

YORP Effect on Asteroid 162173 Ryugu: Implications for the Dynamical History

M. Kanamaru¹, S. Sasaki², T. Morota³, Y. Cho³, E. Tatsumi⁴, M. Hirabayashi⁵, N. Hirata⁶, H. Senshu⁷, Y. Shimaki¹, N. Sakatani⁸, S. Tanaka¹, T. Okada¹, T. Usui¹, S. Sugita³, S. Watanabe⁹.

¹Institute of Space and Astronautical Science (ISAS), Japan Aerospace Exploration Agency (JAXA),

3-3-1 Yoshinodai, Sagamihara 252-5210, Japan.

²Osaka University, 1-1 Machikaneyama, Toyonaka, Osaka 560-0043, Japan.

³The University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 1130033, Japan.

⁴Instituto de Astrofísica de Canarias, C/Vía Láctea, 38205 La Laguna - Tenerife - España.

⁵Auburn University, 211 Davis Hall, Auburn, AL 36849-5338, United States

⁶University of Aizu, Tsuruga, Ikkimachi, Aizu Wakamatsu, Fukushima 965-8580, Japan.

⁷Chiba Institute of Technology, 2-17-1 Tsudanuma, Narashino, Chiba 275-0016, Japan.

⁸Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima, Tokyo 171-8501, Japan.

⁹Nagoya University, Furo-cho, Chikusa-ku, Nagoya, Aichi 464-8601 Japan.

Key Points:

- 1 • Thermal recoil torque (i.e., the YORP effect) plays a dominant role in the spin-
2 down of asteroid 162173 Ryugu.
- 3 • The estimated spin-down time scale (0.58 – 8.7 million years) indicates a period
4 of major change in the topography of Ryugu.
- 5 • The YORP effect is responsible for keeping the spin-pole of Ryugu perpendicu-
6 lar to the orbital plane.

Corresponding author: Masanori Kanamaru, kanamaru.masanori@jaxa.jp

Abstract

7 Asteroid 162173 (Ryugu) is a carbonaceous asteroid that was visited by Japan’s Hayabusa2
 8 spacecraft in 2018. The formation mechanism of spinning-top shape of Ryugu is an essential
 9 clue to the dynamical history of the near-Earth asteroid. In this study, we address the long-
 10 term evolution of the spin state of Ryugu induced by the Yarkovsky–O’Keefe–Radzievskii–
 11 Paddack (YORP) effect, i.e., the thermal recoil torque that changes the rotation period and
 12 spin-pole direction.

13 Given the current orbit, spin state, and three-dimensional shape observed by Hayabusa2,
 14 we computed the YORP torque exerted on Ryugu using a simplified thermal model approx-
 15 imating zero thermal conductivity. Despite differences in meter-scaled topography, all 20
 16 shape models that we examined indicate that the spin velocity of Ryugu is currently de-
 17 creasing at a rate of $(-0.42 - -6.3) \times 10^{-6}$ deg/day². Our findings also suggest that the
 18 thermal torque on the asteroid is responsible for maintaining the spin pole upright with
 19 respect to the orbital plane.

20 Therefore, the YORP effect could explain the significant spin-down from a period of
 21 3.5 h initially to 7.6 h currently. The corresponding time scale of the rotational deceleration
 22 is estimated to be 0.58 – 8.7 million years, depending on the input shape models. This time
 23 scale is comparable to e.g., the formation period of the largest crater, *Urashima* (5 – 12
 24 Ma) or the western bulge (2 – 9 Ma) as derived from previous studies on crater statistics in
 25 Ryugu. It is considered that the rotation of the asteroid started to decelerate in the wake
 26 of the major crater formation or the resurfacing event on the western hemisphere.

Plain Language Summary

27 The Japanese spacecraft Hayabusa2 visited the kilometer-sized asteroid, Ryugu, and
 28 found it to have a spinning-top shape with a diamond-like cross section. For an aggregate
 29 of rock fragments to deform in this way, fast rotation is required. The rotation period of
 30 Ryugu is 7.6 h, and its rotational speed is not sufficiently fast to deform the entire body.
 31 It is proposed that Ryugu initially spun rapidly and has since slowed down. Light has no
 32 mass, but it does have momentum and produces a faint pressure. As the asteroid is heated
 33 from the Sun, radiation is emitted from the asteroid surface, resulting in a braking effect
 34 and changing the rotational speed of the asteroid over millions of years. We found that the

35 radiation pressure is a reasonable mechanism for the spin-down of the asteroid and thus
36 provides a clue to Ryugu's history.

1 Introduction

37 Japan’s Hayabusa2 was a sample return mission from the C-type near-Earth asteroid,
 38 162173 (1999 JU₃) Ryugu (Tachibana et al., 2014; Watanabe et al., 2017; Tsuda et al.,
 39 2019). The Hayabusa2 spacecraft arrived at the target asteroid in June 2018 and started its
 40 homeward journey to Earth in November 2019 after an approximately 17-month asteroid-
 41 proximity phase. The mission included two successful touchdowns to sample the surface ma-
 42 terial, an artificial cratering experiment, and deployment of a lander and rovers. Hayabusa2
 43 revealed the nature of the rocky surface and its spinning-top shape (Watanabe et al., 2019).
 44 The spinning-top-shaped body has an elevated ridge in the equatorial region and a flat cross
 45 section in the mid-latitude region, unlike spherical or ellipsoidal objects. Ryugu’s shape is
 46 considered to be the result of deformation induced by fast rotation in the past (Watanabe
 47 et al., 2019). According to finite-element-method analysis Hirabayashi et al. (2019), a fast
 48 rotation at a period of approximately 3.0 – 3.5 h is sufficient to induce interior structural
 49 failure or surface mass wasting due to centrifugal force. However, the spin-down process
 50 from the past rapid rotation to the current milder state (7.6 h period) remains unknown.
 51 The goal of this study is to explore the Yarkovsky–O’Keefe–Radzievskii–Paddack (YORP)
 52 effect on Ryugu, i.e., thermally induced spin alteration (Rubincam, 2000), which is one
 53 of the greatest contributors to the spin dynamics of the asteroid. We propose a new ap-
 54 proach to reveal its evolutionary history by combining a dynamical simulation and analyses
 55 of geologic features. The dynamical process sensitive to a topographic change enables us to
 56 integrate the two perspectives.

1.1 Asteroid Ryugu revealed by Hayabusa2

57 We present a brief review of the scientific achievements of Hayabusa2 at the time of
 58 writing. Watanabe et al. (2019) is a flagship report on the first impression of Ryugu,
 59 including the spinning-top shape as mentioned above. The spinning-top shape and rocky
 60 surface strongly suggested that Ryugu is a rubble pile formed by the catastrophic disruption
 61 of a parent body and reaccumulation of the fragments. For our later simulations, we utilized
 62 the orbital elements, rotation period, spin-pole orientation, and other physical properties
 63 of Ryugu reported in this study (see Table 1). Ryugu is a retrograde rotator with a pole
 64 almost perpendicular to its orbital plane, for which the obliquity ε (i.e., tilt angle of the
 65 spin axis with respect to the normal vector of a body’s orbital plane) corresponds to 171.6°.

Table 1. Properties of asteroid 162173 Ryugu in the J2000.0 frame at the epoch of 2018 July 1.0 TDB (See the supplementary material of Watanabe et al. (2019)).

Parameters	Notation	Value	Unit
Orbital elements			
Semi-major axis	a	1.190	AU
Eccentricity	e	0.1903	–
Inclination	I	5.884	deg
Longitude of ascending node	Ω	251.6	deg
Argument of perihelion	ω	211.4	deg
Mean anomaly	Φ	21.94	deg
Rotation pole and period			
Right ascension (RA)	α	96.40	deg
Declination (Dec)	δ	–66.40	deg
Ecliptic longitude	λ	179.3	deg
Ecliptic latitude	β	–87.44	deg
Obliquity	ε	171.6	deg
Rotation period	P	7.633	h
Physical properties			
GM	GM	30.0	m ³ /s ²
Mass	M	4.50×10^{11}	kg
Volume	V	0.377 ± 0.005	km ³
Mean density	ρ	$1,190 \pm 20$	kg/m ³

66 Three-dimensional (3D) shape models of Ryugu were constructed from images captured
67 by the onboard optical navigation camera (ONC) and have been updated until the time of
68 writing. In the Hayabusa2 project, two different methods are used for 3D shape reconstruc-
69 tion: stereo-photoclinometry (SPC) (R. Gaskell et al., 2006; R. W. Gaskell et al., 2008) and
70 structure-from-motion (SfM) (Szeliski, 2011). Ryugu’s volume, as derived from the shape
71 model and mass from spacecraft tracking data during a descent operation onto the asteroid,
72 yielded a bulk density of $1190 \pm 20 \text{ kg/m}^3$ (Watanabe et al., 2019). The average reflectance
73 spectrum of Ryugu is very flat from visible to near-infrared wavelengths, and its geometric
74 albedo is very low, i.e., $4.0 \pm 0.5\%$ at the $0.55 \mu\text{m}$ band (Tatsumi et al., 2020). The re-
75 flectance spectrum can be classified as Cb-type in the Bus and Binzel taxonomy (Sugita et
76 al., 2019) and C/F-type in the Tholen taxonomy (Tatsumi et al., 2020). A weak but sharp
77 absorption feature at $2.72 \mu\text{m}$ was detected across the entire surface. These features suggest
78 that, similar to the heated Ivuna meteorite, Ryugu is composed of CM- or CI-like materials
79 (Kitazato et al., 2019). Because the bulk density of Ryugu is smaller than that of many
80 types of carbonaceous chondrites, the porosity of Ryugu could exceed 50% (Watanabe et
81 al., 2019).

82 Global ONC observations of Ryugu revealed many of its geologic properties, including
83 an east-west dichotomy, an equatorial ridge, numerous impact craters, and a high abundance
84 of large boulders (Sugita et al., 2019). Closer examinations of surface features on Ryugu
85 show evidence of mass motion from the equatorial ridges toward mid-latitude regions, such
86 as imbricated boulders and regolith run-ups on the ridge sides of boulders. Such direction of
87 mass motion is consistent with geopotential changes due to the spin deceleration of Ryugu;
88 a decrease in centrifugal force increases the geopotential of the equatorial ridge and lowers
89 that of mid-latitude regions (Sugita et al., 2019; Morota et al., 2020). Global mapping
90 also revealed that the surface of Ryugu exhibits distinctive latitudinal color variation that
91 supports the deceleration-induced mass motion. The most prominent color variation in
92 visible wavelengths is observed in the spectral slope between the b- and x-bands ($0.48\text{--}0.86$
93 μm) (Sugita et al., 2019; Tatsumi et al., 2020). The variation in the b–x spectral slope
94 is correlated with the geopotential (or elevation measured from an equipotential surface).
95 Areas of high potential, such as the polar and equatorial regions, tend to have smaller
96 or negative b-x slopes (i.e., bluer spectra). In contrast, the mid-latitude areas of Ryugu
97 have positive b-x slopes (i.e., redder spectra). This color variation suggests that materials
98 weathered on the surface migrate from highlands to lowlands in response to the current shape

99 and gravity field of Ryugu; this is likely caused by the most recent major mass motion on
100 Ryugu (Sugita et al., 2019). Thus, both morphological and spectral surface features on
101 Ryugu support the recent deceleration in spin rate.

102 Further, crater statistics can serve as indicators for the surface age of a solid objects and
103 the mechanical properties of the surface layer. Hirata et al. (2020) provided a comprehensive
104 list of impact craters larger than 20 m on Ryugu and discussed their spatial distribution.
105 More detailed morphological studies of the craters are reported in Noguchi et al. (2021). A
106 statistical randomness analysis by Hirata et al. (2020) confirmed that those craters are con-
107 centrated in the equatorial region (30°S–30°N) rather than follow a random distribution.
108 Moreover, the number density of the craters varies longitudinally. The so-called western
109 bulge (160°E–290°E) has fewer craters than regions around the prime meridian of Ryugu
110 (300°E – 30°E). Additionally, Michikami et al. (2019) reported a difference in boulder abun-
111 dance (> 5 m) between the eastern and western hemispheres. In fact, the number density
112 of the boulders is relatively lower in the western hemisphere. The origin of the western
113 bulge is proposed to be a past deformation process of Ryugu during a period of fast ro-
114 tation (Hirabayashi et al., 2019) or regolith landslides toward the western side at a rapid
115 spin (Scheeres, 2015). These processes could resurface in the western hemisphere of Ryugu
116 and result in an east–west dichotomy in the crater and boulder densities. Ryugu’s craters
117 were also found to possess morphological features, such as raised rims and wall slumping,
118 consistent with unconsolidated surface materials. Based on this observation, Sugita et al.
119 (2019) estimated the residence time of Ryugu in the main asteroid belt since the formation
120 of the current topography to be 8.9 ± 2.5 Ma using the gravity scaling rule for coarse-grain
121 targets (Tatsumi & Sugita, 2018). The use of gravity-scaling was subsequently validated by
122 the artificial impact experiment conducted by Hayabusa2 (Arakawa et al., 2020).

