

1 **Supporting Information for**
 2 **“SERMeQ model produces realistic retreat of 155 Greenland out-**
 3 **let glaciers”**

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8 **Contents**

- 9 1. Text S1 to S6
 10 2. Figures S1 to S6

11 **Additional Supporting Information (Files uploaded separately)**

- 12 1. Table S1, a list of all Greenland outlet glaciers in the MEaSUREs dataset with
 13 their glacier ID number, name(s), optimal yield strength found, and notes on
 14 inclusion in the analysis. The note “Flagged for bad flowline trace” indicates
 15 glaciers that required manual intervention to complete data processing, but
 16 which are now included in the analysis.

17 **Introduction**

18 **Text S1. Ice dynamics in SERMeQ**

The ice dynamics in our model are based on a perfectly-plastic limiting case of a viscoplastic rheology (Bassis & Ultee, 2019). This rheology describes a glacier with two characteristic timescales: viscous deformation (slow) and mass loss by calving (fast). Modifications to the simple plastic formulation allow calving at a grounded ice-water interface (Ultee & Bassis, 2016) and interaction between multiple tributary glaciers (Ultee & Bassis, 2017). By requiring instantaneous stress balance across the glacier terminus, this formulation finds that the ice thickness H_{terminus} at a given terminus position, in water of depth D , is limited by the yield strength and cannot exceed the yield thickness,

$$H_y = 2 \frac{\tau_y}{\rho_i g} + \sqrt{\frac{\rho_w}{\rho_i} D^2 + 2 \frac{\tau_y}{\rho_i g}}, \quad (\text{S1})$$

19 with τ_y the yield strength of glacier ice, $\rho_i = 920 \text{ kg m}^{-3}$ the density of glacier ice,
 20 $\rho_w = 1020 \text{ kg m}^{-3}$ the density of seawater, and $g = 9.81 \text{ m s}^{-2}$ the acceleration due
 21 to gravity (Ultee & Bassis, 2016).

In a perfectly plastic glacier (Nye, 1951), the upstream ice thickness H along a central flowline, with along-flow direction x and ice surface elevation s , is also controlled by the yield strength:

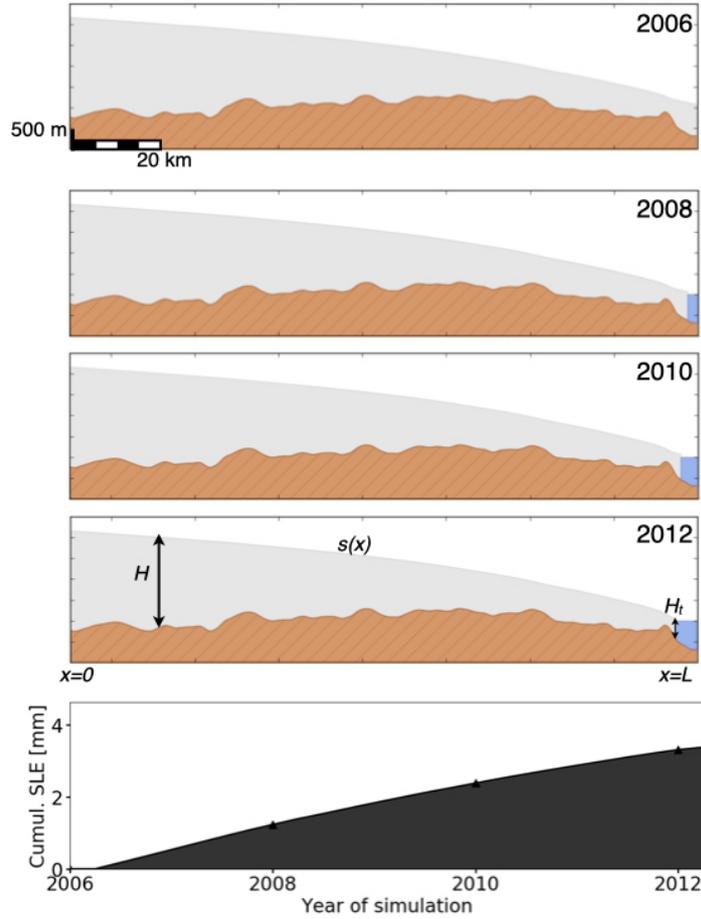
$$H \frac{\partial s}{\partial x} = \frac{\tau_y}{\rho_i g}. \quad (\text{S2})$$

