar{\delta}$  represents  
 87 the time delay between the peak in the HF absorption and peak solar irradiance of the  
 88 event, whereas  $\bar{\delta}_s$  represents the time delay when both solar irradiance and ionospheric  
 89 response are changing most rapidly (during the peak of time derivative) and  $\bar{\delta}_c$   
 90 represents the time delay that maximizes statistical similarities between solar irradiance  
 91 and ionospheric response. Although the three different time delays defined in equations  
 92 (2)-(4) have different reference times, measurement, and estimation techniques, all of  
 93 them are indicative of the inertial property of the ionosphere. Finally, our proposed  
 94 definitions in terms of peak time derivative and correlation are advantageous for  
 95 characterizing the response of the ionosphere to impulsive events such as flares  
 96 measured using instruments such as riometers and SuperDARN HF radars.

97 Figure 1(a-c) present examples of the estimation of height integrated ionospheric  
 98 sluggishness  $\bar{\delta}$ ,  $\bar{\delta}_s$ , and  $\bar{\delta}_c$  using the conventional, peak time derivative, and  
 99 correlation methods, respectively. The data were obtained with the Ottawa riometer  
 100 data during a solar flare event on 11 March 2015. The red curve and black dots in all  
 101 three panels indicate solar soft X-ray (.1-.8 nm) irradiance from a GOES satellite and  
 102 cosmic noise absorption (CNA) from the Ottawa riometer, respectively. The solid and  
 103 dashed vertical lines in panel (a) and (b) indicate peaks and maximum time derivative  
 104 in X-ray irradiance (red) and CNA data (black), respectively. The difference in the solid  
 105 [dashed] vertical lines in panel (a) [(b)] represents the estimated conventional [time  
 106 derivative] sluggishness. Furthermore, the red dashed curve in panel (c) shows the time-  
 107 shifted solar soft X-ray (.1-.8 nm) irradiance. The correlation coefficient and estimated  
 108 sluggishness are shown in the panel. The estimated sluggishness from the three  
 109 different methods are  $\bar{\delta} = 46s$ ,  $\bar{\delta}_s = 139s$ , and  $\bar{\delta}_c = 80s$ , for this event, respectively.

110 Since Appleton first described sluggishness, experimental studies have used very  
 111 low frequency (VLF, 3-30 kHz) receivers to understand its variations with solar zenith  
 112 angle ( $\chi$ ), and peak solar irradiance  $I_{\infty}^{max}$  (Ellison, 1953; Palit et al., 2015). The  
 113 sluggishness recorded using VLF instruments is defined as the time difference between  
 114 the peak in VLF amplitude ( $A^{max}$ ) and  $I_{\infty}^{max}$ , as described in equation (5).  
 115

$$\delta^{VLF} = T_{A^{max}} - T_{I_{\infty}^{max}} \quad (5)$$

116 VLF Studies have reported a typical value of sluggishness ( $\delta^{VLF}$ ) is 3-10 minutes  
 117 (Basak & Chakrabarti, 2013; Palit et al., 2015). Most of these studies reported wide  
 118 variability of sluggishness values during M and C class flares but did not try to explain  
 119 the chemical processes that manifest the sluggishness.  
 120

121 Sluggishness measurements are useful because they provide information about the  
 122 ionospheric electron density and the effective recombination coefficient ( $\alpha_{eff}$ )  
 123 (Appleton, 1953); the latter being controlled by the atmospheric negative ions (e.g.  
 124  $O^-$ ,  $O_2^-$ ,  $NO_3^-$ ,  $CO_3^-$ ,  $HNO_3^-$  etc and their hydrates) and positive ions (e.g.  $H^+(H_2O)_n$ )  
 125 (Palit et al., 2015; Reid, 1970; Verronen et al., 2006). Specifically,  $\alpha_{eff}$  defines the  
 126 effective loss rate of electrons due to cascading photochemical reactions following  
 127 electron production due to photoionization (Pequignot et al., 1991). Sluggishness  
 128 measurements can thus provide insight into D-region and mesospheric photochemistry  
 129 and be used to validate models.

130 Here we report on the first study to compare the basic characteristic of  
 131 sluggishness using both passive and active high frequency (HF, 3-30 MHz) instruments,

132 namely, riometers and SuperDARN HF radars, respectively. We present a statistical  
 133 characterization of ionospheric sluggishness following C, M, and X class flares and  
 134 report on the variations of conventional sluggishness ( $\delta$ ) with  $\chi$ ,  $I_{\infty}^{max}$ , local time (LT)  
 135 and latitude ( $\phi$ ). Through a theoretical modeling study and measured  $\bar{\delta}$  from riometer  
 136 data, we show how  $\alpha_{eff}$  varies with peak solar soft X-ray flux. Finally, we discuss how  
 137 our results inform the physics of sluggishness and its variability, and our understanding  
 138 of D-region photochemical processes.

## 139 2. Instrumentations

140 In this study, we used GOES-15 X-ray sensor data for the solar X-ray irradiance  
 141 information during solar flares and ionospheric absorption in the HF bands from  
 142 ground-based riometers and SuperDARN HF radars, respectively (Bland et al., 2018).  
 143 Solar X-ray flux information was obtained from the solar X-ray sensor of the National  
 144 Oceanic and Atmospheric Administration’s (NOAA) GOES 15 satellite (Machol,  
 145 2016). This instrument has two channels, namely hard (0.05-0.4 nm) and soft (.1-.8 nm),  
 146 to detect variations in solar flux in these two wavebands. We primarily used soft X-ray  
 147 (SXR) flux for our analysis; however, hard X-ray (HXR) information is also used for  
 148 comparison.