123 Based on detailed crater observations using close-up images, Morota et al. (2020) found
124 that Ryugu experienced orbital excursion toward the Sun after leaving a stable orbit in
125 the main belt. This sunward orbital excursion likely reddened the surface layer (≤ 1 m)
126 through solar heating and/or solar wind irradiation. Crater counting indicates that the
127 surface reddening event was terminated at 0.3 to 8.1 Ma. Because the erosion of the red
128 surface layer through the despinning-induced mass motion postdates the reddening event,
129 it can be deduced that the rotational deceleration of Ryugu has likely occurred in the last
130 0.3 – 8.1 Ma.

1.2 Observational and theoretical studies on YORP

131 Spin parameters of asteroids have been actively investigated through light curve and
 132 radar observation. However, to detect a secular change in the rotation period, multiple
 133 observation sessions over several years are required. The YORP effect was initially detected
 134 by the increase in the spin velocity of asteroid 54509 YORP (2000 PH5) (Lowry et al.,
 135 2007; Taylor et al., 2007). Since then, YORP-induced spin-up has been observed in several
 136 sub-kilometer-sized asteroids: 1862 Apollo (Kaasalainen et al., 2007; Āurech, Vokrouhlický,
 137 Kaasalainen, Weissman, et al., 2008), 1620 Geographos (Āurech, Vokrouhlický, Kaasalainen,
 138 Higgins, et al., 2008), 3103 Eger (Āurech et al., 2012, 2018), 25143 Itokawa (Lowry et al.,
 139 2014), 1685 Toro (Āurech et al., 2018), and 161989 Cacus (Āurech et al., 2018). Most
 140 recently, asteroid 101955 Bennu was observed to be spinning up at a rate of $(3.63 \pm 0.52) \times$
 141 10^{-6} deg/day² by ground-based observations and NASA’s OSIRIS-REx spacecraft (Nolan
 142 et al., 2019; Hergenrother et al., 2019). Although the rotation period of asteroid 162173
 143 Ryugu was monitored during the proximity phase of Hayabusa2, no significant change in
 144 period was confirmed. To compare the results of observations and numerical simulations in
 145 terms of the YORP effect on Ryugu, we have to wait for the next opportunity of light curve
 146 acquisition.

147 Since the YORP modeling by Rubincam (2000), many numerical studies based on three-
 148 dimensional shapes of real asteroids have been performed. The computational models of the
 149 YORP effect have been developed to incorporate non-zero thermal conductivity (Āapek &
 150 Vokrouhlický, 2004) and projected shadows (Vokrouhlický & Āapek, 2002). The advanced
 151 thermophysical model (ATPM) proposed by Rozitis and Green (2011, 2012) completely
 152 implemented both the reabsorption of thermal emission due to uneven terrain and the
 153 surface roughness effect to deflect radiation in the direction of the Sun. Moreover, it has
 154 been found that lateral heat conduction is likely to significantly impact the thermal torque
 155 (Golubov et al., 2014; Ševeček et al., 2016), which has been neglected in most YORP models
 156 that solve the one-dimensional heat conduction problem. However, an all-in-one simulation
 157 method is computationally costly and difficult to apply to highly accurate shape models
 158 acquired by spacecrafts.

159 In this study, we aim to demonstrate the YORP-induced spin evolution of Ryugu
 160 and compare its time scale with the surface age of the asteroid. Although a simplified
 161 computational model is used herein (Section 2), we compared various types of Ryugu’s

162 shape models (Section 3) to overcome the inherent problem of numerical YORP modeling,
163 in which the net torque is highly dependent on input shape models (Statler, 2009). In
164 Section 4, we evaluate the model sensitivity to shape and compare our numerical model
165 with another thermophysical model. In Section 5, we associate the spin alteration of Ryugu
166 with geological events that have occurred on the asteroid.

Table 2. Notation in this paper.

Symbol	Description
A	Geometric albedo
s_i	Shadowing factor of the i th surface element (1 for shadow or 0 for insolation)
Φ	Solar irradiation per unit area on a body's orbit
$\hat{\mathbf{n}}_i$	Normal vector to the i th surface element
$\hat{\mathbf{r}}_{sun}$	Direction of the Sun
ϵ	Emissivity of the body's surface
σ	Stefan-Boltzmann constant
T_i	Temperature of the i th surface element
K	Thermal conductivity of the material
$d\mathbf{f}_i$	Thermally induced force on the i th element
c	Speed of light
dS_i	Area of the i th element
$\boldsymbol{\tau}$	YORP torque on the body
\mathbf{r}_i	Centroid position of the i th element
N_S	Number of surface elements
\mathbf{L}	Angular momentum of rotation
C	Moment of inertia around the shortest axis
ω	Angular velocity of rotation
$\hat{\mathbf{s}}$	Direction of the spin pole
ϵ	Obliquity of the spin pole
ψ	Longitude of precession

2 Method of YORP Simulation

167 To calculate the thermally induced torque on an asteroid, we need to evaluate the
168 surface temperature or radiation energy flux of the body's surface based on its orbit, spin
169 state, and irregular shape. Subsequently, we simply have to integrate the equation of motion
170 for the asteroid's rotation. All symbols used in this section are listed in Table 2.

2.1 Thermal model

171 We begin with the energy conservation law at each surface element of a small body's
 172 shape. The following equation presents the balance between the incident energy from sun-
 173 light (left-hand side) and the sum of energy derived from thermal re-radiation from the
 174 surface element and heat conduction into the ground (right-hand side).

$$175 \quad (1 - A)(1 - s_i)\Phi(\hat{\mathbf{n}}_i \cdot \hat{\mathbf{r}}_{sun}) = \epsilon\sigma T_i^4 + K\hat{\mathbf{n}}_i \cdot \nabla T_i \quad (1)$$

176 In this study, we calculated the energy flux $\Phi(t)$ in each time step based on the Kepler
 177 motion of the asteroid around the Sun.

$$178 \quad \Phi(t) = \Phi_{\text{Earth}} \left(\frac{r_{\text{Earth}}}{r_{\text{body}}(t)} \right)^2 \quad (2)$$

179 The solar irradiation at the Earth's orbit $r_{\text{Earth}} = 1$ AU is called the solar constant Φ_{Earth} ,
 180 and it is inversely proportional to the square of the body's distance from the Sun. It greatly
 181 influences the strength or time scale of the YORP effect depending on the orbital semi-major
 182 axis. For example, there is a difference in the energy flux by a factor of approximately six
 183 between the near-Earth orbit (~ 1 AU) and inner main belt (~ 2.5 AU). Asteroid Ryugu
 184 exhibits seasonal variation in solar irradiation by a few times because of its eccentric orbit.
 185 We used 1366.0 W/m² for the solar constant in our simulations.

186 The left-hand side of Equation 1 expresses the amount of solar energy absorbed by the
 187 i th surface element of the shape model. Therefore, the factor $(\hat{\mathbf{n}}_i \cdot \hat{\mathbf{r}}_{sun})$ decreases the solar
 188 irradiation per unit area depending on the tilt of the element. On the night-side of the body,
 189 this factor becomes negative, and solar irradiation is supposedly turned off. In addition, we
 190 implemented a ray-trace algorithm to check whether each element is illuminated or not at
 191 a certain time, as implemented in, e.g., Breiter et al. (2009) and Rozitis and Green (2012).
 192 The shadowing factor, s_i , returns an integer of 1 or 0, depending on whether solar rays
 193 towards the i th element are blocked by other elements or not, respectively. To reduce the
 194 computation time, we sometimes ignore the shadowing effect in our later simulations and
 195 perform the so-called ‘‘pseudo-convex’’ model, originally implemented in Rubincam (2000).

196 The right-hand side of Equation 1 represents the energy released from each surface
 197 element, which includes the thermal radiation and heat flux of the body's interior. Some
 198 authors implemented one-dimensional thermophysical modeling to evaluate the surface tem-
 199 perature (e.g., Čapek & Vokrouhlický, 2004). This study simplified the computation of ther-
 200 mal radiation using the Rubincam (2000) approximation Rubincam (2000), which assumed

201 (1) zero-conductivity and (2) Lambert radiation from each surface element. According to
 202 assumption (1), we can neglect the conduction term in Equation 1 as follows:

$$203 \quad (1 - A)(1 - s_i)\Phi(\hat{\mathbf{n}}_i \cdot \hat{\mathbf{r}}_{sun}) \approx \epsilon\sigma T_i^4 \quad (3)$$

204 This equation holds that the incident energy from sunlight is immediately emitted from
 205 the surface with no time lag. The second assumes that each surface element isotropically
 206 radiates energy, with the same intensity of infrared radiation observed from any angle. The
 207 Lambert radiation assumption results in a simple formula for the force exerted on each
 208 surface element (Rubincam, 2000; Vokrouhlický & Čapek, 2002):

$$209 \quad d\mathbf{f}_i = -\frac{2}{3} \frac{\epsilon\sigma T^4}{c} \hat{\mathbf{n}}_i dS_i \quad (4)$$

$$210 \quad = -\frac{2\Phi}{3c} (1 - s_i)(\hat{\mathbf{n}}_i \cdot \hat{\mathbf{r}}_{sun}) \hat{\mathbf{n}}_i dS_i \quad (5)$$

212 The thermal “kick-back” force, $d\mathbf{f}_i$, is directed opposite of the facet normal, $\hat{\mathbf{n}}_i$, and its
 213 magnitude is proportional to the area of the element dS_i . The thermal radiation, $\epsilon\sigma T^4$,
 214 can be replaced by the incident energy based on the assumption in Equation 3. We convert
 215 the factor $(1 - A)$ to 1 to combine the effects of scattering on the surface. If the scattered
 216 light reflects isotropically, like thermal radiation, we can add its contribution to the factor
 217 $(1 - A)$.

218 We can then compute the net torque, $\boldsymbol{\tau}$, of the YORP effect by integrating the above
 219 force over the entire surface of the asteroid. Given a polyhedral shape model covered with
 220 N_S triangular meshes, one simply has to sum the torque on every surface element as a cross
 221 product of the element’s position, \mathbf{r}_i , and thermal kick-back, $d\mathbf{f}_i$, as follows:

$$222 \quad \boldsymbol{\tau} = \int_S \mathbf{r} \times d\mathbf{f} = \sum_{i=1}^{N_S} \mathbf{r}_i \times d\mathbf{f}_i \quad (6)$$

2.2 Equation of motion

223 Given uniform rotation around the shortest axis, the angular momentum \mathbf{L} of a spinning
 224 body is simply expressed as follows:

$$225 \quad \mathbf{L} = C\omega\hat{\mathbf{s}} \quad (7)$$

226 Here, the direction of \mathbf{L} always matches that of the spin pole $\hat{\mathbf{s}}$ by neglecting small com-
 227 ponents of the angular velocity about the other axes. Contrarily to a typical YORP time
 228 scale (\sim millions of years), the rotation pole is considered to be quickly relaxed to the short-
 229 est axis by energy dissipation associated with inelastic distortion (Efroimsky, 2001; Mysen,

230 2006). The YORP-induced torque, $\boldsymbol{\tau}$, in Equation 6 changes the angular momentum of the
 231 asteroid, and the equation of motion is expressed as follows:

$$232 \quad \frac{d\mathbf{L}}{dt} = \boldsymbol{\tau} \quad (8)$$

233 Some authors decompose the above equation into three essential parameters to describe
 234 the spin state of the body. According to the expression given by Bottke et al. (2006), the
 235 equation of motion is expressed by time derivatives of angular velocity ω , obliquity ε , and
 236 longitude of precession ψ :

$$237 \quad \frac{d\omega}{dt} = \frac{\tau_\omega}{C} \equiv \frac{\boldsymbol{\tau} \cdot \hat{\mathbf{s}}}{C} \quad (9)$$

$$238 \quad \frac{d\varepsilon}{dt} = \frac{\tau_\varepsilon}{C\omega} \equiv \frac{\boldsymbol{\tau} \cdot \hat{\mathbf{e}}_{\perp 1}}{C\omega} \quad (10)$$

$$239 \quad \frac{d\psi}{dt} = \frac{\tau_\psi}{C\omega} \equiv \frac{\boldsymbol{\tau} \cdot \hat{\mathbf{e}}_{\perp 2}}{C\omega} \quad (11)$$

241 The first term, τ_ω , is a component of the YORP torque parallel to the spin pole and changes
 242 the angular velocity of rotation or the period. The other two components, τ_ε and τ_ψ , are
 243 components along the basis vectors perpendicular to the pole, as shown in the following
 244 equations and Figure 1:

$$245 \quad \hat{\mathbf{e}}_{\perp 1} \equiv \frac{(\hat{\mathbf{N}} \cdot \hat{\mathbf{s}})\hat{\mathbf{s}} - \hat{\mathbf{N}}}{\sin \varepsilon} \quad (12)$$

$$246 \quad \hat{\mathbf{e}}_{\perp 2} \equiv \frac{\hat{\mathbf{s}} \times \hat{\mathbf{N}}}{\sin \varepsilon} \quad (13)$$

248 Thus, in Equations 10 and 11, the torque components τ_ε and τ_ψ change the obliquity of the
 249 spin pole and induce precession of rotation, respectively. The obliquity, ε , is defined as the
 250 axial tilt angle between the spin normal vector $\hat{\mathbf{s}}$ and a normal vector $\hat{\mathbf{N}}$ to the body's orbital
 251 plane. In fact, although the torque component along $\hat{\mathbf{e}}_{\perp 2}$ may excite wobbling rotation, we
 252 assume that the spin pole is quickly relaxed toward uniform rotation around the shortest
 253 axis by energy dissipation, and thus we focus on changes in ω and ε .