22 This approximation corresponds to a case where the glacier bed is (nearly) plastic
 23 and the glacier stress balance is dominated by shear at the glacier bed and valley
 24 walls—appropriate for most Greenland outlet glaciers. We also account for longitudinal

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25 stresses in a boundary layer near the terminus, where they are more likely to be
 26 important (Bassis & Ultee, 2019).

27 Finally, we use mass continuity to derive an expression for the rate of terminus
 28 advance or retreat due to calving (see Text S2, below). With each change in terminus
 29 position, we calculate a new surface profile according to Equations S1-S2, and we
 30 integrate the changes in ice volume above buoyancy throughout the catchment to
 31 deduce a contribution to global mean sea level. Figure S1 shows an example sequence
 32 of glacier profiles and corresponding sea level contribution as calculated by SERMeQ.



33 **Figure S1.** Surface profiles produced by SERMeQ along a flowline in the central part of Ser-
 34 meq Kujalleq’s catchment, with corresponding cumulative sea level contribution (SLE) below.
 35 Profiles show glacier ice in grey, bedrock in brown, and fjord water in blue. Spatial scale is in-
 36 dicated on the 2006 panel and consistent throughout. Labels on 2012 panel indicate along-flow
 37 direction x , ice surface elevation $s(x)$, ice thickness H , terminus ice thickness H_t , and terminus
 38 location $x=L$ as used in Equations S1-S6. Cumulative SLE on bottom panel reflects catchment-
 39 integrated loss of ice volume above buoyancy converted to an equivalent volume of seawater and
 40 distributed over the area of the global ocean.

41 Despite the simplicity of the model, preliminary experiments have shown promise
 42 in reproducing both surface elevation profiles and advance/retreat rates of glaciers in
 43 Alaska and Greenland (Ultee & Bassis, 2016, 2017). However, our model only applies to
 44 grounded glaciers and cannot simulate the dynamics of floating ice tongues or shelves.

45 **Text S2. Time evolution of the terminus position**

46 Glacier terminus position in SERMeQ evolves in response to near-terminus stretching,
 47 bedrock topography, and changes in catchment-wide surface mass balance as
 48 described in Ultee (2018) and Bassis and Ultee (2019). Below is a brief summary
 49 derivation of the terminus evolution condition as implemented in SERMeQ code.

50 Let $x = 0$ represent the ice divide and $x = L$ the terminus, where $L = L(t)$ is the
 51 length of the glacier (labelled in Figure S1). The time derivative dL/dt then represents
 52 the change in terminus position over time.

Taking the material derivative of the terminus ice thickness $H = H_y$ (constrained
 by Equation S1), we find

$$\begin{aligned} \left. \frac{DH}{Dt} \right|_{x=L} &= \left. \frac{DH_y}{Dt} \right|_{x=L} \\ \left[\frac{\partial H}{\partial t} + \frac{dL}{dt} \frac{\partial H}{\partial x} \right]_{x=L} &= \frac{\partial H_y}{\partial t} + \frac{dL}{dt} \frac{\partial H_y}{\partial x} \\ \left. \frac{\partial H}{\partial t} \right|_{x=L} &= \frac{dL}{dt} \left[\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x} \right]_{x=L}. \end{aligned} \quad (\text{S3})$$

Mass continuity requires

$$\frac{\partial H}{\partial t} + \frac{\partial}{\partial x}(HU) = \dot{a} \quad (\text{S4})$$

53 where $H = H(x, t)$ is the ice thickness, $U = U(x, t)$ the ice velocity, and $\dot{a} = \dot{a}(x, t)$
 54 the net ice accumulation rate, for all (x, t) .

