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**Hourly temperature data do not support the views of the Climate Deniers:
Evidence from Barrow Alaska**

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Key Points:

- 1) At NOAA’s Barrow Observatory in Alaska, the annual temperature during 2015-2020 was about 3.37 °C higher than in 1985-1990.
- 2) Virtually all the upward trend in annual temperature through 2015 can be attributed to higher CO₂ concentrations.
- 3) The model’s out-of-sample predictions are more accurate if the estimated associations between CO₂ and temperature are not ignored.

Abstract

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23 Survey evidence has indicated that a significant percentage of the population does not fully
24 embrace the scientific consensus regarding climate change. This paper assesses whether the
25 hourly temperature data support this denial. The analysis examines the relationship between
26 hourly CO₂ concentration levels and temperature using hourly data from the NOAA-operated
27 Barrow observatory in Alaska. At this observatory, the average annual temperature over the
28 2015-2020 period was about 3.37 °C higher than in 1985–1990. A time-series model to explain
29 hourly temperature is formulated using the following explanatory variables: the hourly level of
30 total downward solar irradiance, the CO₂ value lagged by one hour, proxies for the diurnal
31 variation in temperature, proxies for the seasonal temperature variation, and proxies for possible
32 non-anthropomorphic drivers of temperature. The purpose of the time-series approach is to
33 capture the data’s heteroskedastic and autoregressive nature, which would otherwise “mask”
34 CO₂’s “signal” in the data. The model is estimated using hourly data from 1985 through 2015.
35 The results are consistent with the hypothesis that increases in CO₂ concentration levels have
36 nontrivial consequences for hourly temperature. The estimated annual contributions of factors
37 exclusive of CO₂ and downward total solar irradiance are very small. The model was evaluated
38 using out-of-sample hourly data from 1 Jan 2016 through 31 Aug 2017. The model’s out-of-
39 sample hourly temperature predictions are highly accurate, but this accuracy is significantly
40 degraded if the estimated CO₂ effects are ignored. In short, the results are consistent with the
41 scientific consensus on climate change.

Plain Language Summary

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46 According to the IPCC and other scientific organizations, “it is extremely likely that human
47 influence has been the dominant cause of the observed increase in global temperatures since the
48 mid-20th century.” However, a significant percentage of the population does not fully embrace
49 this consensus. Using data from the Barrow Atmospheric Observatory, this paper assesses
50 whether the hourly temperature data support this apparent denial. It is first noted that the
51 average annual temperature at Barrow over the 2015-2020 period was about 3.37 °C higher than
52 in the 1985-1990 period. The formal analysis employs hourly solar irradiance, CO₂, and
53 temperature data. The model controls for possible non-anthropomorphic drivers of annual
54 temperature and other factors. The model was estimated using hourly data over the time interval
55 1 Jan 1985 through 31 Dec 2015. The estimated annual effects of CO₂ are significant in
56 magnitude, while the non-anthropomorphic drivers exclusive of solar irradiance are quantitatively
57 unimportant. The model is evaluated over the 1 Jan 2016 through 31 Aug 2017 time interval.
58 The model’s out-of-sample hourly temperature predictions are highly accurate, but this accuracy
59 is degraded if the estimated CO₂ effects are ignored. In short, the results are consistent with the
60 scientific consensus on climate change.
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Index Terms

6620 Science Policy
1630 Impacts of Global Change
1616 Climate Variability
9315 Arctic Region
3270 Time series analysis
1986 Statistical methods: Inferential

Key Words:

CO₂ Concentrations, Hourly Temperature, Downward total solar irradiance, Climate Change, Arctic Region, Alaska

Acronyms: AMAP, Arctic Monitoring and Assessment Program, ARCH, Autoregressive conditional heteroskedasticity; ARMA, autoregressive–moving-average; ARMAX, autoregressive–moving-average with exogenous inputs; ECMWF, European Centre for Medium-Range Weather Forecasts. MFP, multivariable fractional polynomial; RMSE, root-mean-squared-error.