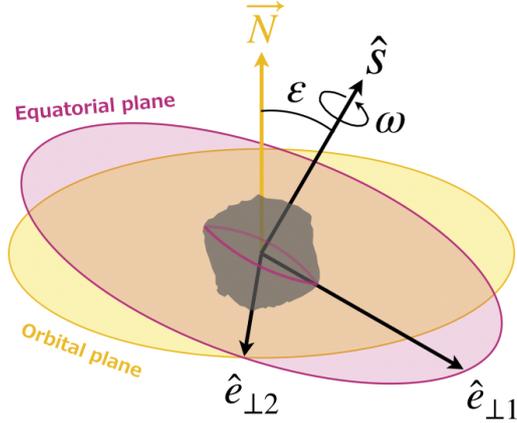


Figure 1. Basis vectors for a spinning body.

3 Results

3.1 Year-averaged torque on Ryugu

254 For the YORP modeling of asteroid Ryugu, we utilized the orbital elements, spin-pole
 255 orientation, and rotation period published by Watanabe et al. (2019) (see Table 1). As a
 256 nominal shape model for this study, we chose the 49152-mesh SPC model released on August
 257 2, 2019. The mean mesh size of the shape model (i.e., mean diameter of circles of equivalent
 258 areas) was 8.4 m. Herein, we present the results of this nominal model and later compare
 259 the resultant YORP effects between shape models of different resolutions, release dates, and
 260 3D reconstruction methods. We divided the cycle of Ryugu’s rotation into 72 equal parts
 261 (every 5 degrees of the rotation angle) and computed the YORP torque, $\boldsymbol{\tau}$, at each time
 262 step. For a rotation period of 7.6 h, the interval of time steps was 382 s. The simulation
 263 was stopped when the asteroid completed one orbit (474 days; 107 288 time steps).

264 Figure 2 illustrates the time variations of each torque component over the cycles of
 265 Ryugu’s rotation (left panels) and revolution (right panels). As the torque variation is
 266 not completely cancelled over the cycles because of Ryugu’s irregular shape, the residual
 267 induces a secular change in the spin parameters. A net torque, $\bar{\boldsymbol{\tau}}$, can be obtained by
 268 averaging the diurnal and seasonal variations. In the nominal case of the SPC-based 49k-
 269 mesh model with the self-shadowing effect, the year-averaged torque results in $(\bar{\tau}_\omega, \bar{\tau}_\epsilon, \bar{\tau}_\psi) =$
 270 $(-0.161, 0.161, 4.05) \text{ N} \cdot \text{m}$. The negative value of the ω -related component implies that
 271 the angular velocity of Ryugu is currently decreasing. According to Equation 9 and the

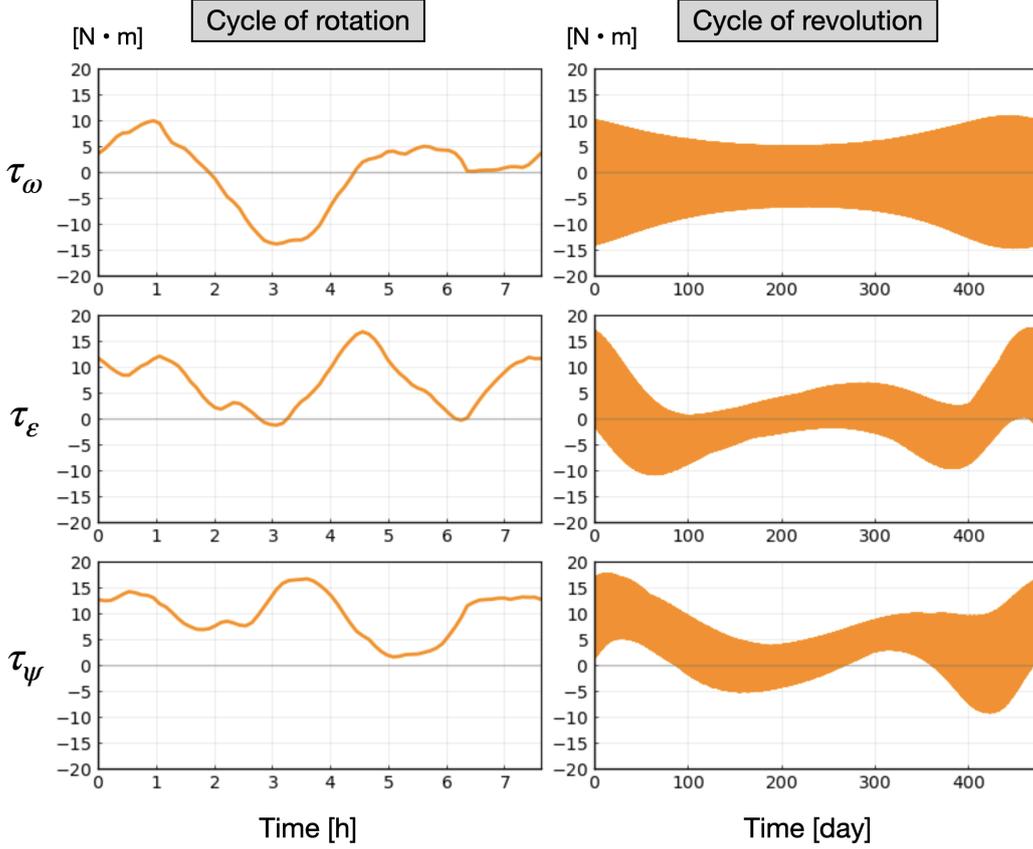


Figure 2. Diurnal and seasonal variations of YORP torque components.

272 moment of inertia of $4.04 \times 10^{16} \text{ kg} \cdot \text{m}^2$, the change in the spin rate of Ryugu corresponds
 273 to $\dot{\omega} = -1.71 \times 10^{-6} \text{ deg/day}^2$. The strength of the YORP effect is often characterized by
 274 the YORP time scale (Rubincam, 2000), which corresponds to the time required to double
 275 or halve the angular velocity ω . For Ryugu, the YORP time scale for doubling the current
 276 rotation period corresponds to $t_{7.6\text{h} \rightarrow 15.2\text{h}} = 0.909$ million years. Note that this time scale
 277 is computed assuming that the rotation decelerates at a constant rate. To investigate the
 278 detailed process of spin evolution and its time scale, the reorientation of the spin axis must
 279 be considered.

280 In addition, the resultant rate of deceleration may vary depending on the meter-scaled
 281 differences of an input shape model (Statler, 2009). Although the highest-resolution models
 282 described in Watanabe et al. (2019) are well matched regardless of the two different tech-
 283 niques of reconstruction, they may contain artifacts in the polar region where fewer images
 284 are obtained, and/or there are slight differences when reducing the resolution of the shape

285 models. Therefore, we surveyed various versions of shape models to determine the sensitivity
 286 of the input model. Table 3 lists the year-averaged torque on each shape model considering
 287 the self-shadowing effect. A shape model ID consists of the reconstruction technique (SFM
 288 or SPC), number of surface meshes, and release date (in YYYYMMDD format). The YORP
 289 simulations are performed only for the low-resolution models of $\sim 49\text{k}$ meshes because de-
 290 tection of locally generated shadows at every time step is computationally expensive. In all
 291 cases, the net torque yields a negative rate of change for angular velocity ω and a positive
 292 one for obliquity ε , indicating that Ryugu is currently spinning down and increasing its
 293 obliquity toward 180° . The torque component that causes precession is difficult to cancel
 294 during a cycle of revolution and yields greater net torque. The deceleration of Ryugu’s
 295 rotation is consistent with its fast rotation in the past. The spin-down time scales are esti-
 296 mated assuming that the spin rate has been decreasing at a constant rate from a 3.5-h to
 297 a 7.633-h period. The estimated time scales of deceleration vary from 0.58 to 8.7 million
 298 years. The cases can be classified into two types: type II, which yields more rapid deceler-
 299 ation ($t_{3.5\text{h}\rightarrow 7.6\text{h}} < 1 \text{ Myr}$), and type IV, which yields slower deceleration (predominantly
 300 $t_{3.5\text{h}\rightarrow 7.6\text{h}} > 1 \text{ Myr}$). The classification criteria are detailed in Section 3.2.

3.2 Obliquity dependence of YORP

301 The spin rate ω and obliquity ε are essential parameters for simulating the long-term
 302 evolution of a rotating body. As the spin-pole direction and obliquity change, the solar irra-
 303 diation conditions of the body vary. In this section, we demonstrate the dependence of the
 304 YORP effect on obliquity and predict Ryugu’s spin evolution in millions of years. To achieve
 305 this, we calculate the thermal net torque on the asteroid, as in the previous section, but for
 306 various obliquities from 0° to 180° . Figure 3 shows the rates of change in ω (dashed) and ε
 307 (solid) as functions of ε , as derived from the nominal model (SHAPE_SPC_49k_v20190802)
 308 in a similar manner to previous studies (Rubincam, 2000; Vokrouhlický & Čapek, 2002;
 309 Čapek & Vokrouhlický, 2004; Bottke et al., 2006). It should be noted that the solid curve
 310 $\tau_\varepsilon/C (= \omega\dot{\varepsilon})$ has three “asymptotic” nodes at $\varepsilon = 0^\circ$, 90° , and 180° . The thermal torque
 311 tends asymptotically toward one of these nodes depending on the initial obliquity ε_0 . For
 312 the nominal shape model, the boundaries at $\varepsilon = 37^\circ$ and 143° dominate the destiny of the
 313 spin evolution and whether the spin pole finally stands upright ($\varepsilon \rightarrow 0^\circ$ or 180°) or falls on
 314 the orbital plane ($\varepsilon \rightarrow 90^\circ$). On the other hand, the dashed curve $\tau_\omega/C (= \dot{\omega})$ in Figure 3
 315 shows that the rotation of Ryugu decelerates at every obliquity. In this case, Ryugu should

Table 3. Thermal net torque and deceleration time scales derived from different shape models. According to Equations 9 to 11, the torque components divided based on the moment of inertia are shown as $\dot{\omega} = \tau_{\omega}/C$, $\omega\dot{\epsilon} = \tau_{\epsilon}/C$, and $\omega\dot{\psi} = \tau_{\psi}/C$. The self-shadowing effect is considered.