Substituting equation (S4) into (S3), we find

$$\dot{a} - H \frac{\partial U}{\partial x} - U \frac{\partial H}{\partial x} = \frac{dL}{dt} \left[\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x} \right]_{x=L} \quad (\text{S5})$$

$$\frac{dL}{dt} = \frac{\dot{a} - H \frac{\partial U}{\partial x} - U \frac{\partial H}{\partial x}}{\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x}}, \quad (\text{S6})$$

55 with all terms of equation (S6) evaluated at $x = L$, the terminus of the glacier (compare
 56 with Equation 54 of Bassis and Ultee (2019)). With the exception of ice accumulation
 57 rate \dot{a} , all terms are determined by the rheology of ice.

Upstream from the terminus, we assume a plastic yielding layer at the bed of the
 glacier. A perfectly plastic glacier would have a rigid ice plug above the yielding layer,
 but the perfect plastic approximation is a limiting case of several other rheologies that
 could be used to describe the slow deformation of ice in a pseudo-plug (e.g. Balmforth
 et al., 2006). Here we choose to describe the slow deformation of intact ice with
 the familiar Glen’s flow law. At the terminus, as in Ultee and Bassis (2016, 2017),
 we require a vertical yield surface to describe the more rapid motion of fractured,
 disarticulated ice as it calves away from the intact glacier. This implies that the
 effective stress in a region of length δ upstream from the terminus is within ϵ of the
 yield strength τ_y . Near the terminus, we have

$$\begin{aligned} \frac{\partial U}{\partial x} &= \dot{\epsilon}_{xx} = A\tau_{xx}^n \\ &= A\tau_y^n, \end{aligned} \quad (\text{S7})$$

58 where flow law exponent $n = 3$ and A is the flow rate parameter of Glen’s flow law.

We integrate equation (S4) in x to find

$$\int_0^L \frac{\partial H}{\partial t} dx + (HU)|_{x=L} = \int_0^L \dot{a} dx \quad (\text{S8})$$

$$U(x=L) = \frac{1}{H_{\text{terminus}}} \int_0^L \left[\dot{a} - \frac{\partial H}{\partial t} \right] dx, \quad (\text{S9})$$

and by the chain rule $\frac{\partial H}{\partial t} = \frac{\partial H}{\partial L} \frac{dL}{dt}$. Separating the integral in equation (S9) and expanding $\frac{\partial H}{\partial t}$ gives

$$U(x=L) = \frac{\dot{\alpha}L}{H_{\text{terminus}}} - \frac{dL}{dt} \frac{1}{H_{\text{terminus}}} \int_0^L \frac{\partial H}{\partial L} dx, \quad (\text{S10})$$

59 where $\dot{\alpha} = \frac{1}{L} \int_0^L \dot{a} dx$ is the spatially-averaged ice accumulation rate along the flowline.

We now substitute our expressions (S7, S10) in to equation (S4) and rearrange to find

$$\frac{dL}{dt} = \frac{\dot{a} - A\tau_y^3 H_{\text{terminus}} + \frac{\dot{\alpha}L}{H_{\text{terminus}}} \frac{\partial H}{\partial x}}{\frac{\partial H_y}{\partial x} - \frac{\partial H}{\partial x} \left(1 - \frac{1}{H_{\text{terminus}}} \int_0^L \frac{\partial H}{\partial L} \right)}. \quad (\text{S11})$$

60 We implement a discretized version of Equation S11 to describe the time evolution
61 of glacier terminus position in SERMeQ.