1. Introduction

According to the IPCC, “It is extremely likely that human influence has been the dominant cause of the observed increase in global temperatures since the mid-20th century “(IPCC, 2013, p. 17). As early as 2001, the science academies of Australia, Belgium, Brazil, Canada, the Caribbean, China, France, Germany, India, Indonesia, Ireland, Italy, Malaysia, New Zealand, Sweden, Turkey, and the United Kingdom all endorsed the IPCC’s Third Assessment ([Australian Academy of Sciences et al., 2001](#)). A more recent list of scientific academies that have accepted this view includes the science academies in Japan, Russia, and the USA. (National Academies of Science, 2005). These institutes are not indicating that human activity is only partly responsible for climate change. Instead, they have indicated that human activity is the dominant driver.

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95 In the United States, a country in which a nontrivial number of climate deniers hold powerful
96 elected positions, a group of 18 highly respected scientific organizations explicitly endorsed the
97 scientific consensus on climate change in a 2009 letter to U.S. policymakers (American
98 Association for the Advancement of Science, 2009). This Letter was released again in 2016 by a
99 larger group of 31 scientific organizations (American Association for the Advancement of Science,
100 2016). The updated Letter makes the following point:

101 “Observations throughout the world make it clear that climate change is
102 occurring, and rigorous scientific research concludes that the greenhouse gases
103 emitted by human activities are the primary driver. This conclusion is based on
104 multiple independent lines of evidence and the vast body of peer-reviewed
105 science.”

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AAAS, 2016

This paper’s starting point is the observation that the survey data does not fully reflect the scientific
consensus. This paper applies methods developed to address issues in economics and finance to
assess whether the temperature data at the Barrow Atmospheric Observatory in northern Alaska
supports this view. While some might sharply question the approach employed in this paper
because the methodology is “unorthodox” relative to the conventional meteorological framework,
it may be worth noting that the methodology applied in this paper has revolutionized the analysis
in other sectors when the data are found to be autoregressive and heteroskedastic in nature. One
modest example of this is Forbes and Zampelli (2019), who analyzed CO₂ emissions from the Irish
power grid using the methods presented in this paper after observing that the emission levels had
autoregressive and heteroskedastic properties. These properties will be shown to be highly
relevant when modeling hourly temperature. Ignoring these properties makes extracting CO₂’s
“signal” from the “noisy” data almost impossible.

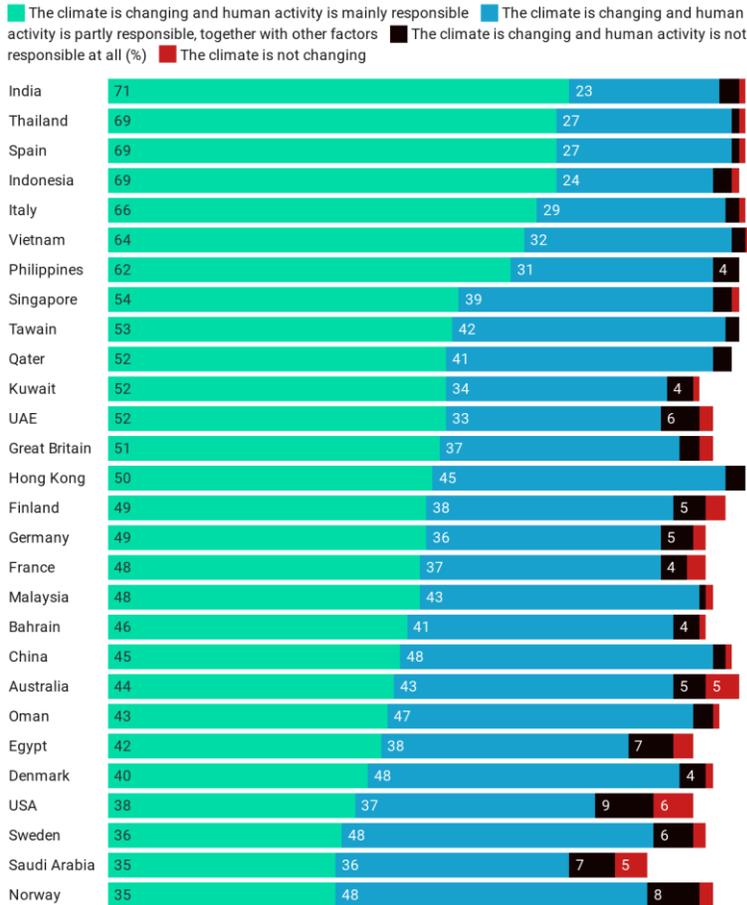
121 In terms of organization, section 2 of the paper discusses the survey data. Section 3
122 summarizes the views of individuals identified as being climate deniers within the scientific
123 community. Section 4 discusses the data used in the analysis. To provide context, the trends in
124 hourly temperature, downward total solar irradiance, and CO₂ concentrations at the Barrow
125 Atmospheric Observatory are reported. In response to an assertion about a lack of recent warming
126 relative to the pre-1940 period by Lindzen (2020, pp. 12-13), the annual temperature at the nearby
127 Barrow Airport from 1921 through 2020 is reported. The time-series nature of hourly temperature
128 at Barrow is also discussed to facilitate the modeling discussion in the remaining sections of the
129 paper. Section 5 introduces a modeling framework to examine the possible association between
130 CO₂ concentrations and hourly temperature. Section 6 discusses the estimation process and also
131 presents the results. Section 7 evaluates the model. The paper's findings are discussed in section
132 8.