Model ID	$\dot{\omega}$	$\omega\dot{\epsilon}$	$\omega\dot{\psi}$	$t_{3.5\text{h}\rightarrow 7.6\text{h}}$	Classification
SHAPE_ ...	$\times 10^{-6}$ [deg/day ²]			[Myr]	
SFM_49k_v20180705	-5.207	2.282	38.34	0.7032	II
SFM_49k_v20180714	-5.834	2.523	39.82	0.6277	
SFM_47k_v20190130	-6.261	2.691	43.28	0.5849	
SPC_49k_v20180705	-5.065	3.410	46.07	0.7230	
SPC_49k_v20180710	-5.010	2.973	43.03	0.7310	
SPC_49k_v20180717	-4.781	2.785	40.81	0.7660	
SPC_49k_v20180719_2	-3.647	2.367	39.12	1.004	
SFM_49k_v20180725_2	-4.560	1.775	40.38	0.8030	IV
SFM_49k_v20180804	-3.531	1.667	39.73	1.037	
SPC_49k_v20180731	-0.5352	1.561	41.35	6.842	
SPC_49k_v20180810	-0.6878	1.434	39.71	5.324	
SPC_49k_v20180816	-0.4212	1.362	39.81	8.693	
SPC_49k_v20180829	-0.6152	1.586	42.25	5.952	
SPC_49k_v20181014	-1.706	1.735	43.17	2.147	
SPC_49k_v20181109	-1.368	1.719	43.03	2.676	
SPC_49k_v20181204	-0.6796	1.477	42.91	5.388	
SPC_49k_v20190308	-1.207	1.607	43.35	3.035	
SPC_49k_v20190328	-1.069	1.548	42.99	3.426	
SPC_49k_v20190802*	-1.705	1.701	42.86	2.148	
SPC_49k_v20200323	-1.406	1.245	42.22	2.604	

*Nominal shape model in this study

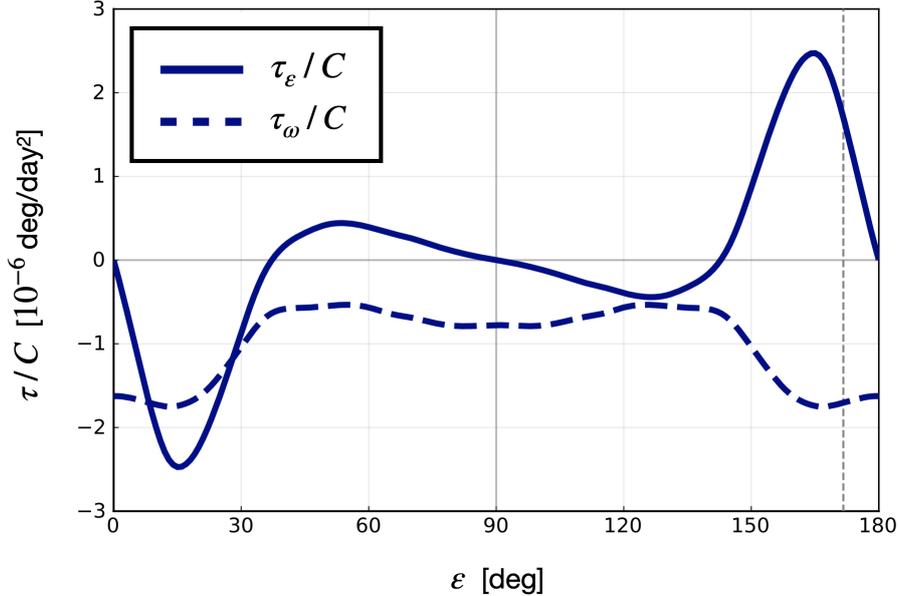


Figure 3. Obliquity dependence of the thermal torque derived from the nominal shape model. The self-shadowing effect is considered. Rates of change in obliquity ε (solid) and spin rate ω (dashed) as functions of the obliquity. The vertical dashed line at $\varepsilon = 171.6^\circ$ represents the nominal obliquity observed by Hayabusa2.

316 reach a permanent spin-down phase at one of the three asymptotic obliquities. The vertical
 317 dashed line in Figure 3 represents the current obliquity of Ryugu ($\varepsilon = 171.64^\circ$), which was
 318 observed by Hayabusa2 (Watanabe et al., 2019). As already mentioned in 3.1, Ryugu is cur-
 319 rently considered to be spinning down with the obliquity of the spin pole increasing toward
 320 180° . In contrast, the spin of asteroid 101955 Bennu (a target body of NASA’s OSIRIS-REx
 321 mission) is accelerating with an obliquity of nearly 180° (Nolan et al., 2019; Hergenrother
 322 et al., 2019).

323 Vokrouhlický and Čapek (2002) performed YORP simulations using randomly gener-
 324 ated shapes of virtual asteroids and classified hundreds of the cases according to the obliquity
 325 they would settle into after sufficient time. For types I and II, the spin axes will eventually
 326 fall ($\varepsilon \rightarrow 90^\circ$) and rise ($\varepsilon \rightarrow 0^\circ$ or 180°), respectively. These two types account for 80%
 327 of the 500 cases. A further 10% of the cases are classified as type III, which have different
 328 asymptotic obliquities from the above two types (e.g., $\varepsilon = 30^\circ$ and 150° in the shape of
 329 asteroid 2063 Bacchus). Type IV is the remaining minority, which has three asymptotic

330 obliquities at $\varepsilon = 0^\circ$, 90° , and 180° depending on the initial obliquity. The nominal case
 331 plotted in Figure 3 is classified as this type.

332 Next, we examine the ε -dependence of the net torque on the various shape models in
 333 Table 3. The self-shadowing effect is considered in this survey. It is found that the YORP
 334 effect on Ryugu results in either type II or IV. The seven cases in type II and 13 cases
 335 in type IV are shown separately in Figure 4. Considering the symmetry of the even/odd
 336 functions, half of each is omitted from display. The rates of change in the spin rate on the left
 337 and obliquity on the right can be observed. In the high-obliquity area around the nominal
 338 obliquity ($\varepsilon = 171.6^\circ$; marked by the gray dashed line), both types tend toward the state
 339 of the upright spin pole. If Ryugu follows type IV evolution, it is necessary for the body to
 340 start with an obliquity of over $\sim 140^\circ$ to reach the current value. Otherwise, Ryugu's spin
 341 axis will become parallel to the orbital plane. When the axis of rotation becomes upright (at
 342 an obliquity of 0° , equivalent to 180°), type II shapes tend to yield greater deceleration than
 343 type IV shapes. Thus far, the time scale of deceleration depends on subtle differences in the
 344 shape models to be entered and the indeterminacy of approximation in our numerical model,
 345 but Ryugu is likely to be spinning down with the pole rising toward $\varepsilon = 180^\circ$. Changes in
 346 Ryugu's spin state over time based on the obliquity dependence is discussed in Section 5.1.

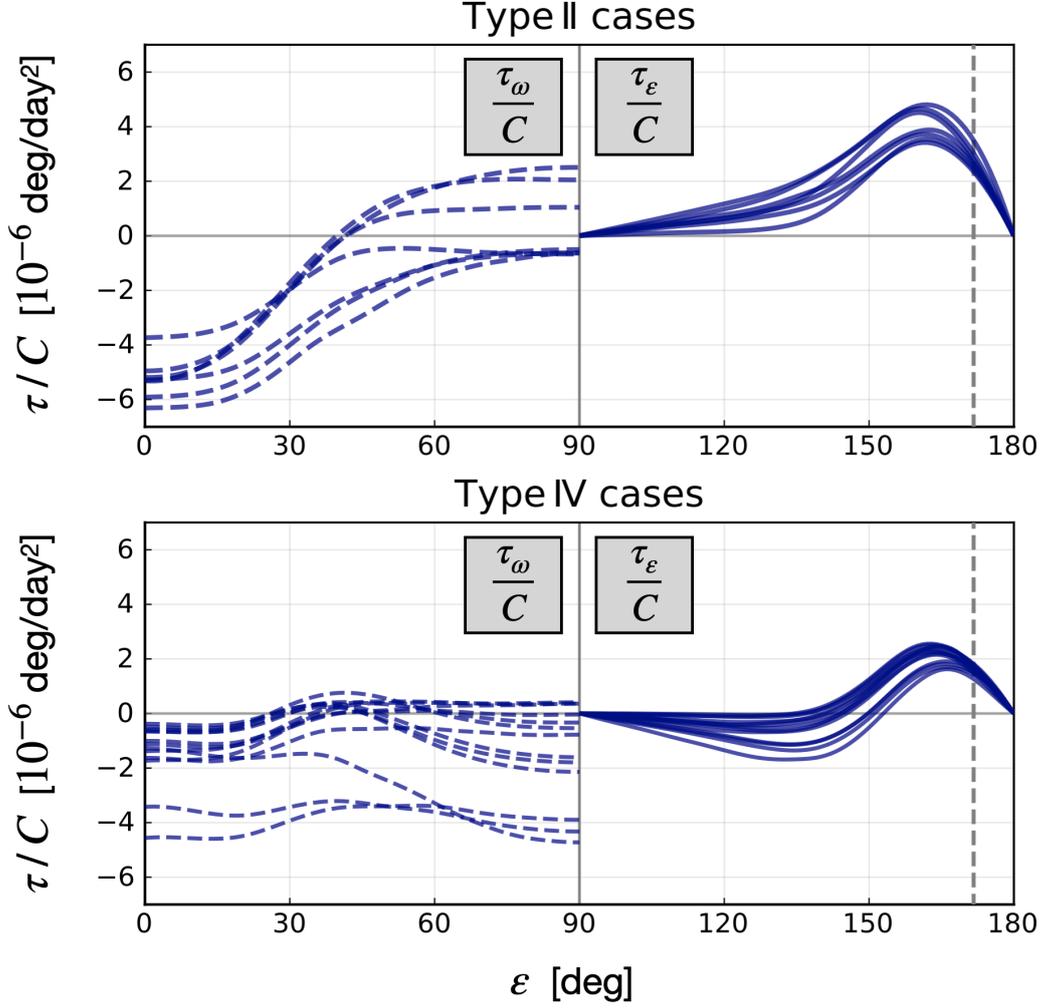


Figure 4. Obliquity dependence surveyed for 20 shape models in Table 3. The self-shadowing effect is considered. The left half of each panel shows the thermal torque component required to change the spin rate as a function of obliquity. The right half shows the torque component required to change the obliquity. The 20 models are classified into types II (seven cases in the upper panel) and IV (13 cases in the lower panel) according to Vokrouhlický's criteria.

4 Validity of YORP Simulations

347 In general, a numerical simulation of the YORP effect strongly depends on small-scale
 348 topographic features of the shape model (Statler, 2009; Breiter et al., 2009). To evaluate this
 349 uncertainty, we prepared “perturbed” shape models from the nominal model used in Section
 350 3 and repeated the YORP simulations (following the numerical experiments by Nolan et
 351 al. (2019)). The perturbed models were created by applying noise to the nominal model
 352 on a scale similar to the facet size. Each vertex of the original shape model was randomly
 353 shifted in the radial direction, for example, within a range of ± 1 m. We demonstrated 1000
 354 perturbed models for each noise of ± 1 m and ± 2 m by ignoring the self-shadowing effect.
 355 The upper panels in Figure 5 illustrate the nominal shape model and perturbed models with
 356 different noise levels. The mean mesh size \bar{D}_S of the nominal shape model is 8.4 m, which
 357 is hereby defined as the mean diameter of circles of equivalent areas. As the noise increases,
 358 more artificial bumps appear on the surface. The histograms show the distributions of
 359 the rates of year-averaged acceleration, $\dot{\omega}$. Given the noise within ± 1 m (orange), $\dot{\omega}$ is
 360 distributed around the nominal value of -1.32×10^{-6} [rad/day²] with a 1σ uncertainty of
 361 $\pm 19\%$. For larger-scale noise in the shape model, the distribution of the YORP acceleration
 362 spreads, and some of the cases change to spinning up ($\dot{\omega} > 0$). According to Watanabe et al.
 363 (2019), the shape models of 3 million meshes derived from SPC and SfM are well matched
 364 within a standard deviation of elevation of ~ 1.5 m. The lower-resolution model used in
 365 this study was created by downsizing the 3M-mesh model. Random artifacts on the shape
 366 model at the meter scale affect the magnitude of the resultant YORP effect to some extent;
 367 however, they are unlikely to change the sign of the acceleration rate.