149 A riometer is a ground-based passive radio receiver, which provides information  
 150 about the ionospheric HF absorption by measuring variations in cosmic radio noise at  
 151 30 MHz frequency (e.g., Browne et al., 1995; Fiori & Danskin, 2016). The CNA values  
 152 used in this study are taken from a network of riometers distributed across Canada  
 153 operated partially by Natural Resources Canada (NRCan) and partially by the  
 154 University of Calgary (Geospace Observatory riometer, or GO-RIO) (Danskin, 2008;  
 155 Lam, 2011; Rostoker et al., 1995).

156 SuperDARN is a global network of HF radars, operating between 8 and 18 MHz,  
 157 located across the middle, high and polar latitudes of both hemispheres. Each radar  
 158 observes the line-of-sight (LoS) component of plasma velocity along 16 to 20 beams in  
 159 75-110 range gates spaced 45 km apart beginning at 180 km range (Chisham et al.,  
 160 2007; Greenwald et al., 1985; Nishitani et al., 2019). Typically, each beam sounding  
 161 has a 3s or 6s integration period, resulting in a full radar sweep through all beams in 1  
 162 or 2 minutes. SuperDARN observations primarily consist of two types of backscatter,  
 163 namely, ionospheric scatter and ground scatter. In the case of ground scatter, due to the  
 164 high daytime vertical gradient in the refractive index, the rays bend toward the ground  
 165 and are reflected from surface roughness and return to the radar following the same  
 166 paths. Ionospheric scatter is due to the reflection of the transmitted signal from  
 167 ionospheric plasma irregularities. However, in this study, we will only use the ground  
 168 scatter observations. Specifically, we use the “inverse ground scatter count” during a  
 169 particular period, determined as the drop in ground scatter echo counts during an event  
 170 (i.e., maximum count – actual count) to estimate the ionospheric sluggishness observed  
 171 by the HF radars (Chakraborty et al., 2018).

172 Figure 2 presents the location of the instruments used in this study. Radar fields-  
 173 of-view of SuperDARN radars located in middle and high latitudes across the North  
 174 American sectors are colored in red and blue, respectively. The fields-of-view indicated  
 175 by the shading indicates the region of the ionosphere where SuperDARN is likely to be  
 176 sensitive to solar flare driven fadeout-induced absorption spanning range gates 1-7. The  
 177 green circles centered around the black dots represent the riometers used in this study.  
 178 These filled circles denoting riometer station locations indicate the 100-km diameter  
 179 region around each riometer station where absorption is detected.

### 180 3. Results

181 In this section, we characterize ionospheric sluggishness measured from riometer  
 182 and SuperDARN observations, using the equations defined in Section 1 and describe a  
 183 technique to estimate  $\alpha_{eff}$  from the sluggishness measured by the riometer.  
 184 Specifically, we present one classic example of ionospheric sluggishness in  
 185 SuperDARN observations extracted using the peak time derivative and correlation  
 186 methods proposed in Section 1. Next, we will statistically characterize  $\bar{\delta}$  measured in  
 187 the riometer observations and describe its dependence on  $\chi$ ,  $\phi$ , LT, and  $I_{\infty}$ . Then, we  
 188 discuss the typical practice of using solar SXR as a reference to measure sluggishness  
 189 and compare it with the measurement considering solar HXR as a reference. Finally,  
 190 we describe a theoretical method to estimate  $\alpha_{eff}$  from the sluggishness measured by  
 191 the riometer ( $\bar{\delta}$ ), validate it with the theoretical values, and get an insight into the D  
 192 region chemistry. Note, unlike other two sluggishness, defined by equations (3) and (4),  
 193  $\bar{\delta}$  can only be used to estimate  $\alpha_{eff}$ , hence, we used  $\bar{\delta}$  estimates from riometer  
 194 observations to characterize the behavior of the sluggishness.

#### 195 3.1 SuperDARN Event Study: 11 March 2015

196 As an example, consider an X2.1 solar x-ray flare that erupted on 11 March 2015,  
 197 peaking at 16:22 UT. Fiori et al. (2018) used this event to demonstrate the potential of  
 198 SuperDARN for monitoring the space weather impact due to solar X-ray flares due to  
 199 the widespread observation of the event across Canada and the Northern United States.

200 Figure 3 presents a time series of inverse ground scatter count data from the  
 201 SuperDARN Blackstone radar (black) in response to the sudden increase in solar SXR  
 202 due to a solar flare (red) on 11 March 2015. The dashed red curve represents time  
 203 delayed SXR data. The difference in timing of the peaks in the time derivatives,  
 204 indicated by the red and black vertical dotted lines, represents the sluggishness  
 205 associated with the peak time derivative method, which is  $\bar{\delta}_s = 38$ s. The sluggishness  
 206 estimated using correlation analysis is  $\bar{\delta}_c = 50$ s. Both sluggishness values are  
 207 significantly lower than the values obtained from the riometer measurements using  
 208 peak time derivative and correlation method,  $\bar{\delta}_s = 139$ s and  $\bar{\delta}_c = 80$ s, respectively (refer  
 209 Figure 1(b-c)). This significant difference in the sluggishness measured by the two  
 210 instruments is most likely due to differences in their operating frequencies and the fact  
 211 that riometers are passive receivers and operate in a vertical mode while the  
 212 SuperDARN radars are active oblique sounders.

#### 213 3.2 Correlation Analysis

214 To characterize the statistical behavior of  $\bar{\delta}$  estimated from riometer observations,  
 215 we choose 92 C, 63 M, and 18 X class solar flare events between 2006 to 2017. Note  
 216 that, these solar flare events were selected from GOES XRS reports maintained by  
 217 NOAA when the NRCAN riometers were online, to ensure the largest possible data set,  
 218 and predominantly located on the dayside such that several riometers observed  
 219 absorption enhancements in association with the enhanced solar X-ray flux. Finally, we  
 220 choose events showing an absorption peak of at least 0.5 dB and at least 0.2 dB greater  
 221 than the minimum absorption during the flare interval. Each solar flare event affects 4-  
 222 5 riometers on average, and 640 individual riometer absorption events were collectively  
 223 observed, in total.