62 **Text S3. The role of adjustable parameters**

63 **Yield strength τ_y**

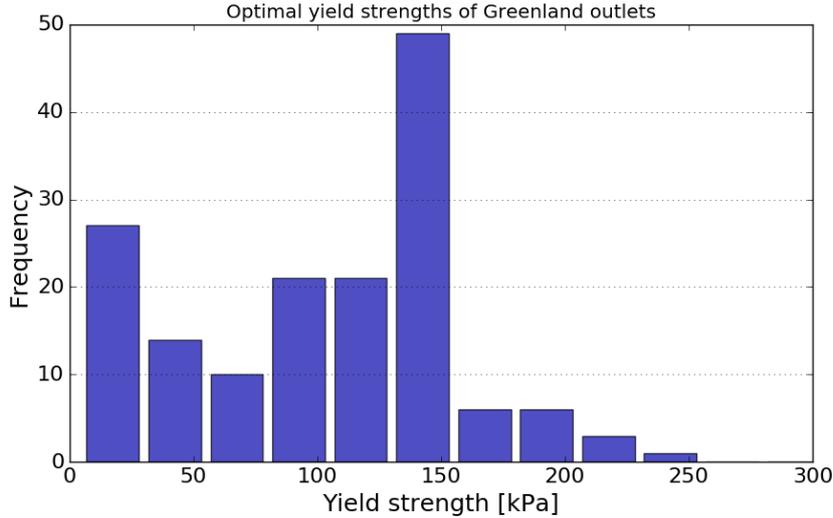
64 For each glacier, we optimize the yield strength τ_y to find the best fit between
65 a reconstructed and observed centerline surface elevation profile. Glaciers with flat-
66 ter surface slopes, including those close to flotation, are best fit by lower values of
67 τ_y . Steeper surface slopes are better fit by higher values of the yield strength. The
68 optimization procedure is discussed in more detail in Ultee and Bassis (2016). The
69 optimal value of τ_y found for each glacier is listed in Supplementary Table 1. There
70 is no correlation between optimal yield strength and glacier latitude, and no other
71 spatial pattern is evident.

72 Figure S2 shows a histogram of the best-fit values of τ_y obtained for the Greenland
73 outlets we simulated. A central peak in the distribution shows that approximately 1/3
74 of the glaciers we simulate have an optimal yield strength between 125 kPa and 150
75 kPa. A smaller peak shows that there are also several glaciers in our set best fit by
76 yield strengths between 5 kPa-25 kPa.
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78 In this work, we have used a single value of τ_y at both the ice-bed interface
79 and the calving front. It is plausible that the ice-bed interface could be deforming
80 more readily than the pure ice at the calving front, for example if the glacier bed is
81 composed of saturated marine sediments or if the ice is very close to flotation. Such a
82 case would lead to low ice surface slopes and a low optimal value of τ_y , even though
83 pure ice throughout the glacier may be stronger. We discuss the case of $\tau_{\text{bed}} < \tau_{\text{ice}}$ in
84 Bassis and Ultee (2019).

85 **Ice temperature T**

86 The ice temperature T is used to select an appropriate value of the flow-rate
87 parameter A in Glen's flow law. Here, we use an ice temperature constant in space
88 and time and do not optimize for its value. In our previous work, we have found that
89 warmer ice ($T = -2^\circ \text{C}$) is softer and more prone to rapid retreat. Conversely, colder
90 ice ($T = -30^\circ \text{C}$) is stiffer and retreats more slowly. For more details, we refer the
91 interested reader to Ultee (2018).



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Figure S2. Histogram of optimal yield strength value found for each glacier.

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Text S4. Inclusion of submarine melt

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We do not explicitly simulate loss of ice from glacier termini by submarine melting. Rather, we have constructed an upper-bound estimate of retreat that is consistent with high submarine melt rates. Our requirement that effective stress near the glacier terminus must equal the yield strength of ice (see Text S1) makes an implicit constraint on the submarine melt rate, because the rate of submarine melt shapes the stress field near glacier termini (Ma, 2018; Ma & Bassis, 2019). There are three cases to consider:

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Case I The submarine melt rate is very small compared with the terminus velocity, $u_s \ll u_t$. In this case, the terminus would be able to advance and thin episodically. However, advance and thinning would lower the effective stress at the glacier terminus, such that it would fall below the yield strength of ice and no longer satisfy our criterion. We therefore disallow Case I.

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Case II The submarine melt rate is comparable to the terminus velocity, $u_s \sim u_t$. In this case submarine melt would balance the tendency of ice near the terminus to stretch and thin, maintaining the terminus ice thickness at the yield thickness.