133 **2. The Survey Evidence**

134 A 2019 YouGov survey of 30,000 individuals that are believed to be representative of the online
135 population in 28 countries indicated that there were only 14 countries in which 50 % or more of
136 the respondents would agree with the statement that “The climate is changing and human activity
137 is mainly responsible” (Figure 1). A significant number of the respondents indicated that human
138 activity is only partly responsible for climate change. For example, while 40% of the respondents
139 in Denmark agreed with the scientific consensus, 48% agreed with the view that “...human activity
140 is partly responsible, **together with other factors (emphasis added)**. In the United Kingdom,
141 51% endorsed the scientific consensus, while 37% believe that human activity is only partly
142 responsible. In China, 45% endorsed the scientific consensus, while 48% believe human activity
143 is only partly responsible. In the USA, 38% endorsed the scientific consensus, 37% reported that
144 is only partly responsible. In the USA, 38% endorsed the scientific consensus, 37% reported that
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146 they believe that human activity is only partly responsible for climate change, 9% believe that
 147 human activity is not a driver of climate change, and 6% reported that they do not believe that the
 148 climate is changing.

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Created with Datawrapper

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151 Source: [10.5281/zenodo.5833580](https://doi.org/10.5281/zenodo.5833580)

152

153 **Figure 1. Responses to a 2019 YouGov survey question posed to 30,000 people**
 154 **in 28 countries. Thinking about the global environment...In general, which of**
 155 **the following statements, if any, best describes your view?"**

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159 While it is tempting to attribute the findings for China in Figure 1 as evidence of a form of climate
160 denial by a large proportion of its population, the recent findings by Yang et al. (2021) would seem
161 to suggest that a sincere misunderstanding of the nature of climate change might be a more
162 important consideration. In other countries, other survey data are largely consistent with the data
163 presented in Figure 1. For example, in a 2019 Irish Times/Iposos MRBI poll (Leahy, P., 2019),
164 respondents were asked if they agreed with the following statement: “I don’t think climate change
165 will be as bad as some say so I’m not that worried about it.” While 57% of the respondents
166 implicitly endorsed the scientific consensus by disagreeing with the statement, 33% agreed. In
167 this same poll, only 44% of the respondents agreed with the statement, “I am okay with the price
168 of oil, gas, petrol and diesel increasing to help tackle climate change.” This is obviously not a
169 majority and thus represents a challenge to implementing policies to reduce emissions.

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171 A November 2018 survey of 1,202 adults by the Energy Policy Institute at the University of
172 Chicago and the AP-NORC Center yields useful insights (EPIC, 2018). According to this
173 survey, 57% of the respondents were willing to pay a \$1 monthly fee to combat climate change.
174 About 23% were willing to pay 40 USD per month. However, 43 percent were unwilling to pay
175 anything, highlighting the challenge of doing anything significant to reduce emissions.

176 Acceptance of the view that human activity contributes to climate change was a useful indicator
177 of whether respondents were willing to pay to reduce emissions.