224 Figure 4 presents a correlation analysis of the  $\bar{\delta}$  observed by riometers with  $\chi$ ,  $\phi$ ,  
 225 local time (LT), and  $I_{\infty}^{max}$  (panels a-d), while panel (e) shows a generalized linear  
 226 regression of  $\bar{\delta}$  versus these four factors. A separate analysis is presented for C, M, and  
 227 X class flares in the top, middle, and bottom rows, respectively. The correlation  
 228 coefficients are listed inside each panel. This analysis shows the typical range of  $\bar{\delta}$  is  
 229 the 60s-1500s, which is in contrast with a reported range of  $\delta^{VLF}$ , typically 5-10  
 230 minutes (Hayes et al., 2017; Palit et al., 2015). In the left-most column, it can be seen  
 231 that  $\bar{\delta}$  has a relatively higher positive correlation with  $\chi$  for C and M class flares and  
 232 shows almost no correlation for X-class flares. By contrast, the correlation of delta with  
 233 latitude shows  $\bar{\delta}$  shows almost no correlation for C-class flares, and correlation  
 234 increases with flare class, as presented in the second left column. Besides,  $\bar{\delta}$  does not  
 235 show any linear dependence on local time as shown in the middle column,  $\bar{\delta}$  does not  
 236 have a linear dependence on LT for C, M, and X class flares. Sluggishness  $\bar{\delta}$  shows  
 237 negative correlations with  $I_{\infty}$ , with the highest correlation coefficient for M-class flares  
 238 as shown in the second right column. Note that for C-class flares shows no correlation  
 239 with  $I_{\infty}$ . Finally, the generalized linear regression of  $\bar{\delta}$  versus the four factors, shown  
 240 in the rightmost column. The models do a reasonably good job reproducing measured  
 241  $\bar{\delta}$  (i.e., the correlation coefficient is high).

### 242 3.3 Hard X-ray Waveband as Reference

243 Ever since Appleton first developed the theory of ionospheric sluggishness most  
 244 of the observational VLF studies have considered the peak of solar SRX irradiance as  
 245 the reference time for estimating sluggishness (Ellison, 1953; Kvirivský, 1962; Palit et  
 246 al., 2015), under the assumption that solar SRX irradiance is the best proxy for the  
 247 photoionization. However, photoionization at different altitudes is regulated by solar  
 248 irradiance wavebands, which peak at different times during a solar flare (Huang et al.,  
 249 2014). Consequently, the reference time should vary with ionospheric heights, which  
 250 creates ambiguity when estimating sluggishness from height integrated ionospheric  
 251 response considering SXR data as the only reference.

252 Figure 5 presents one example of the issue described in the previous paragraph.  
 253 Panels (a) and (b) present sluggishness estimated using conventional and peak time  
 254 derivative methods from Ottawa riometer measurements during a solar flare event on  
 255 11 March 2015, considering SXR irradiance (in red) and HXR irradiance (in black) as  
 256 a reference, respectively. Black dots represent observations from the Ottawa riometer.  
 257 The estimated sluggishness using conventional and peak time derivative methods  
 258 considering SXR irradiance as the reference is  $\bar{\delta} = 46\text{s}$  and  $\bar{\delta}_s = 139\text{s}$ , respectively. In  
 259 contrast, using HRX irradiance as reference the corresponding estimates for  
 260 sluggishness are  $\bar{\delta} = 91\text{s}$  and  $\bar{\delta}_s = 151\text{s}$ . There is thus a substantial difference in  
 261 sluggishness estimation using HXR as a reference over SXR.

### 262 3.4 Theoretical Study: Effective Recombination Coefficient, $\alpha_{eff}$

263 The focus of this section is to examine how chemical processes in the D region  
 264 may play a role in regulating ionospheric sluggishness and estimate  $\alpha_{eff}$  from the  
 265 conventional sluggishness,  $\bar{\delta}$ , measured from riometer observations. There are a  
 266 plethora of chemistry models exist that describe D region dynamics in terms of  
 267 following constituents: electrons, positive ions, anions, and heavy positive ions or  
 268 cluster ions (Glukhov et al., 1992; McRae & Thomson, 2004; Mitra, 1974; Mitra &

269 Jain, 1963; Žigman et al., 2007). Glukhov-Pasko-Inan (GPI) is a widely recognized  
 270 model that describes chemistry in D region altitudes (Glukhov et al., 1992). In brief,  
 271 the GPI model describes the ionosphere as a mixture of four constituents: electrons ( $n_e$ ),  
 272 negative ions ( $n^-$ ), positive ions ( $n^+$ ), and heavy positive cluster ions ( $n_x^+$ ). Assuming  
 273 charge neutrality, the effective recombination coefficient is  
 274

$$\alpha_{eff} = \left[ \frac{\beta - \gamma\lambda}{n_e} + \alpha_d^c \frac{n_x^+}{n_e} + \alpha_d \right] = \alpha_{eff}^{n^-} + \alpha_{eff}^{n_x^+} + \alpha_{eff}^{n^+} \quad (6)$$