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Case III The submarine melt rate is very large compared with the terminus velocity, $u_s \gg u_t$. In this case, the erosion of the terminus by high submarine melt would create an overhang and promote calving (Ma & Bassis, 2019). Considered at long enough time scales, e.g. the 0.25 annum standard time step in SERMeQ rather than the hours to days considered in finer-scale process models, high submarine melting and enhanced calving would also maintain the terminus ice thickness at the yield thickness.

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Both Cases II and III are consistent with our assumption that there is a yielding boundary layer at the glacier front that constrains the terminus ice thickness (see Bassis & Ultee, 2019). The maximum rate of length change computed in Equation 1 is compatible with both cases, and the ice mass lost in each time step can be considered a combination of mass lost to calving and to submarine melting.

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The upper-bound retreat rate that we have sought in this work does not require explicit simulation of the submarine melt rate. Nevertheless, future adaptations of



136 **Figure S3.** Network of flowlines on Kangerlussuaq Glacier, MEaSUREs Glacier ID 153, as
 137 defined with our tracing and filtering algorithm.

121 our method to simulate calving in larger-scale models may seek to add a mechanism
 122 for forcing by time-varying submarine melt. We suggest that those efforts begin by
 123 allowing submarine melt rate u_s to modify the terminus velocity, U in Equation 1,
 124 with the understanding that doing so may introduce scenarios that are incompatible
 125 with our original assumptions.

126 **Text S5. Flowline network selection**

127 We apply our depth-integrated, width-averaged model on a network of interacting
 128 glacier flowlines, as described in Ultee and Bassis (2017). Previous applications have
 129 used flowlines selected by hand (Ultee & Bassis, 2016; Ultee, 2018) or by an automated
 130 method that detects valley walls of mountain glacier networks (Kienholz et al., 2014;
 131 Ultee & Bassis, 2017). Neither method is suitable for the hundreds of Greenland
 132 outlet glaciers we consider here. It is impractical to select hundreds of flowlines by
 133 hand, and outlets of the Greenland Ice Sheet, unlike mountain glaciers, expand to a
 134 nearly featureless catchment upstream with no valley walls to aid in flowline selection.
 135 We therefore apply a new selection algorithm based on tracing ice surface velocity.

138 We begin with a surface velocity composite covering the entire ice sheet (ENVEO,
 139 2017). For each glacier included in the MEaSUREs dataset (Joughin et al., 2015, up-
 140 dated 2017), we extract all points observed along the 2006 terminus position. We then
 141 trace each point up the surface velocity field until a pre-determined minimum velocity
 142 cutoff (identical for all glaciers); our viscoplastic approximation is most suitable near
 143 the glacier terminus (Ultee & Bassis, 2017; Bassis & Ultee, 2019), so we do not extend
 144 our simulated catchments all the way to the ice divide. Finally, we filter the set of
 145 full-length flowlines so that the most central flowline is defined as the “main trunk”.
 146 The parallel portions of the remaining flowlines are trimmed and network intersec-
 147 tions defined where the angle between flowlines exceeds a threshold value (identical
 148 for all glaciers). The code used in network selection is available in our public GitHub
 149 repository, and an example network is shown in Figure S3.

150 The tracing and filtering of flowlines from surface velocity is prone to error where
 151 the velocity dataset is noisy or includes holes. Errors in flowline tracing generally
 152 become apparent in later data-processing steps, for example if no optimal yield strength

153 value can be found. Networks affected by such errors include the note “Flagged for
154 bad flowline trace” in Table S1.

155 **Text S6. Detailed case studies**

156 As described in the main article text, 40% of terminus positions simulated by
157 SERMeQ fall within the range of observed terminus position for the same year. Be-
158 cause SERMeQ is sensitive to bed topography features (Ultee, 2018) and is forced by
159 climate reanalysis data, model performance will generally be best where those data
160 products are most accurate. The agreement between modelled and observed retreat
161 of Sermeq Kujalleq (glacier ID 3, also called Jakobshavn Isbræ, main text Figure 3c),
162 where bed topography has been especially well examined by previous glaciological
163 studies, illustrates this point.