178
179 Suggestive of the possible political implications of the polling data, the UNFCCC secretariat
180 (United Nations Framework Convention on Climate Change) issued a report in September 2021
181 that indicated that the combined updated Paris Accord pledges fall short of what it will take to
182 meet the goals of the Paris Accords. Specifically, even with the updated pledges, projected GHG

183 emissions in 2030 are only about 0.5% lower than in 2010, which is far lower than what it would
184 take to limit global warming to below two °C (UNFCCC Secretariat, 2021a). The COP26
185 meetings that were held in November of 2021 have done little to improve the prospects that the
186 goals of the 2015 Paris Accords will be met. The United States did announce its good intentions,
187 but climate deniers will most likely make those goals very difficult to achieve. The conference
188 faced other challenges including objections to phasing out coal. While the conference made
189 progress in the areas of carbon markets and finance, the fact remains that there is a significant
190 emissions gap (UNFCCC Secretariat, 2021b).

191 **3 The Views of the Climate Deniers from within the Scientific Community**

192 Somewhat surprisingly, some prominent individuals from within the scientific community who
193 have been labeled as climate deniers have actually conceded that increases in CO₂ concentrations
194 have consequences for surface warming. For example, the CO₂ Coalition (2015), a sharp critic of
195 the scientific consensus, whose members include the well-known influencers Richard Lindzen,
196 Patrick Michaels, Roy Spence, and William Happer, has explicitly acknowledged the greenhouse
197 effect. It notes that predicting greenhouse-induced warming is difficult because atmospheric
198 processes are very complicated. It then pivots back and reports that it believes that the data
199 suggests that the warming associated with a doubling of CO₂ levels will be very modest. In its
200 words,

201 “Basic physics implies that more atmospheric CO₂ will increase greenhouse
202 warming. However, atmospheric processes are so complicated that the amount of
203 warming cannot be reliably predicted from first principles. Recent observations of
204 the atmosphere and oceans, together with geological history, point to very modest
205 warming, about 1 C (1.8 F) if atmospheric CO₂ levels are doubled.”

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207 CO₂ Coalition, 2015
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209 The CO₂ Coalition's assertion that the warming associated with a doubling of CO₂ will be modest
210 appears to be largely premised on a belief that the recent warming is about the same as before the
211 1940s (Lindzen, 2020, pp. 12-13). As will be seen, this belief is not supported by the data in
212 northern Alaska.

213

214 **4 An Overview of the Changing Climate in Northern Alaska**

215

216 The study employs temperature, solar radiation, and CO₂ data reported by the Barrow (BRW)
217 Atmospheric Observatory. This is one of the baseline observatories of the Earth System Research
218 Laboratory (ESRL), Global Monitoring Division (GMD), of the National Oceanic and
219 Atmospheric Administration (NOAA). It is located near sea level about 8 km east of Utqiagvik
220 (formerly Barrow), Alaska at 71.3230 degrees north and 256.6114 degrees West (Vasel et al.,
221 2020). Continuous atmospheric measurements of CO₂ have been recorded at this observatory since
222 July 1973 (Thoning et al., 2021). Herbert et al. (1986) discuss how the data are processed.
223 Peterson et al. (1986) discuss the first ten years (1973-1982) of operations and report consistency
224 of the Barrow results with the reported data from four neighboring locations. Tans and Thoning
225 (2020) provide a general overview of the methods used to collect and process the CO₂ data at
226 Mauna Loa, one of NOAA's other baseline observatories. Along with the hourly temperature data
227 corresponding to BRW, the CO₂ data for BRW were downloaded using the following link:
228 (<http://www.esrl.noaa.gov/gmd/dv/data/>).

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231 Measurements of downward total solar irradiance have been reported at the BRW observatory
232 since January 1976. Before 1998, the data were reported at three minutes intervals. The data were
233 subsequently reported at one-minute intervals. For this study, the reported values were rolled up

234 to hourly averages. Data were dropped from the analysis if the number of valid minutes of data
235 for an hour was less than 15.

236

237 Consideration was given to the inclusion of CH₄ data in the analysis. This action would have
238 resulted in the loss of 26,381 hourly observations due to unavailable or invalid CH₄ measurements.
239 (the collection of the CH₄ data commenced in 1986 but was subsequently suspended for about nine
240 months in 2012/2013). The probable effect of this data loss on model convergence was an
241 important consideration in excluding this variable from the analysis, model convergence being one
242 of the major challenges of the methodology employed in this paper (STATA, 2021, p. 33). The
243 omission of CH₄ and other variables reflecting greenhouse gas concentrations represents a
244 shortcoming in the analysis.