368 We also provide an overview of the YORP acceleration dependence on the resolution
 369 of an input shape model in the case of Ryugu. Ignoring the self-shadowing effect, we
 370 performed YORP simulations up to the highest-resolution models. The SPC-based models
 371 of each version have four different resolutions (i.e., numbers of surface facets): $N_S = 49\ 152$,
 372 $196\ 608$, $786\ 432$, and $3\ 145\ 728$. The SfM models are also released with approximately the
 373 same resolutions. Figure 6 represents the YORP acceleration rates derived from the various
 374 shape models as functions of their resolutions. The SPC and SfM models are plotted as
 375 blue circles and orange triangles, respectively. Shape models released on the same date are
 376 connected with each other. A lower-resolution model was created by reducing the highest-
 377 resolution model released on the same date. Except for the five shape families (the SPC
 378 models released on 2018-07-31, 2018-08-10, 2018-08-16, 2018-08-29, and 2020-03-23), the

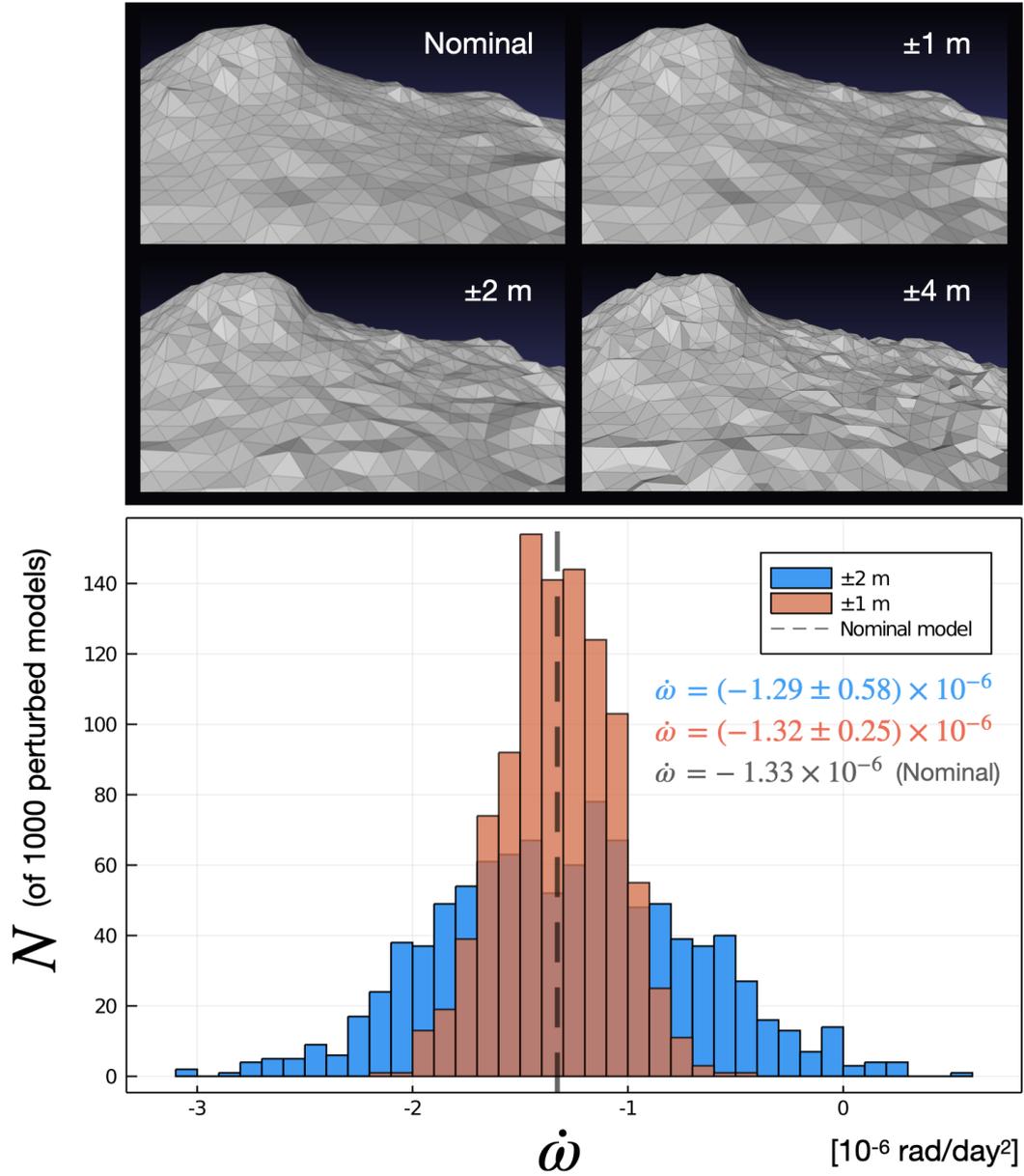


Figure 5. YORP acceleration/deceleration derived from perturbed shape models. The self-shadowing effect is neglected in this survey.

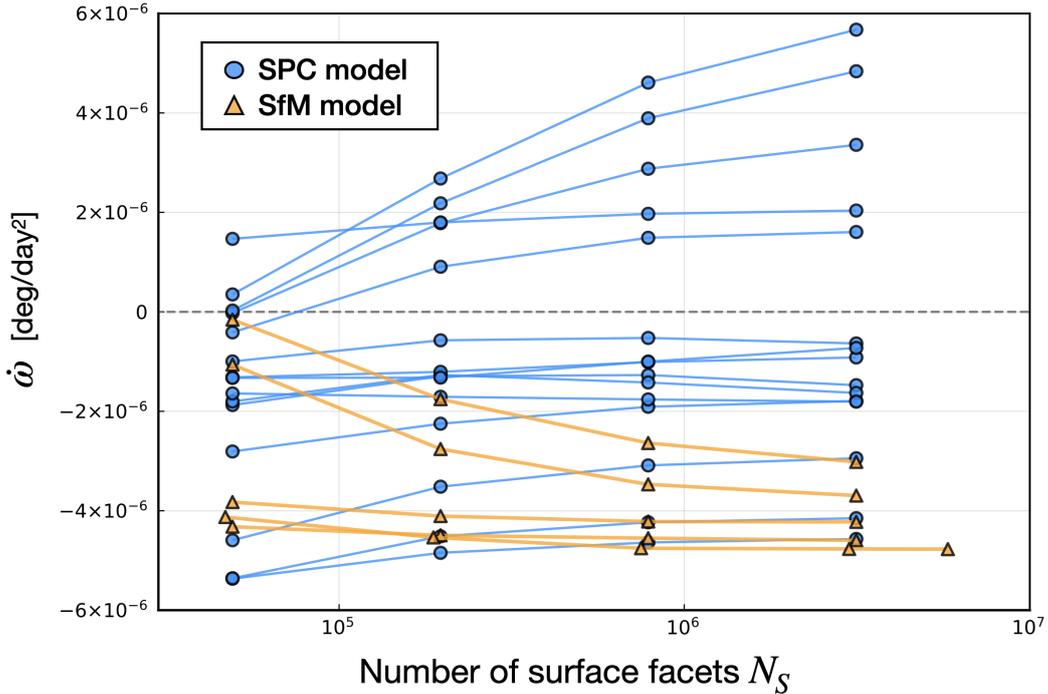


Figure 6. Rotational acceleration as a function of the resolution of the input shape models. The self-shadowing effect is neglected.

379 remaining models yielded negative rates of rotational acceleration. In the low-resolution
 380 models of ~ 49 k meshes, however, we confirmed that all cases resulted in deceleration of
 381 rotation when considering the self-shadowing effect (see Table 3). As reported by Breiter et
 382 al. (2009), some shape families tend to yield greater rates of acceleration/deceleration as the
 383 resolution of the shape models increases without converging to a certain value. The higher
 384 resolution model has a larger variance in the slopes of the surface facets, and the magnitude
 385 of the resultant acceleration can increase. A detailed thermal model, as described below,
 386 is computationally costly, and its convergence to the resolution of the shape model has not
 387 yet been confirmed.

388 In this study, we approximated the balance of incoming and outgoing radiation using
 389 a simple model based on Rubincam (2000). We examined the extent to which this model
 390 works for the YORP simulation on asteroid Ryugu. Rugged topography can block direct
 391 sunlight and cast a shadow on the surface. This self-shadowing effect could generate a
 392 significant bias in the radiation emitted from the body (Breiter et al., 2009). Herein, we
 393 turned self-shadowing on and off depending on the computation time. In addition, reabsorp-

394 tion of thermal emission from the surrounding ground (“self-heating”) and nonzero thermal
 395 conductivity could alter the thermal torque exerted on the asteroid (Čapek & Vokrouh-
 396 lický, 2004). A thermophysical model (TPM) was developed for simulating the distribution
 397 of the surface temperature on Ryugu and comparing its results with mid-infrared images
 398 obtained from the thermal infrared imager (TIR) on the Hayabusa2 spacecraft (Takita et
 399 al., 2017). We performed the TPM simulation using Ryugu’s ephemeris and obtained the
 400 net torque component required to change the spin rate of Ryugu on August 1, 2018. The
 401 200k-mesh SfM model (SHAPE_SFM_200k_v20180804) and a constant thermal inertia of
 402 $300 \text{ J} \cdot \text{m}^{-2} \cdot \text{K}^{-1} \cdot \text{s}^{-0.5}$ (tiu) were used for the simulation. Figure 7 compares the diurnal
 403 variation of the thermal torque obtained for different thermal models. The blue curve in
 404 the lower panel considers the total irradiation energy accounting for the self-shadowing and
 405 self-heating effects (upper left panel), but zero conductivity is assumed in accordance with
 406 Equation 3. The orange curve represents the time variation of the thermal torque based
 407 on the distribution of surface temperature considering nonzero conductivity (upper right
 408 panel). The TPM simulation solves the one-dimensional heat conduction equation in the
 409 depth direction on each facet with the surface boundary condition according to Equation 1.
 410 The gray dashed curve is derived from our implementation of Rubincam’s model with the
 411 spin phase fitted to the TPM simulation.

412 The blue curve indicates that the local shadows on the surface generate a fine irregular-
 413 ity in the time variation in the thermal torque. By averaging its ω -related component, the
 414 shadowing effect is shown to increase the magnitude of the YORP deceleration compared to
 415 the simplest model in this period of time. The daily averaged torque was (1) $\bar{\tau}_\omega = -0.365$
 416 $\text{N} \cdot \text{m}$ in Rubincam’s model and (2) $\bar{\tau}_\omega = -0.407 \text{ N} \cdot \text{m}$ in the shadowing model. In one
 417 revolution cycle, we confirmed that the shadows increased or decreased the magnitude of
 418 deceleration randomly. As shown by the orange curve, thermal inertia lowered the contrast
 419 of radiation between the hemispheres of daytime and nighttime and lowered the peak of
 420 the thermal torque. In addition, a phase delay of approximately 15 min can be observed
 421 between the nonzero conductivity model and the others. Nonzero conductivity, however,
 422 does not change the total amount of radiation throughout one rotational cycle. Therefore,
 423 the phase lag of the thermal torque variation was insignificant to the net acceleration or
 424 deceleration, as established previously (Čapek & Vokrouhlický, 2004). On the other hand,
 425 the delayed radiation due to thermal inertia is considered to be more effective in altering
 426 the spin pole direction (Čapek & Vokrouhlický, 2004; Breiter et al., 2007; Mysen, 2008;

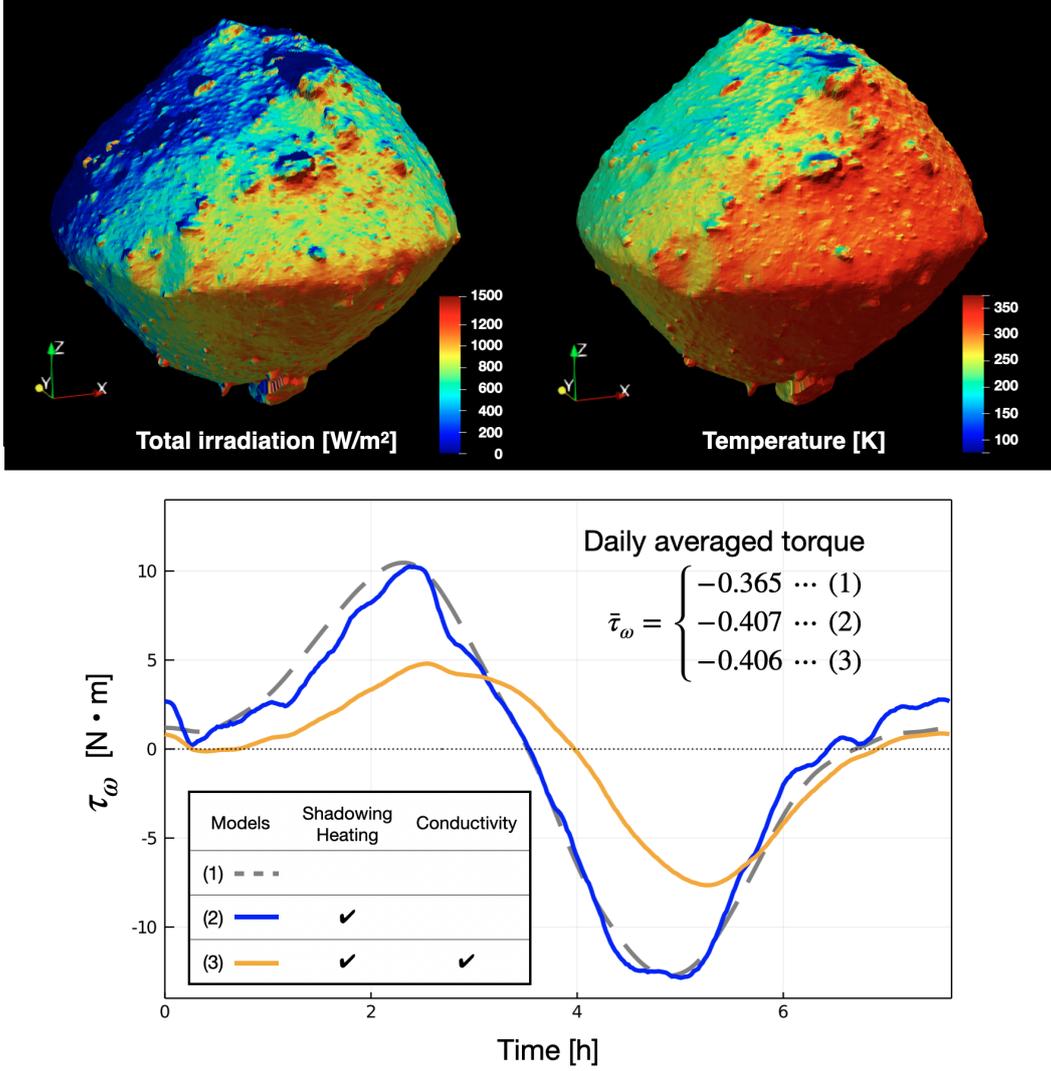


Figure 7. (*Upper*) Spatial distribution of the total radiation input to each facet and the surface temperature obtained using the TPM (Takita et al., 2017). (*Lower*) Time variation of the thermal torque component required to change the spin rate of Ryugu over a diurnal cycle. The blue curve considers the self-shadowing and self-heating effects in addition to our implementation of Rubincam’s model (gray curve). Thermal inertia ($\Gamma = 300$ tiu) is also accounted for in the orange curve.