164 It is our aim to produce an upper bound on outlet glacier retreat and associated
165 mass loss. We demonstrated in Bassis and Ultee (2019) that Equation 1 is a theoretical
166 bound on the rate of calving retreat. Thus, we anticipate that the rate of retreat
167 simulated by SERMeQ will generally exceed the observed rate of retreat. To support
168 future implementation of this calving-rate bound in our model or others, it is important
169 to understand where it does not perform as expected. There are two cases to consider:
170 (1) the retreat rate simulated by SERMeQ is slower than the rate observed, or (2) the
171 retreat rate simulated by SERMeQ far exceeds the rate observed (by a factor of 5 or
172 more). We describe three illustrative examples here.

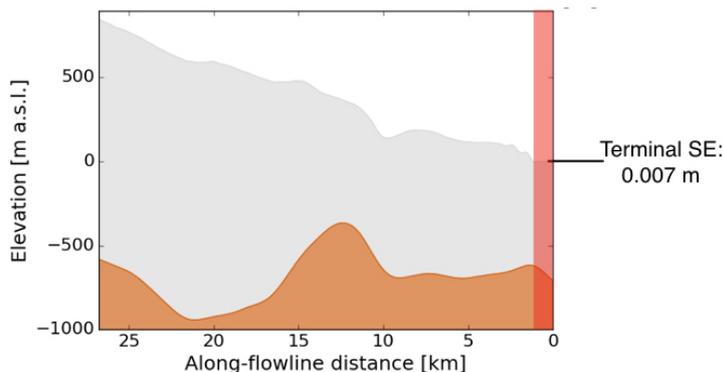
173 **Mean simulated retreat slower than observed**

174 Main text Figure 3a shows the simulated and observed changes in length for
175 Apuseeq Anittangasikkaajuk (MEaSURES Glacier ID 137), a small outlet glacier on
176 the east coast of Greenland. Our analysis shows that the mean rate of simulated
177 (single point) terminus retreat was 31 m/a, while the mean observed rate of retreat
178 of the terminus centroid was 87 m/a. This is one of only a handful of cases in which
179 the mean observed rate over the 2006-2014 period exceeds the supposed upper-bound
180 rate produced by Equation 1. However, in this case both rates are small, and the
181 simulated terminus position remains within the observed range of terminus positions.
182 We also note that Apuseeq Anittangasikkaajuk is seldom included in other studies of
183 Greenland outlets; as such, the quality of bed topography and climate data for this
184 outlet may be relatively lower.

185 **Mean simulated rate far exceeds observed**

186 Main text Figure 3b shows the simulated and observed changes in length for Hel-
187 heim Glacier (MEaSURES Glacier ID 175), a large and well-studied outlet in southeast
188 Greenland. The data quality for this outlet should be comparatively high. Neverthe-
189 less, SERMeQ simulates a mean retreat rate of 1980 m/a, which far exceeds the mean
190 observed retreat rate of 313 m/a. We attribute this rapid retreat to features in the
191 bed topography, combined with the no-flotation condition we have implemented in
192 SERMeQ.

193 The terminus of Helheim Glacier has been observed to float in some years, and
194 was likely floating at the beginning of our simulation period according to bed and
195 surface topography from Morlighem et al. (2017). The glacier bed is more than 600
196 m below sea level and retrograde for several kilometers upstream of the present ter-
197 minus, as shown in Figure S4. As explained in main text section 2 and in Ultee and
198 Bassis (2016, 2017), SERMeQ does not allow floating ice tongues to form. Where
199 small tongues are present, we remove them and simulate the first grounded point as
200 the “terminus”. In the case of Helheim Glacier, when we removed floating ice, the



206 **Figure S4.** Near-terminus bed topography of Helheim Glacier. Brown filled region shows
 207 glacier bed and grey filled region shows glacier ice, both from Morlighem et al. (2017). Note 10:1
 208 exaggeration in vertical scale. A red overlay indicates floating ice that was removed in our simu-
 209 lation. Annotation at figure left indicates the ice surface elevation at the terminus as recorded in
 210 Morlighem et al. (2017), further evidence that the initial terminus could not have been grounded
 211 ice.