275  
 276 where:  $q$ ,  $\gamma$ ,  $\beta$ ,  $\alpha_d$ ,  $\alpha_d^c$ , and  $\lambda$  represent photoionization rate, electron detachment rate,  
 277 electron attachment rate, electron-ion dissociative coefficient, electron-cluster ion  
 278 dissociative coefficient, and negative ion to electron ratio, respectively. Note that the  
 279 GPI model uses relatively constant values of  $\alpha_d$  and  $\alpha_d^c$  for D region heights, however,  
 280  $\gamma$  and  $\beta$  are functions of electron temperature ( $T_e$ ) (Glukhov et al., 1992; Lehtinen &  
 281 Inan, 2007). The effective recombination coefficient,  $\alpha_{eff}$ , depends on negative ion  
 282 chemistry (first term,  $\alpha_{eff}^{n^-}$ ), positive cluster ion chemistry (second term,  $\alpha_{eff}^{n_x^+}$ ), and  
 283 dissociative recombination rates (third term,  $\alpha_{eff}^{n^+}$ ), with typical ranges of values  $10^{-11}$   
 284  $- 10^{-12} \text{ m}^3\text{s}^{-1}$ ,  $10^{-11} - 10^{-12} \text{ m}^3\text{s}^{-1}$ , and  $3 \times 10^{-13} - 10^{-13} \text{ m}^3\text{s}^{-1}$ , respectively  
 285 (Ananthkrishnan et al., 1973; Schunk & Nagy, 2009). Alternatively, a study by  
 286 Žigman (2007) showed that  $\alpha_{eff}$  can be estimated from measured  $\delta$ , peak electron  
 287 density, and irradiance flux as:  
 288

$$\alpha_{eff} = \frac{3}{8\delta \left( n_e^{max} - \frac{I_{\infty}^{max} \delta g m_{avg}}{\rho e k T} \cos \chi \right)} \quad (7)$$

289  
 290 where:  $e$  is the base of the natural logarithm,  $k$  is the Boltzmann constant,  $g$  is the  
 291 gravitational acceleration,  $m_{avg} = 4.8 \times 10^{-26} \text{ kg}$  is the mean molecular mass (Mitra,  
 292 1992),  $\rho = 34 \text{ eV}$  is the average energy required to produce one electron-ion pair  
 293 (Whitten et al., 1965), and  $T \sim 210 \text{ K}$  is the averaged electron temperature of the D  
 294 region (Schmitter, 2011; Sharma et al., 2004).

295 We used equation (7) with simplified D region assumptions<sup>1</sup> to estimate  $\alpha_{eff}$   
 296 from sluggishness measured from riometer observations using the conventional method,  
 297  $\bar{\delta}$ . Figure 6 presents the results of using this approach. Specifically, panel (a) shows  
 298 estimated peak electron density at 74.1km heights and for  $\chi \sim 60^\circ - 80^\circ$  following  
 299 Žigman et al. (2007) (in red),  $\bar{\delta}$  from riometer measurement for  $\chi \sim 60^\circ - 80^\circ$  (in blue  
 300 dots), and fitted  $\bar{\delta}$  (in the blue curve). Panel (b) shows variations in estimated  $\alpha_{eff}$  from  
 301 equation (7), with peak solar flux intensity. Regions shaded in blue, green, and red show  
 302 typical ranges of  $\alpha_{eff}^{n^-}$ ,  $\alpha_{eff}^{n_x^+}$ , and  $\alpha_{eff}^{n^+}$ , respectively (Glukhov et al., 1992). Note for C  
 303 class flares  $\alpha_{eff}$  remains almost constant and within the negative and cluster ion  
 304 chemistry region shaded blue. However, with increasing peak solar irradiance  $\alpha_{eff}$   
 305 decreases, and the value drops below  $10^{-14} \text{ m}^3\text{s}^{-1}$ . The slope of the line is  $m =$

<sup>1</sup> Assumptions: i. D region is one thin layer; ii. all sluggishness in riometer measurements  $\bar{\delta}$  coming from the D region, this implies  $\bar{\delta} \approx \delta$  and  $\bar{\alpha}_{eff} \approx \alpha_{eff}$ ; iii.  $n_e^{max}$  is taken from Žigman (2007) considering D region is one thin layer concentrated around  $h \sim 74.1 \text{ km}$  and  $\chi > 50^\circ$ .

306  $-7.72 \times 10^{-2} \text{ m}^3\text{s}^{-1}/10 \text{ Wm}^{-2}$ . One explanation for this drop-in D region  $\alpha_{eff}$  could be  
 307 an increase in D region electron density and a decrease in electron photo-detachment  
 308 rate under the influence of the increased solar irradiance.

## 309 4. Discussion

310 In this study, we have defined two new methods to estimate ionospheric  
 311 sluggishness  $\bar{\delta}_s$  and  $\bar{\delta}_c$  using maximum slope and correlation analysis. In addition, we  
 312 compared estimates of ionospheric sluggishness using both passive and active high  
 313 frequency (HF, 3-30 MHz) instruments, namely riometers and SuperDARN HF radars,  
 314 respectively. Furthermore, we did a comprehensive characterization of  $\bar{\delta}$  using  
 315 riometers following 92 C, 63 M, and 18 X-class flares that occurred between 2006 and  
 316 2017 (Figure 4). We have also presented a comparison between the sluggishness  
 317 estimated, considering SXR and HXR (Figure 5). Finally, we used theoretical  
 318 arguments to estimate  $\alpha_{eff}$  from measured  $\bar{\delta}$  and gain some insights into the D region  
 319 chemistry (Figure 6). In this section, we summarize the findings and discuss how they  
 320 inform our understanding of the physical processes that control ionospheric  
 321 sluggishness.