427 Scheeres, 2007). As revealed by the infrared observations of TIR and the Mobile Asteroid
428 Surface Scout (MASCOT) lander, the thermal inertia of Ryugu's surface material was esti-
429 mated as approximately 300 tiu (Okada et al., 2020) or 225 ± 45 tiu (Shimaki et al., 2020),
430 corresponding to a thermal conductivity of ~ 0.1 W/(m · K) (Grott et al., 2019). Although
431 Ryugu is spinning at a relatively mild spin rate and is covered with porous boulders of low
432 conductivity, the dependence of the net torque on thermal inertia should be investigated in
433 the future.

5 Discussion

5.1 YORP-induced spin evolution of Ryugu

434 We explored the effect of the obliquity of Ryugu’s spin pole on the thermally induced
 435 torque in Section 3.2. This enables us to predict the long-term evolution of the spin state
 436 over millions of years. The top panels in Figure 8 demonstrate representative examples
 437 of the ε -dependence of the YORP effect for type II and IV cases. The latest SFM model
 438 (SHAPE_SFM_47k_v20190130) and our nominal model (SHAPE_SPC_49k_v20190802) were
 439 chosen from each group. Again, the self-shadowing effect was considered, and the current
 440 orbit of Ryugu was used ($a = 1.19$ AU). The middle and bottom panels represent the rotation
 441 period and obliquity of the asteroid, respectively, as functions of time after providing initial
 442 conditions. The initial rotation period is set to 3.5 h, obliquities range from 100° to 170° .
 443 The evolution paths follow the ε -dependence on the corresponding upper panels and the
 444 equations of motion in Equations 9 and 10. The currently observed spin parameters of
 445 Ryugu are marked at $P = 7.632$ h and $\varepsilon = 171.6^\circ$ by gray dashed lines in each panel. The
 446 nominal case of type IV clearly shows that an initial obliquity smaller than 143° cannot
 447 achieve an upright spin pole. For the type II example, an upright spin pole can be achieved
 448 for any initial obliquity exceeding 90° . The time scale for the spin axis to rise ($\varepsilon \rightarrow 180^\circ$) is
 449 within a few million years for the nominal case. For a type II case starting with a smaller
 450 obliquity, the spin pole can take nearly 5 million years to rise.

451 Moreover, we also surveyed for various initial rotation periods. The contour plots in
 452 Figure 9 show the time required for the rotation period to reach 7.632 h as a function of the
 453 initial obliquity and period. The same shape models as Figure 8 were used. In the nominal
 454 case of type IV, the time scale of rotational deceleration is within a few million years. Note
 455 that the possible obliquity must equal or exceed 143° to prevent the spin pole from collapsing
 456 onto the orbital plane. For the type II case, the spin-down time scale could be up to 6.5
 457 million years if the body enters a collapsed spin-pole state with a small deceleration rate.
 458 Although the time scale varies depending on the input shape models, the path of the spin
 459 evolution is as described above.

460 As mentioned above, the YORP-induced torque is responsible for keeping the spin pole
 461 perpendicular to the orbital plane. However, the current obliquity of Ryugu is 172° , and
 462 it does not perfectly match 180° . Considering the relatively short time scale of change in
 463 the spin-pole direction, Ryugu is likely to have experienced a spin-related disturbance event

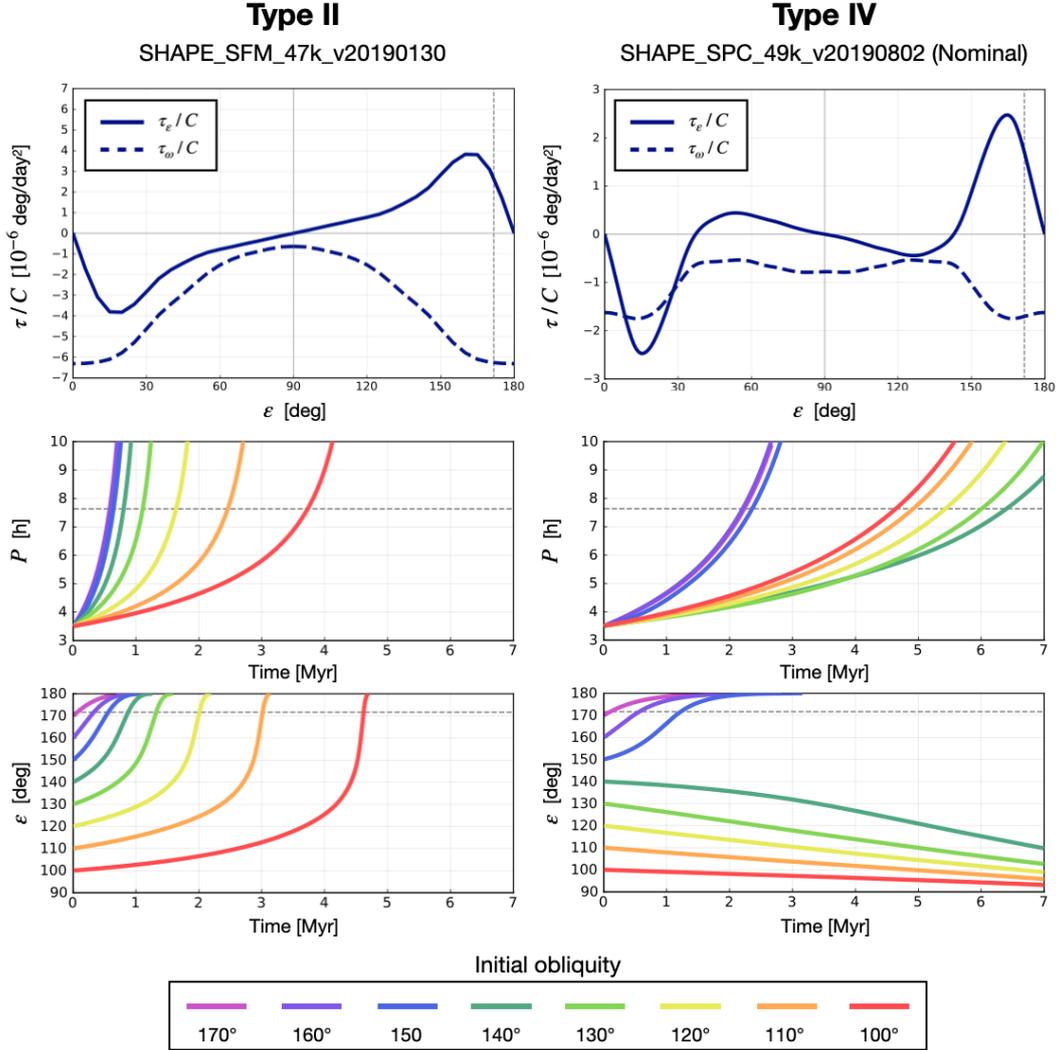


Figure 8. Paths of spin evolution according to representative examples of obliquity dependence on the YORP effect for type II (left) and type IV (right) cases. The top panels show the dependence of the thermal torque on obliquity. The middle and bottom panels plot the temporal evolution of the rotation period P and obliquity ε , respectively, assuming an initial period of 3.5 h and obliquities in the range of $100^\circ - 170^\circ$. The horizontal gray dashed lines indicate the current period and obliquity of Ryugu.

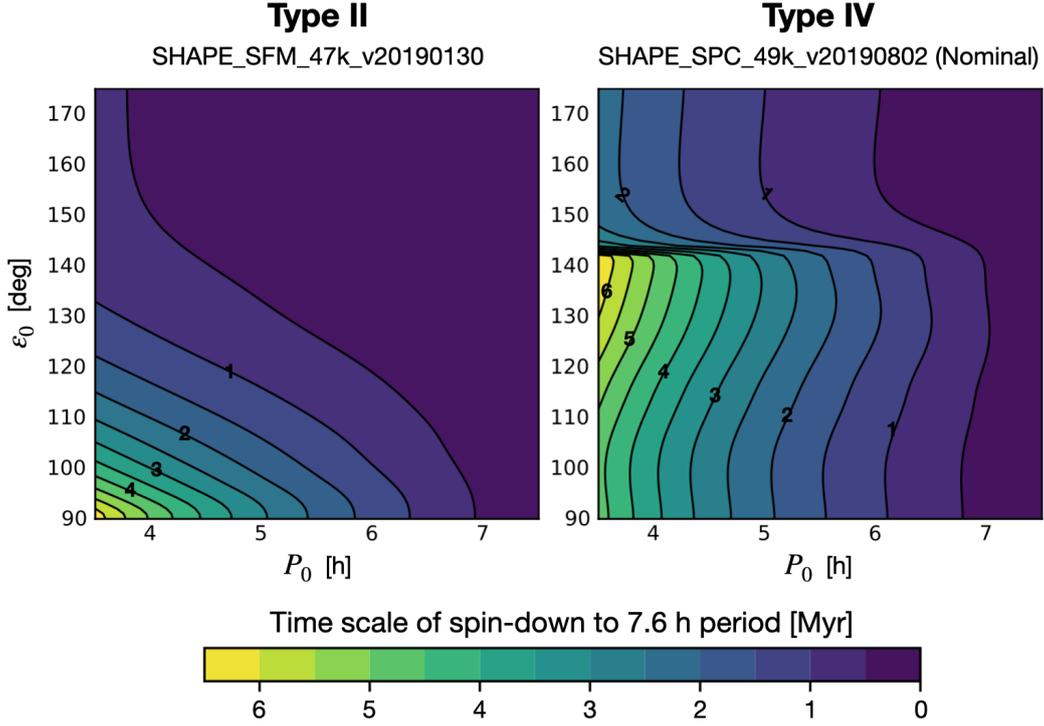


Figure 9. Time required to decelerate to the current rotation period of Ryugu as a function of the initial obliquity, ϵ_0 , and period, P_0 for a type II (left) and type IV evolution (right).

464 within the last several million years. As a single event, a close encounter with a planet
 465 could potentially alter radically the angular momentum of a near-Earth asteroid (Scheeres
 466 et al., 2000; Benson et al., 2019). The spin modification due to the gravitational torque of
 467 a planet strongly depends on the hyperbolic orbit and spin-pole direction of the asteroid
 468 with respect to the planet. The kinetic energy of an impactor could also directly alter the
 469 angular momentum of an asteroid. The effect of an impact event on Ryugu is estimated
 470 in Section 5.2. A topographic change caused by crater formation could have altered the
 471 YORP effect on the body over its geological time scale. According to the list of craters on
 472 Ryugu compiled by Noguchi et al. (2021), the total area of all these craters is $3.65 \times 10^5 \text{ m}^2$,
 473 which corresponds to approximately 13% of the total surface area of the body. In addition,
 474 prediction of non-uniform rotation is left for future work because the thermal torque can
 475 cause precession of the spin pole.