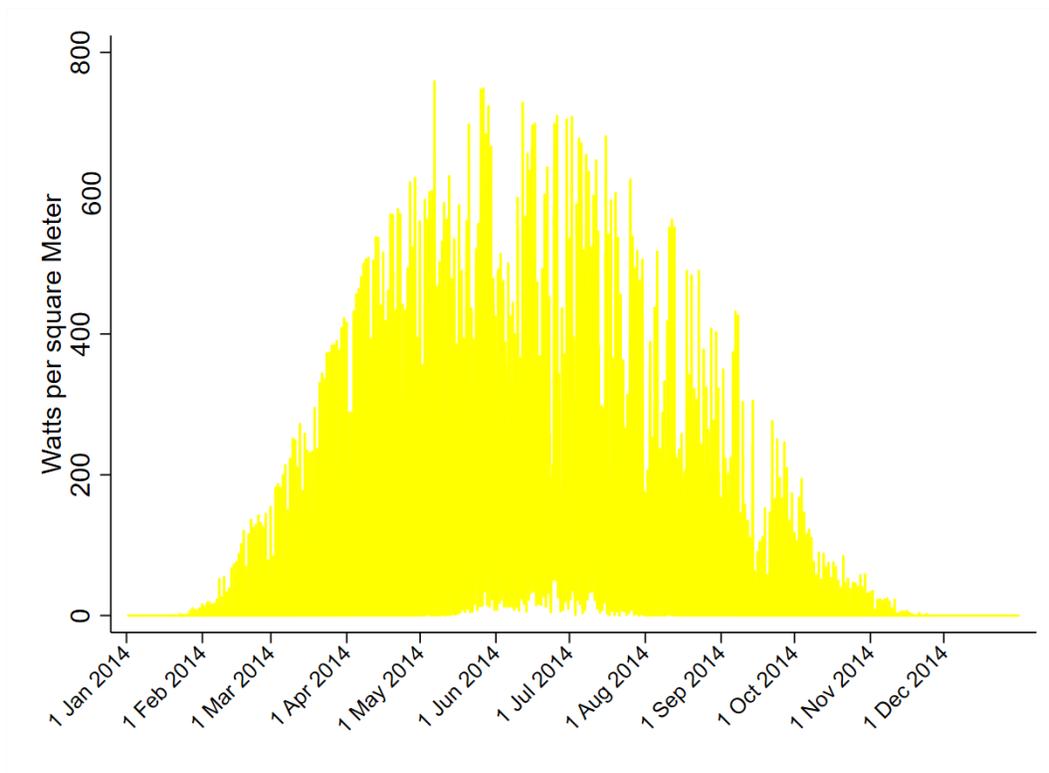
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246 The sample for this study spans from 1 Jan 1985 through 31 Dec 2015. Data before 1 Jan 1985
247 were not employed in this study because the reported downward total solar irradiance data largely
248 did not meet ESRL's standards before that date. For example, only about 31% of the downward
249 total solar irradiance values in 1984 were deemed by ESRL to be valid. The 1 Jan 2016 - 31 Aug
250 2017 time interval is reserved for out-of-sample analysis. The evaluation period terminates on 31
251 Aug 2017 because of a significant data availability issue.

252

253 In thinking about meteorological issues at BRW, it is useful to begin by first noting the
254 extremes and high level of variability in the level of downward total solar irradiance at this
255 location. In terms of variability, the data from 2014 is instructive (Figure 2). Concerning the

256 extremes, there are about 67 days of virtually total darkness each year (about 18 Nov to 22 Jan),
 257 while the sun does not completely set from 11 May to 31 Jul.