322 As noted previously, sluggishness is an inertial property of the ionosphere (Basak  
 323 & Chakrabarti, 2013; Ellison, 1953). Early studies claimed that sluggishness is related  
 324 to recombination processes and inversely proportional to the product of electron density  
 325 and  $\alpha_{eff}$ , where  $\alpha_{eff}$  is relatively constant for a particular latitude, local time and  
 326 height. If this were the case, sluggishness would only be a function of electron density  
 327 (Palit et al., 2015). However, in this study, we found the measured sluggishness varies  
 328 significantly with the measuring techniques (see Figures 1 and 2), and we also found  
 329 the estimation of sluggishness using the peak time derivative (equation 3) is greater  
 330 than that using the conventional definition (equation 2). The probable reason might be  
 331 larger electron density during the peak of solar flare event than before the peak. This  
 332 implies that ionospheric sluggishness is indeed inversely proportional to electron  
 333 density but does not confirm that  $\alpha_{eff}$  is a constant. Furthermore, this explanation does  
 334 not fit the reasoning for the smaller values of sluggishness from SuperDARN HF radar  
 335 observations using the modified definition (refer Figure 3). The most likely explanation  
 336 is the difference in the ionospheric sounding techniques between the instruments. For  
 337 example, SuperDARN rays traverse the D region four times and at a lower operating  
 338 frequency, hence, they are more sensitive to the D region perturbations. Taking all these  
 339 factors together we can conclude that the choice of ionospheric sounding technique  
 340 impacts the sluggishness measurement. What matters then, are the relative differences  
 341 in sluggishness measured by a single instrument under different conditions.

342 The choice of solar irradiance also impacts the sluggishness estimation, as  
 343 presented in Figure 5. Historically, SXR has been used as reference data to estimate  
 344 sluggishness (e.g., Palit et al., 2015), the assumption being that SXR characterizes the  
 345 intensity of ionizing radiation at D region altitudes. However, HXR also produces a  
 346 significant amount of ionization at the lower D region heights, and photoionization at  
 347 different heights is regulated by different solar irradiance wavebands that peak at  
 348 different times during solar flares (Huang et al., 2014). Moreover, because riometer  
 349 observations provide a height integrated measurement of HF absorption, it is difficult  
 350 to know the exact relationship of sluggishness estimates to ionospheric parameters  
 351 without the help of modeling efforts. Hence, the question arises, which reference  
 352 waveband should we use to extract sluggishness from the riometer measurements? We

353 suggest referring to the ionizing solar radiation wavebands that have an optical depth  
 354 associated with the altitude that is equal to the altitude of maximum HF absorption.

355 From the correlation analysis (Figure 4), we found that  $\bar{\delta}$  is positively associated  
 356 with increasing solar zenith angle and decreasing solar SXR intensity, which is  
 357 consistent with previous VLF studies (Basak & Chakrabarti, 2013; Palit et al., 2015).  
 358 These results are consistent with the physics described by Appleton (1953), namely that  
 359 an increase in solar zenith angle produces a decrease in photoionization and electron  
 360 density, which leads to an increase in ionospheric sluggishness. Naively, one might  
 361 expect sluggishness to also decrease with latitude for similar reasons; however, panels  
 362 b-1~3 show a high correlation of  $\bar{\delta}$  with latitude, but only for M and X class flares.  
 363 One possible explanation for this mixed latitude dependence is variability in  
 364  $\alpha_{eff}$  which is known to have a strong dependence on anionic chemistry at higher  
 365 latitudes (Amemiya & Nakamura, 1996; Mitra, 1974). Further detailed analysis and  
 366 modeling of sluggishness across latitudes and local time may provide further insights  
 367 into the variability of D region chemistry. Future work will also examine the statistical  
 368 behavior of  $\bar{\delta}_c$  and  $\bar{\delta}_s$  measured from riometer and SuperDARN observations.

369 Another focus of this study has been to estimate  $\alpha_{eff}$  from  $\bar{\delta}$  measured using  
 370 riometer measurements. Equation (6) describes the effective recombination coefficient  
 371 in terms of negative ion formation and destruction (first term  $\alpha_{eff}^{n^-}$ ), dissociative  
 372 electron-cluster ion recombination (second term  $\alpha_{eff}^{n_x^+}$ ), and dissociative electron-ion  
 373 recombination (third term  $\alpha_{eff}^{n^+}$ ) (Glukhov et al., 1992; Schunk & Nagy, 2009; Žigman  
 374 et al., 2007). We have shown the effective ionospheric recombination coefficient ( $\alpha_{eff}$ )  
 375 varies by several orders of magnitude (typically between  $10^{-11} - 10^{-14} \text{ m}^3\text{s}^{-1}$ ) with peak  
 376 solar SXR irradiance (Figure 6). The range of values for  $\alpha_{eff}$  is consistent with those  
 377 found in previous literature (García-Rigo et al., 2007; Gledhill, 1986; Schunk & Nagy,  
 378 2009). We conclude that reductions in estimated  $\alpha_{eff}$  are mainly due to drops in the  
 379 negative and positive cluster ion effective recombination coefficients denoted by  $\alpha_{eff}^{n^-}$   
 380 and  $\alpha_{eff}^{n_x^+}$ , respectively. Specifically, decreases in  $\alpha_{eff}$  are caused by enhancements in  
 381 electron density ( $n_e$ ) due to photoionization and to enhancements in electron  
 382 detachment rate ( $\gamma$ ) due to the sudden rise of molecular vibrational and rotational  
 383 energy under the influence of energetic EM radiation (Verronen et al., 2006). Taken  
 384 all together, we conclude that intense solar flares alter the negative and positive ion  
 385 chemistry at the D-region altitudes. Recent studies have suggested that an increase in  
 386 flare time D-region electron temperature that changes the electron-ion dissociative  
 387 coefficient ( $\alpha_d$ ) can lead to an overall drop in the effective recombination coefficient  
 388 (see Figure 5 in Nina et al., 2012; Bajcetic et al., 2015). More detailed data analysis and  
 389 modeling efforts are required to fully understand D-region negative ion and positive  
 390 cluster ion chemistry during solar flares and how it is affected by changes in D-region  
 391 electron temperature.