5.2 Effect of an impact event

The Hayabusa2 mission conducted an artificial cratering experiment using a small carry-on impactor (SCI), which revealed that the artificial crater on Ryugu was formed in the gravity-dominated regime owing to the significantly small cohesion of its surface materials (Arakawa et al., 2020). According to the conventional scaling law in this regime and other parameters from the impact conditions of the SCI experiment, Arakawa et al. (2020) provided the scaling law for the cohesionless surface of Ryugu as follows:

$$\pi_R = 0.62 \times \pi_2^{-0.17} \pi_4^{0.0014} \quad (14)$$

where π_R , π_2 , and π_4 are the conventional dimensionless parameters (Housen & Holsapple, 2011). Using this scaling law and the size of the largest crater observed on Ryugu, the maximum change in the rotation parameters owing to an impact can be estimated. The largest crater, *Urashima*, is 246.9 ± 7.0 m in diameter and is located near the equator (Noguchi et al., 2021). The other collision parameters are listed in Table 4. Therefore, we considered a chondritic meteorite of radius ~ 1 m that collided with a rotating spherical body similar to Ryugu at the mean impact velocity in the main belt. Assuming that the target body acquired all the kinetic energy of the impactor without any loss, the maximum change in the angular momentum was calculated to be $\Delta L = 4.1 \times 10^{10}$ kg · m²/s when the impactor collided in a tangential direction to the spherical target. This increase is less than 1% of the original angular momentum of Ryugu, $L = 9.2 \times 10^{12}$ kg · m²/s. Even if the impactor collided in the east–west direction at the equator, the change in the rotation period would be limited to approximately 120 s in both the acceleration and deceleration cases. In the event of a north–south collision, the direction of the spin pole would change by a maximum of only 0.25°. In reality, the change would be significantly smaller because of energy dissipation, etc. It can be concluded that even the formation of the largest crater on Ryugu would not have been able to disturb its rotation to such an extent.

5.3 Implications for geologic history of Ryugu

Despite the uncertainty in the numerical YORP modeling, this study strongly suggests that the YORP effect could have been a major factor in the rotational deceleration of Ryugu since its currently observed shape was formed. Our YORP simulation based on Ryugu’s shape model yielded rates of change in angular velocity of $(-0.42 - -6.3) \times 10^{-6}$ deg/day² (see Table 3). In most cases, the spin pole of Ryugu was maintained for obliquities of nearly

Table 4. Impact parameters used to estimate the maximum change in the rotation of Ryugu.

Parameters	Notation	Value	Unit
Radius of <i>Urashima</i> crater	R	123	m
Impact velocity*	u	5300	m/s
Target density	ρ	1190	kg/m ³
Target gravity**	g	1.2×10^{-4}	m/s ²
Projectile radius	a	1.07	m
Projectile density	δ	3000	kg/m ³

*Equal to mean impact velocity in the main belt (Bottke et al., 1994).

**Corresponding to a spherical body with a GM of $30 \text{ m}^3/\text{s}^2$ and an equatorial radius of 502 m (Watanabe et al., 2019).

505 180°. In this obliquity range, the deceleration rate can be considered to be approximately
 506 constant in all cases (see the left side of Figure 4). Assuming a constant deceleration at
 507 these rates, it would have taken 0.58 – 8.7 million years to alter the rotation period from 3.5
 508 to 7.6 h. This is consistent with the time scales (0.3–8.1 Ma) of spin deceleration estimated
 509 by Morota et al. (2020) based on crater counting, as previously discussed in Section 1.1.

510 As the YORP effect depends on the body’s shape, the deceleration time scale corre-
 511 sponds to the time that has passed since the occurrence of a major change in topography
 512 during the fast rotation phase. Statistical analysis of fresher craters with bluer spectra on
 513 Ryugu indicated that the asteroid experienced surface reddening due to solar heating when
 514 it migrated from the inner main belt to the near-Earth orbit 0.3–8 million years ago (Morota
 515 et al., 2020). Hence, our estimated time scale of the rotational deceleration is comparable
 516 to the time that Ryugu has spent in the near-Earth orbit. A recent paper by Cho et al.
 517 (2021) estimated the surface age of each geological unit on the asteroid. According to these
 518 crater statistics, the equatorial ridge is the oldest terrain on Ryugu, thought to have formed
 519 23 – 30 million years ago. This early deformation is consistent with the direct formation of
 520 the top shape during the accumulation of the rubble pile (Michel et al., 2020). However,
 521 the YORP deceleration time scale is much shorter than the formation age of the equatorial
 522 ridge. Therefore, a more recent resurfacing event may have impacted the YORP effect on
 523 Ryugu, becoming a tipping point in its dynamical history in terms of spin. A corresponding

524 geological event could be the formation of the largest crater, *Urashima*, or the formation
525 of the western bulge, which is considered to be a younger unit with fewer craters than the
526 eastern hemisphere (Hirata et al., 2020). The formation ages of these units are estimated
527 to be 5 – 12 and 2 – 9 Ma, respectively, depending on the timing of the orbital migration of
528 Ryugu from the main belt to its near-Earth orbit (Cho et al., 2021). Our estimate of the
529 deceleration time scale is comparable with the ages of these events, and it is possible that
530 Ryugu had been spinning at a fast rate until the event time.

531 During fast rotation at a period of ~ 3.6 h, the Coriolis force may accumulate impact
532 ejecta asymmetrically on a spinning body (Hirata et al., 2021). Some of the major craters
533 in the equatorial region (e.g., *Urashima*, *Cendrillon*, and *Kolobok*) have higher rims on the
534 west sides. These east-west asymmetric craters may bias the YORP effect on Ryugu. In
535 the future, we need to consider the possibility that the formation of multiple craters has
536 gradually altered the spin history of the body, or that the inward orbital migration decreased
537 the heliocentric distance and hastened the spin alteration. In addition, roughness smaller
538 than the size of the meshes (centimeter to decimeter) may have contributed to the increase
539 in spin rate caused by thermal torque, known as the tangential YORP effect (Golubov &
540 Krugly, 2012; Golubov et al., 2014; Golubov, 2017). The boulder-rich surface of Ryugu
541 tends to impede rotational deceleration caused by the normal YORP and extend the time
542 scale of the spin-down. As observed by the TIR on Hayabusa2, the surface roughness induces
543 thermal infrared beaming toward the Sun (Okada et al., 2020), which also could dampen
544 the magnitude of the YORP effect (Rozitis & Green, 2011, 2012).

545 The YORP simulation in this study also predicts the change in the direction of Ryugu's
546 rotation axis. The currently observed shape of Ryugu yields the stability of the spin pole at
547 an obliquity of 180° . For Ryugu, it is likely that the spin pole has remained perpendicular
548 to the orbital plane even if a spin disturbance event has occurred, as explained in Section
549 5.1. In addition to the mass-shedding process on the surface of Ryugu, the pole stability
550 may contribute to the formation of the latitudinal pattern in the visible and near-infrared
551 spectra (Sugita et al., 2019). This may have protected the polar regions from sunlight and
552 maintained their bluer spectra (Tatsumi et al., in prep.).

6 Conclusion

553 In this study, we investigated the YORP-induced spin evolution of asteroid Ryugu.
 554 We also confirmed that a simplified thermal model assuming zero thermal conductivity can
 555 compute the YORP torque exerted on Ryugu with sufficient accuracy. The approximation
 556 reduced the computational time and allowed us to examine various versions of the shape
 557 models. Regardless of the differences between the 3D construction methods and input
 558 image datasets, it is suggested that Ryugu is currently spinning down at a rate of $(-0.42$
 559 $- -6.3) \times 10^{-6}$ deg/day², and a reasonable time scale of 0.58 – 8.7 million years is given
 560 for the spin alteration that has occurred since the fast rotation in the past. Combined with
 561 Hayabusa2 remote sensing data, our findings on the dynamical and geological history of
 562 Ryugu will contribute to the interpretation of future analyses of samples returning to Earth
 563 at the end of 2020.

Acknowledgments

564 We would like to thank all members of the Hayabusa2 mission team for their support of
 565 the data acquisition. All data will be available at the JAXA Data Archives and Transmission
 566 System (DARTS) at <https://www.darts.isas.jaxa.jp/planet/project/hayabusa2/>. This
 567 study is supported by the JSPS KAKENHI No. JP17H06459 (“Aqua Planetology”) and
 568 the JSPS Core-to-Core Program “International Network of Planetary Sciences”. We would
 569 like to thank Editage (www.editage.com) for English language editing.
 570

References

- Arakawa, M., Saiki, T., Wada, K., Ogawa, K., Kadono, T., Shirai, K., ... Miura, A. (2020).
 An artificial impact on the asteroid (162173) Ryugu formed a crater in the gravity-
 dominated regime. *Science*. doi: 10.1126/science.aaz1701
- Benson, C. J., Scheeres, D. J., & Moskovitz, N. A. (2019). Spin state evolution of asteroid
 (367943) Duende during its 2013 earth flyby. *Icarus*, 113518. Retrieved from <http://www.sciencedirect.com/science/article/pii/S0019103519304075> doi: <https://doi.org/10.1016/j.icarus.2019.113518>
- Bottke, W. F., Nolan, M. C., Greenberg, R., & Kolvoord, R. A. (1994). Velocity
 Distributions among Colliding Asteroids. *Icarus*, 107(2), 255–268. doi: 10.1006/
 icar.1994.1021
- Bottke, W. F., Vokrouhlický, D., Rubincam, D. P., & Nesvorný, D. (2006, may). THE

- YARKOVSKY AND YORP EFFECTS: Implications for Asteroid Dynamics. *Annual Review of Earth and Planetary Sciences*, *34*(1), 157–191. Retrieved from <http://www.annualreviews.org/doi/10.1146/annurev.earth.34.031405.125154> doi: 10.1146/annurev.earth.34.031405.125154
- Breiter, S., Bartczak, P., Czekaj, M., Oczujda, B., & Vokrouhlický, D. (2009). The YORP effect on 25 143 Itokawa. *Astronomy and Astrophysics*, *507*(2), 1073–1081. doi: 10.1051/0004-6361/200912543
- Breiter, S., Michalska, H., Vokrouhlický, D., & Borczyk, W. (2007). Radiation-induced torques on spheroids. *Astronomy and Astrophysics*, *471*(1), 345–353. doi: 10.1051/0004-6361:20077313
- Čapek, D., & Vokrouhlický, D. (2004). The YORP effect with finite thermal conductivity. *Icarus*, *172*(2), 526–536. doi: 10.1016/j.icarus.2004.07.003
- Cho, Y., Morota, T., Kanamaru, M., Takaki, N., Yumoto, K., Ernst, C. M., ... Sugita, S. (2021). Geologic History and Crater Morphology of Asteroid (162173) Ryugu. *Journal of Geophysical Research - Planets*. Retrieved from <https://www.essoar.org/action/showAuthorDashboard?state=submitted> doi: 10.1002/essoar.10506689.1
- Efroimsky, M. (2001). Relaxation of wobbling asteroids and comets - Theoretical problems, perspectives of experimental observation. *Planetary and Space Science*, *49*(9), 937–955. doi: 10.1016/S0032-0633(01)00051-4
- Gaskell, R., Barnouin-Jha, O., Scheeres, D., Mukai, T., Hirata, N., Abe, S., ... Kominato, T. (2006). Landmark Navigation Studies and Target Characterization in the Hayabusa Encounter with Itokawa. *AIAA/AAS Astrodynamics Specialist Conference and Exhibit*. doi: 10.2514/6.2006-6660
- Gaskell, R. W., Barnouin-Jha, O. S., Scheeres, D. J., Konopliv, A. S., Mukai, T., Abe, S., ... Demura, H. (2008). Characterizing and navigating small bodies with imaging data. *Meteoritics & Planetary Science*, *43*(6), 1049–1061. Retrieved from <https://onlinelibrary.wiley.com/doi/abs/10.1111/j.1945-5100.2008.tb00692.x> doi: 10.1111/j.1945-5100.2008.tb00692.x
- Golubov, O. (2017). Analytic Model for Tangential YORP. *The Astronomical Journal*, *154*(6), 238. doi: 10.3847/1538-3881/aa88ba
- Golubov, O., & Krugly, Y. N. (2012). Tangential component of the YORP effect. *Astrophysical Journal Letters*, *752*(1). doi: 10.1088/2041-8205/752/1/L11
- Golubov, O., Scheeres, D. J., & Krugly, Y. N. (2014). A three-dimensional model of