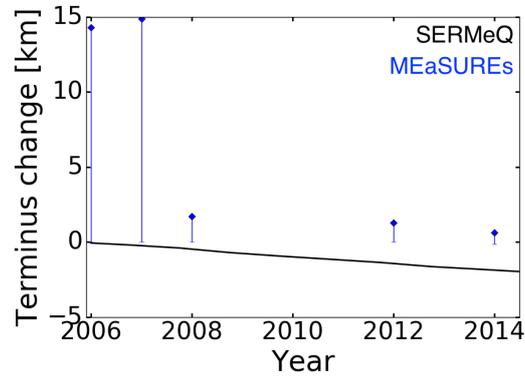
201 simulated terminus was pushed onto the retrograde bed, where it began an unstable
 202 retreat. In summary, the true near-terminus dynamics and stress field of Helheim
 203 Glacier are shaped by the presence of floating ice that interacts with the fjord walls.
 204 SERMeQ does not include these dynamics and therefore simulates an upper-bound
 205 retreat that could occur in the absence of floating ice.

212 Successive under- and over-estimates within observed period

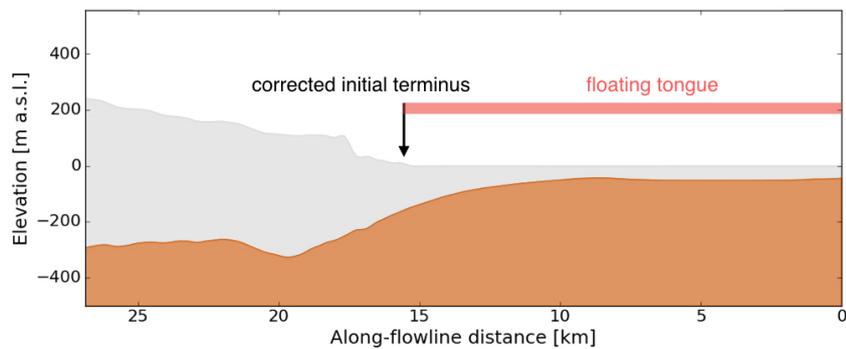
213 In a handful of other cases, the rate of retreat observed during a short period
 214 exceeds the rate simulated during the same period. Underestimated retreat in one
 215 time period is nearly always coupled with overestimated retreat in another period,
 216 such that the aggregate effect over the course of the simulation remains an upper-
 217 bound estimate of net retreat. For example, between 2007 and 2008, the floating ice
 218 tongue of Hagen Brae (MEaSURES Glacier ID 105) disintegrated (Solgaard et al.,
 219 2020). The resulting observed rate of retreat, more than 10 km/a, far exceeded the
 220 rate simulated by SERMeQ (< 1 km/a) over the same period (Figure S4). However,
 221 our model initialization had already removed the floating portion of the glacier as
 222 of 2006, so the SERMeQ-simulated terminus position was still more retreated than
 223 the observed. In the subsequent period between 2008 and 2012, SERMeQ slightly
 224 overestimated the observed retreat rate. Figure S5 illustrates this history. In Figure
 225 S6, we have annotated the floating ice removed upon initialization, the collapse of
 226 which was responsible for anomalously high observed retreat between 2007 and 2008.

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227 **Figure S5.** Observed and simulated change in terminus position on Hagen Brae (glacier ID
 228 105). Black curves indicate SERMeQ-simulated terminus positions, while blue markers indicate
 229 MEaSUREs observations. The blue lines show the most-advanced and most-retreated parts of the
 230 terminus projected onto the centerline, and blue diamonds indicate the centroid of the observed
 231 terminus projected onto the centerline. Positive y-axis values indicate terminus positions more
 232 advanced than the initial position; negative y-axis values indicate terminus positions retreated
 233 from the initial position.



234 **Figure S6.** Near-terminus bed topography of Hagen Brae (glacier ID 105). Brown filled re-
 235 gion shows glacier bed and grey filled region shows glacier ice, both from Morlighem et al. (2017).
 236 Note 10:1 exaggeration in vertical scale. A red bar shows the length of floating ice that was re-
 237 moved during our model initialization, and a black arrow indicates the first grounded point where
 238 SERMeQ could establish an initial terminus.

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