## 392 5. Conclusion

393 In this study, we have compared estimates of ionospheric sluggishness obtained  
 394 from riometer and SuperDARN HF radar observations using three different  
 395 methodologies. A correlation analysis was conducted on the sluggishness estimated  
 396 from riometer observations using a conventional method. We performed a simulation  
 397 study to estimate the effective recombination coefficient ( $\alpha_{eff}$ ) and to examine its

398 variations with peak solar soft X-ray flux. We found that the choice of ionospheric  
399 sounding techniques and reference solar irradiance wavebands affects the estimation of  
400 sluggishness. We also found that ionospheric sluggishness is anti-correlated with solar  
401 EUV radiation intensity, as expected. We showed that the effective recombination  
402 coefficient ( $\alpha_{eff}$ ) varies by several orders of magnitude, typically between  $10^{-11} - 10^{-14}$   
403  $\text{m}^3\text{s}^{-1}$ , with the flare time peak solar soft X-ray irradiance. The results suggest an  
404 increase in electron density and negative ion chemistry under the influence of EUV and  
405 X-ray flux is the major determinant of sluggishness. Future work will examine how  
406 sluggishness depends on latitudinal factors and complex-ion (negative and positive  
407 cluster ion) chemistry and geomagnetic activity.

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414 Calgary for providing riometer data directly via <http://data.phys.ucalgary.ca/>. We also  
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416 of SuperDARN data via <http://vt.superdarn.org/tiki-index.php?page=Data+Access>.  
417 The majority of analysis and visualization was completed with the help of free, open-  
418 source software tools such as matplotlib (Hunter, 2007), IPython (Perez & Granger,  
419 2007), pandas (McKinney, 2010), Spacepy (S. K. Morley et al., 2011), PyForecastTools  
420 (S. Morley & Burrell, 2020), and others (e.g., Millman & Aivazis, 2011).

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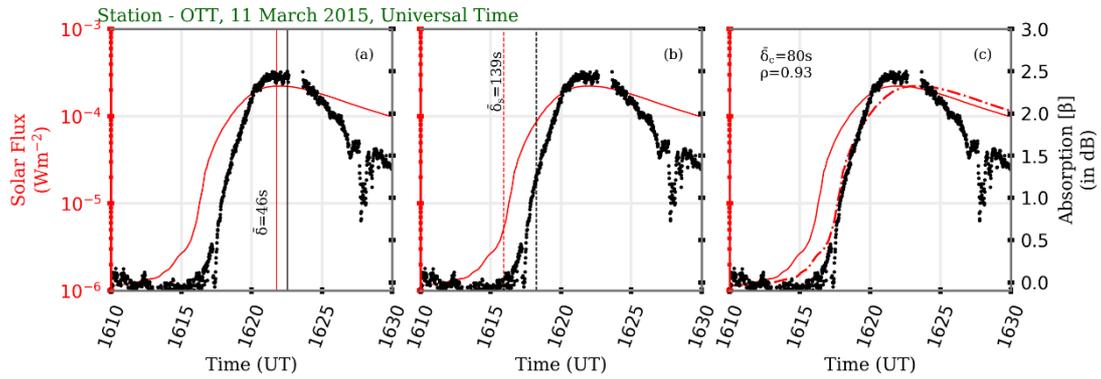
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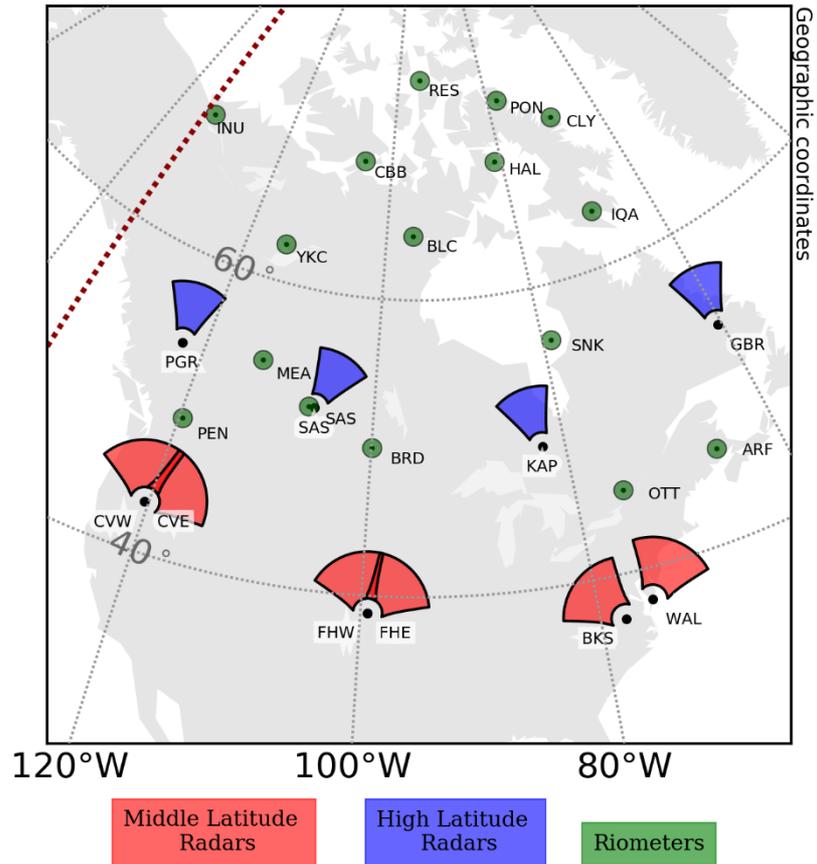
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580 **Figures & Captions**