- tangential yorp. *Astrophysical Journal*, 794(1). doi: 10.1088/0004-637X/794/1/22
- Grott, M., Knollenberg, J., Hamm, M., Ogawa, K., Jaumann, R., Otto, K. A., ... Moussi-Soffys, A. (2019). *Low thermal conductivity boulder with high porosity identified on C-type asteroid (162173) Ryugu*. doi: 10.1038/s41550-019-0832-x
- Hergenrother, C. W., Maleszewski, C. K., Nolan, M. C., Li, J. Y., Drouet d'Aubigny, C. Y., Shelly, F. C., ... Marty, B. (2019). The operational environment and rotational acceleration of asteroid (101955) Bennu from OSIRIS-REx observations. *Nature Communications*, 10(1). doi: 10.1038/s41467-019-09213-x
- Hirabayashi, M., Tatsumi, E., Miyamoto, H., Komatsu, G., Sugita, S., Watanabe, S.-i., ... Tsuda, Y. (2019). The Western Bulge of 162173 Ryugu Formed as a Result of a Rotationally Driven Deformation Process. *The Astrophysical Journal*, 874(1), L10. doi: 10.3847/2041-8213/ab0e8b
- Hirata, N., Morota, T., Cho, Y., Kanamaru, M., ichiro Watanabe, S., Sugita, S., ... ichi Iijima, Y. (2020). The spatial distribution of impact craters on Ryugu. *Icarus*, 338. doi: 10.1016/j.icarus.2019.113527
- Hirata, N., Namiki, N., Yoshida, F., Matsumoto, K., Noda, H., Senshu, H., ... ichiro Watanabe, S. (2021). Rotational effect as the possible cause of the east-west asymmetric crater rims on Ryugu observed by LIDAR data. *Icarus*. doi: 10.1016/j.icarus.2020.114073
- Housen, K. R., & Holsapple, K. A. (2011). Ejecta from impact craters. *Icarus*, 211(1), 856–875. doi: 10.1016/j.icarus.2010.09.017
- Kaasalainen, M., Ďurech, J., Warner, B. D., Krugly, Y. N., & Gaftonyuk, N. M. (2007, mar). Acceleration of the rotation of asteroid 1862 Apollo by radiation torques. *Nature*, 446(7134), 420–422. Retrieved from <http://www.nature.com/articles/nature05614> doi: 10.1038/nature05614
- Kitazato, K., Milliken, R. E., Iwata, T., Abe, M., Ohtake, M., Matsuura, S., ... Tsuda, Y. (2019). The surface composition of asteroid 162173 Ryugu from Hayabusa2 near-infrared spectroscopy. *Science*, 364(6437), 272–275. doi: 10.1126/science.aav7432
- Lowry, S. C., Fitzsimmons, A., Pravec, P., Vokrouhlický, D., Boehnhardt, H., Taylor, P. A., ... Kusnirák, P. (2007). Direct detection of the asteroidal YORP effect. *Science*, 316(5822), 272–274. doi: 10.1126/science.1139040
- Lowry, S. C., Weissman, P. R., Duddy, S. R., Rozitis, B., Fitzsimmons, A., Green, S. F., ... van Oers, P. (2014). The internal structure of asteroid (25143) Itokawa as revealed

- by detection of YORP spin-up. *Astronomy & Astrophysics*, 562, A48. Retrieved from <https://doi.org/10.1051/0004-6361/201322602> doi: 10.1051/0004-6361/201322602
- Michel, P., Ballouz, R.-L., Barnouin, O. S., Jutzi, M., Walsh, K. J., May, B. H., ... Lauretta, D. S. (2020, dec). Collisional formation of top-shaped asteroids and implications for the origins of Ryugu and Bennu. *Nature Communications*, 11(1), 2655. Retrieved from <http://www.nature.com/articles/s41467-020-16433-z> doi: 10.1038/s41467-020-16433-z
- Michikami, T., Honda, C., Miyamoto, H., Hirabayashi, M., Hagermann, A., Irie, T., ... Sugita, S. (2019). Boulder size and shape distributions on asteroid Ryugu. *Icarus*, 331, 179–191. doi: 10.1016/j.icarus.2019.05.019
- Morota, T., Sugita, S., Cho, Y., Kanamaru, M., Tatsumi, E., Sakatani, N., ... Tsuda, Y. (2020). Sample collection from asteroid (162173) Ryugu by Hayabusa2: Implications for surface evolution. *Science*, 368(6491), 654–659. doi: 10.1126/science.aaz6306
- Mysen, E. (2006). Canonical rotation variables and non-Hamiltonian forces: Solar radiation pressure effects on asteroid rotation. *Monthly Notices of the Royal Astronomical Society*, 372(3), 1345–1350. doi: 10.1111/j.1365-2966.2006.10944.x
- Mysen, E. (2008). *Dynamical effects of thermal emission on asteroids* (Vol. 383) (No. 1). doi: 10.1111/j.1745-3933.2007.00405.x
- Noguchi, R., Hirata, N., Hirata, N., Shimaki, Y., Nishikawa, N., Tanaka, S., ... Watanabe, S.-i. (2021). Crater depth-to-diameter ratios on asteroid 162173 Ryugu d/D of craters on Ryugu. *Icarus*, 354, 114016. Retrieved from <http://www.sciencedirect.com/science/article/pii/S0019103520303791> doi: <https://doi.org/10.1016/j.icarus.2020.114016>
- Nolan, M. C., Howell, E. S., Scheeres, D. J., McMahon, J. W., Golubov, O., Hergenrother, C. W., ... Lauretta, D. S. (2019). Detection of Rotational Acceleration of Bennu Using HST Light Curve Observations. *Geophysical Research Letters*, 46(4), 1956–1962. doi: 10.1029/2018GL080658
- Okada, T., Fukuhara, T., Tanaka, S., Taguchi, M., Arai, T., Senshu, H., ... Tsuda, Y. (2020). Highly porous nature of a primitive asteroid revealed by thermal imaging. *Nature*, 579(7800), 518–522. doi: 10.1038/s41586-020-2102-6
- Rozitis, B., & Green, S. F. (2011). Directional characteristics of thermal-infrared beaming from atmosphereless planetary surfaces - a new thermophysical model. *Monthly Notices*

- of the *Royal Astronomical Society*, 415(3), 2042–2062. doi: 10.1111/j.1365-2966.2011.18718.x
- Rozitis, B., & Green, S. F. (2012). The influence of rough surface thermal-infrared beaming on the Yarkovsky and YORP effects. *Monthly Notices of the Royal Astronomical Society*, 423(1), 367–388. doi: 10.1111/j.1365-2966.2012.20882.x
- Rubincam, D. P. (2000). Radiative Spin-up and Spin-down of Small Asteroids. *Icarus*, 148(1), 2–11. doi: 10.1006/icar.2000.6485
- Scheeres, D. J. (2007). The dynamical evolution of uniformly rotating asteroids subject to YORP. *Icarus*, 188(2), 430–450. doi: 10.1016/j.icarus.2006.12.015
- Scheeres, D. J. (2015). Landslides and Mass shedding on spinning spheroidal asteroids. *Icarus*, 247, 1–17. doi: 10.1016/j.icarus.2014.09.017
- Scheeres, D. J., Ostro, S. J., Werner, R. A., Asphaug, E., & Hudson, R. S. (2000). Effects of Gravitational Interactions on Asteroid Spin States. *Icarus*, 147(1), 106–118. doi: 10.1006/icar.2000.6443
- Ševeček, P., Golubov, O., Scheeres, D. J., & Krugly, Y. N. (2016, aug). Obliquity dependence of the tangential YORP. *Astronomy & Astrophysics*, 592, A115. Retrieved from <http://www.aanda.org/10.1051/0004-6361/201628746> doi: 10.1051/0004-6361/201628746
- Shimaki, Y., Senshu, H., Sakatani, N., Okada, T., Fukuhara, T., Tanaka, S., ... ichiro Watanabe, S. (2020). Thermophysical properties of the surface of asteroid 162173 Ryugu: Infrared observations and thermal inertia mapping. *Icarus*, 348. doi: 10.1016/j.icarus.2020.113835
- Statler, T. S. (2009). Extreme sensitivity of the YORP effect to small-scale topography. *Icarus*, 202(2), 502–513. doi: 10.1016/j.icarus.2009.03.003
- Sugita, S., Honda, R., Morota, T., Kameda, S., Sawada, H., Tatsumi, E., ... Tsuda, Y. (2019, mar). The geomorphology, color, and thermal properties of Ryugu: Implications for parent-body processes. *Science*, 364(6437), eaaw0422. Retrieved from <https://www.sciencemag.org/lookup/doi/10.1126/science.aaw0422> doi: 10.1126/science.aaw0422
- Szeliski, R. (2011). Computer vision: algorithms and applications. *Choice Reviews Online*, 48(09), 48–5140–48–5140. doi: 10.5860/choice.48-5140
- Tachibana, S., Abe, M., Arakawa, M., Fujimoto, M., Iijima, Y., Ishiguro, M., ... Kuninaka, H. (2014). Hayabusa2: Scientific importance of samples returned from C-type near-

- Earth asteroid (162173) 1999 JU3. *Geochemical Journal*, 48(6), 571–581. doi: 10.2343/geochemj.2.0350
- Takita, J., Senshu, H., & Tanaka, S. (2017). *Feasibility and Accuracy of Thermophysical Estimation of Asteroid 162173 Ryugu (1999 JU3) from the Hayabusa2 Thermal Infrared Imager* (Vol. 208) (No. 1-4). doi: 10.1007/s11214-017-0336-x
- Tatsumi, E., Domingue, D., Schröder, S., Yokota, Y., Kuroda, D., Ishiguro, M., . . . Sugita, S. (2020). Global photometric properties of (162173) Ryugu. *Astronomy and Astrophysics*. doi: 10.1051/0004-6361/201937096
- Tatsumi, E., & Sugita, S. (2018). Cratering efficiency on coarse-grain targets: Implications for the dynamical evolution of asteroid 25143 Itokawa. *Icarus*. doi: 10.1016/j.icarus.2017.09.004
- Taylor, P. A., Margot, J. L., Vokrouhlický, D., Scheeres, D. J., Pravec, P., Lowry, S. C., . . . Magri, C. (2007). Spin rate of asteroid (54509) 2000 PH5 increasing due to the YORP effect. *Science*, 316(5822), 274–277. doi: 10.1126/science.1139038
- Tsuda, Y., Yoshikawa, M., Saiki, T., Nakazawa, S., & ichiro Watanabe, S. (2019). Hayabusa2 Sample return and kinetic impact mission to near-earth asteroid Ryugu. *Acta Astronautica*, 156, 387–393. doi: 10.1016/j.actaastro.2018.01.030
- Vokrouhlický, D., & Čapek, D. (2002). Yorp-induced long-term evolution of the spin state of small asteroids and meteoroids: Rubincam’s approximation. *Icarus*, 159(2), 449–467. doi: 10.1006/icar.2002.6918
- Watanabe, S., Hirabayashi, M., Hirata, N., Hirata, N., Noguchi, R., Shimaki, Y., . . . Tsuda, Y. (2019). Hayabusa2 arrives at the carbonaceous asteroid 162173 Ryugu-A spinning top-shaped rubble pile. *Science*, 364(6437), 268–272. doi: 10.1126/science.aav8032
- Watanabe, S., Tsuda, Y., Yoshikawa, M., Tanaka, S., Saiki, T., & Nakazawa, S. (2017). *Hayabusa2 Mission Overview* (Vol. 208) (No. 1-4). doi: 10.1007/s11214-017-0377-1
- Ďurech, J., Vokrouhlický, D., Baransky, A. R., Breiter, S., Burkhonov, O. A., Cooney, W., . . . Warner, B. D. (2012). Analysis of the rotation period of asteroids (1865) Cerberus, (2100) Ra-Shalom, and (3103) Eger-search for the YORP effect. *Astronomy and Astrophysics*. doi: 10.1051/0004-6361/201219396
- Ďurech, J., Vokrouhlický, D., Kaasalainen, M., Higgins, D., Krugly, Y. N., Gaftonyuk, N. M., . . . Dyvig, R. R. (2008, oct). Detection of the YORP effect in asteroid (1620) Geographos. *Astronomy and Astrophysics*, 489(2), L25–L28. Retrieved from <http://www.aanda.org/10.1051/0004-6361:200810672> doi: 10.1051/0004-6361:

200810672

- Ďurech, J., Vokrouhlický, D., Kaasalainen, M., Weissman, P., Lowry, S. C., Beshore, E., . . . Kitazato, K. (2008, sep). New photometric observations of asteroids (1862) Apollo and (25143) Itokawa - An analysis of YORP effect. *Astronomy and Astrophysics*, *488*(1), 345–350. Retrieved from <http://www.aanda.org/10.1051/0004-6361:200809663> doi: 10.1051/0004-6361:200809663
- Ďurech, J., Vokrouhlický, D., Pravec, P., Hanuš, J., Farnocchia, D., Krugly, Y. N., . . . Warner, B. D. (2018, jan). YORP and Yarkovsky effects in asteroids (1685) Toro, (2100) Ra-Shalom, (3103) Eger, and (161989) Cacus. *Astronomy & Astrophysics*, *609*, A86. Retrieved from <https://www.aanda.org/10.1051/0004-6361/201731465> doi: 10.1051/0004-6361/201731465