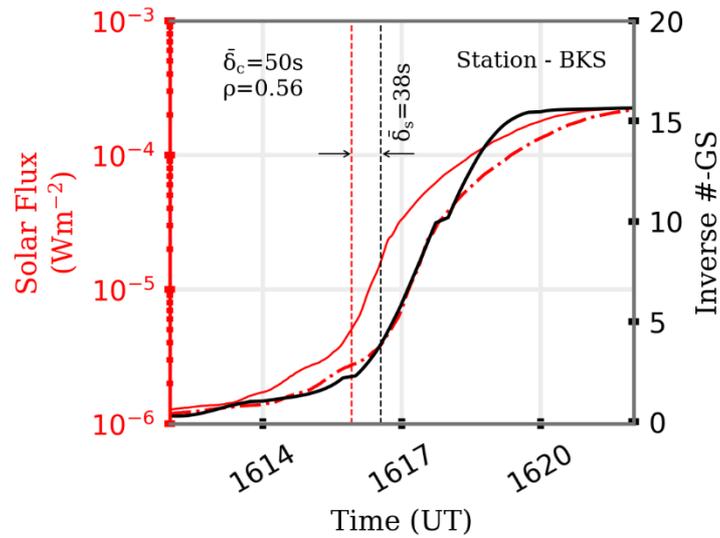


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 582 Figure 1. Ionospheric sluggishness in Ottawa (OTT) riometer measurement during a  
 583 solar flare event on 11 March 2015, estimated using (a) conventional, (b) peak time  
 584 derivative, and (c) correlation methods. Red and black colors represent SXR irradiance  
 585 from GOES and CNA observations from the riometer, respectively. The solid and  
 586 dashed vertical lines in panels (a) and (b) represent peaks and peak time derivative in  
 587 both datasets, respectively. The dashed red curve in panel (c) represents time delayed  
 588 GOES SXR irradiance data. Sluggishness values estimated using the three different  
 589 methods are provided inside each panel.



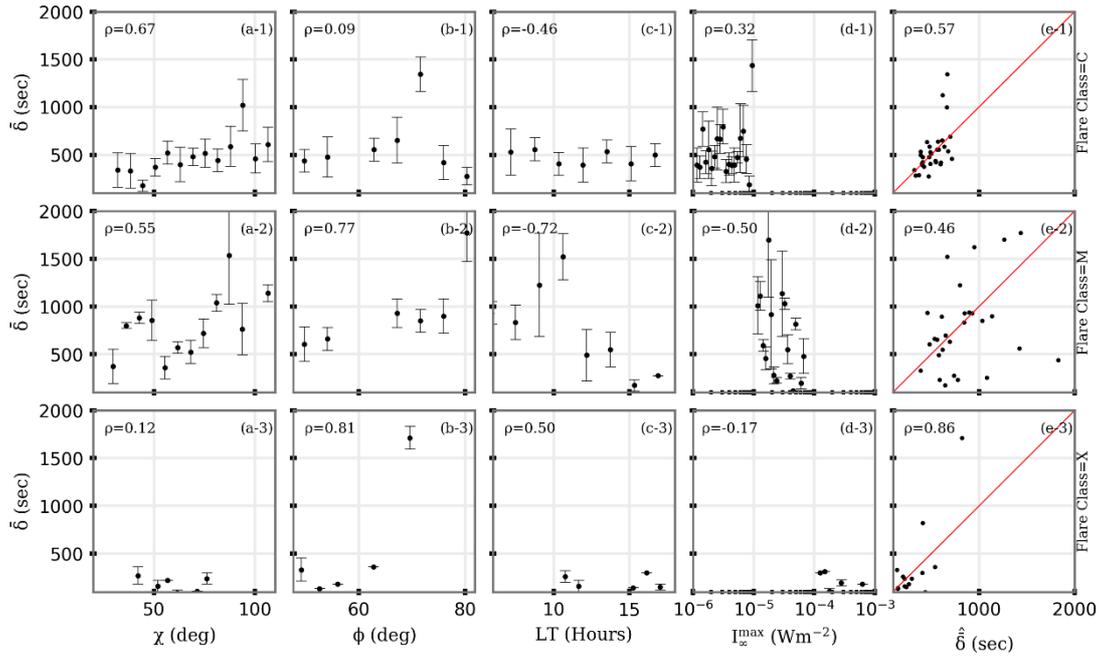
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Figure 2. Location of the various instruments used in the study. The red line at  $-135.3^\circ$  longitude indicates the longitudinal location of the GOES 15 satellite. Colors represent the fields-of-view of the middle (red) and high (blue) latitude SuperDARN radars and riometers (green).



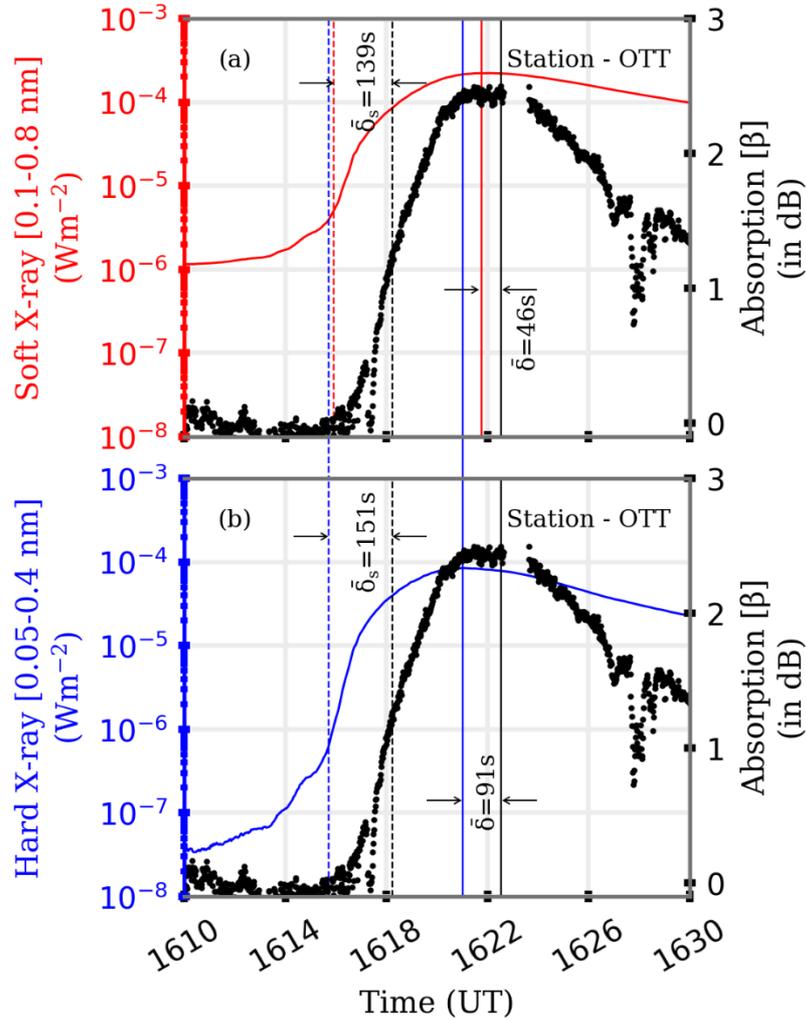
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596 Figure 3. Ionospheric sluggishness in SuperDARN Blackstone radar ground scatter  
 597 measurements estimated using peak time derivative and correlation methods during a  
 598 solar flare event on 11 March 2015. Red and black colors represent SXR irradiance  
 599 from GOES, and inverse ground scatter echoes from Blackstone SuperDARN radar,  
 600 respectively. The solid and dashed red curves represent actual and time-delayed SXR  
 601 irradiance, respectively. The dashed vertical lines represent peak time derivatives in  
 602 both the datasets. Sluggishness values estimated using peak time derivative, correlation  
 603 methods, and correlation coefficient are provided in the panel.

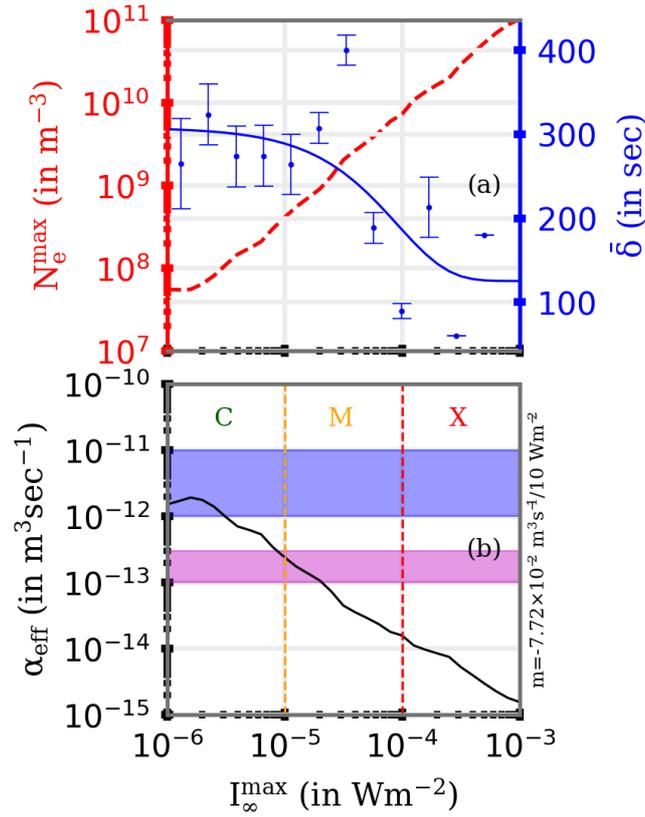


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Figure 4. Correlation analysis between sluggishness estimated using equation (2) ( $\bar{\delta}$ ) with (a-1~3) solar zenith angle ( $\chi$ ), (b-1~3) latitude ( $\phi$ ), (c-1~3) local time (LT), (d-1~3) peak flux ( $I_{\infty}$ ), respectively, and (e-1~3) generalized linear regression analysis of  $\bar{\delta}$  and the four factors under consideration. C, M, and X class flare analyses are shown in the top, middle, and bottom row, respectively. Associated correlation coefficients are provided inside each panel.



611  
 612 Figure 5. Sluggishness in Ottawa riometer measurement during a solar flare event on  
 613 11 March 2015, considering (a) SXR irradiance and (b) HXR irradiance observations  
 614 as reference. Red, blue, and black colors represent SXR, HXR irradiance from GOES,  
 615 and CNA observations from the riometer, respectively. The solid (dashed) red and black  
 616 lines represent the peak times (peak time derivatives) in GOES SRX irradiance and  
 617 riometer cosmic noise absorption, respectively. Sluggishness estimated using  
 618 conventional and peak time derivative methods are mentioned in panels.



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Figure 6. Model-data comparison of variations in (a) peak electron density at D region heights from Zigman et al. (2007) (in red) and  $\bar{\delta}$  from riometer measurement for  $\chi > 50^\circ$  (in blue dots), and (b)  $\bar{\alpha}_{\text{eff}}$  from equation (13), with peak solar flux intensity. Blue smoothed line in panel (a) is the averaged  $\bar{\delta}$ . Vertical orange and red lines in panel (b) represent the separation between C, M, and X class flares. The slope of the black curve (m) in panel (b) is provided along the right vertical axis of the panel.