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259 **Figure 2.** The level of hourly downward total solar irradiance at BRW, 1 Jan 2014 – 31 Dec
 260 2014

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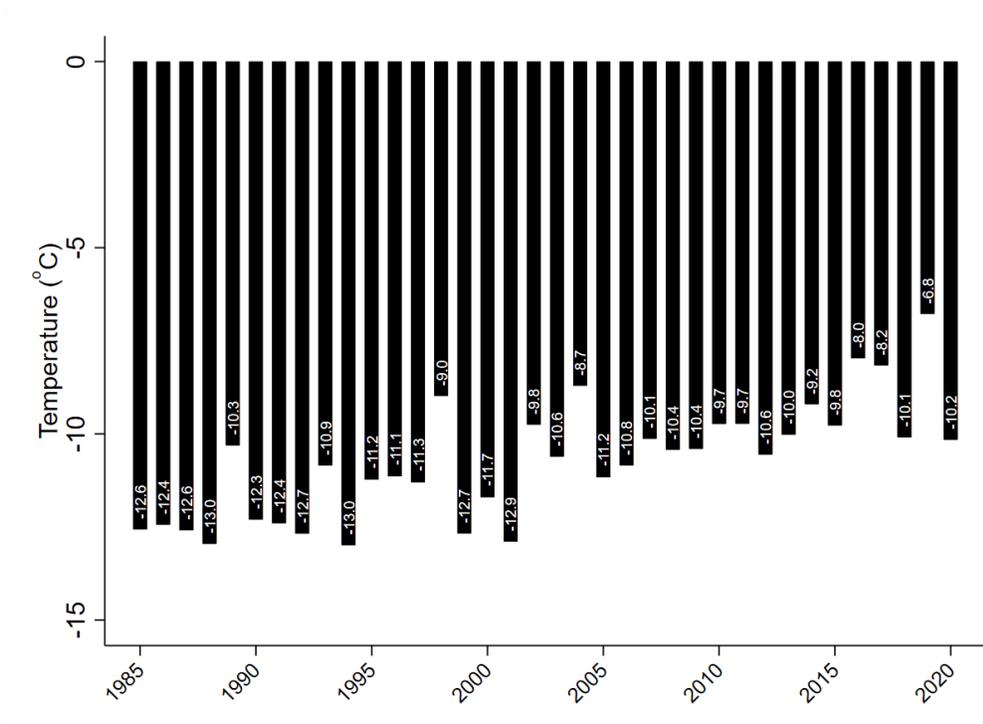
262 The average annual temperature at BRW has increased significantly since 1985 (Figure 3).
 263 Specifically, the average annual temperature over the 2015-2020 time period was about 3.37 °C
 264 higher than in 1985-1990. The temperature data reported by the PABR weather station at the
 265 nearby Barrow Airport from 1985 through 2020 are consistent with the trend at BRW (Figure 4).
 266 The PABR data also indicates that the four warmest years since 1921 occurred in 2016, 2017,
 267 2018, and 2019. In these four years, the average annual temperature was about 5.03 °C higher
 268 than the average annual temperature from 1921 through 1939. These findings do not support the
 269 assertion by Lindzen that the recent warming is about the same as before the 1940s (2020, pp. 12-

270 13). In terms of the magnitudes of the recent warming, the increases are consistent with Arctic
271 amplification, as explained by Pithan & Mauritsen (2014) and Winton (2006).

272 The upward trend in temperature at both BRW and PABR is consistent with the temperature trend
273 for the Arctic noted by Post et al. (2019), Markon et al. (2018, p 1190-1192), and Thoman et al.
274 (2020, p. 4). Box et al. (2019) have reported significant changes in nine key measures of the Arctic
275 climate system over 1971 through 2017. The qualitative story is clear: “the transformation of the
276 Arctic to a warmer, less frozen, and biologically changed region is well underway.” (Thoman et
277 al., 2020, p. 1). Consistent with these changes, the annual mean permafrost temperatures have
278 increased at many locations throughout the Arctic (Romanovsky et al., 2017, p. 69). For example,
279 based on data reported by EPA, the average annual permafrost temperature at the Deadhorse
280 Permafrost Observatory (<https://permafrost.gi.alaska.edu>) over the years 2015 through 2020
281 was about 2.81 °C higher than during the years 1985 through 1990 (EPA, 2021). In four of the 11
282 permafrost observatories whose 2020 annual temperatures are reported by EPA, the 2020 average
283 temperatures were between -1 and 0 °C. There is evidence that thawing has adverse implications
284 for carbon emissions because of stimulated microbial decomposition (Schuur et al., 2021).

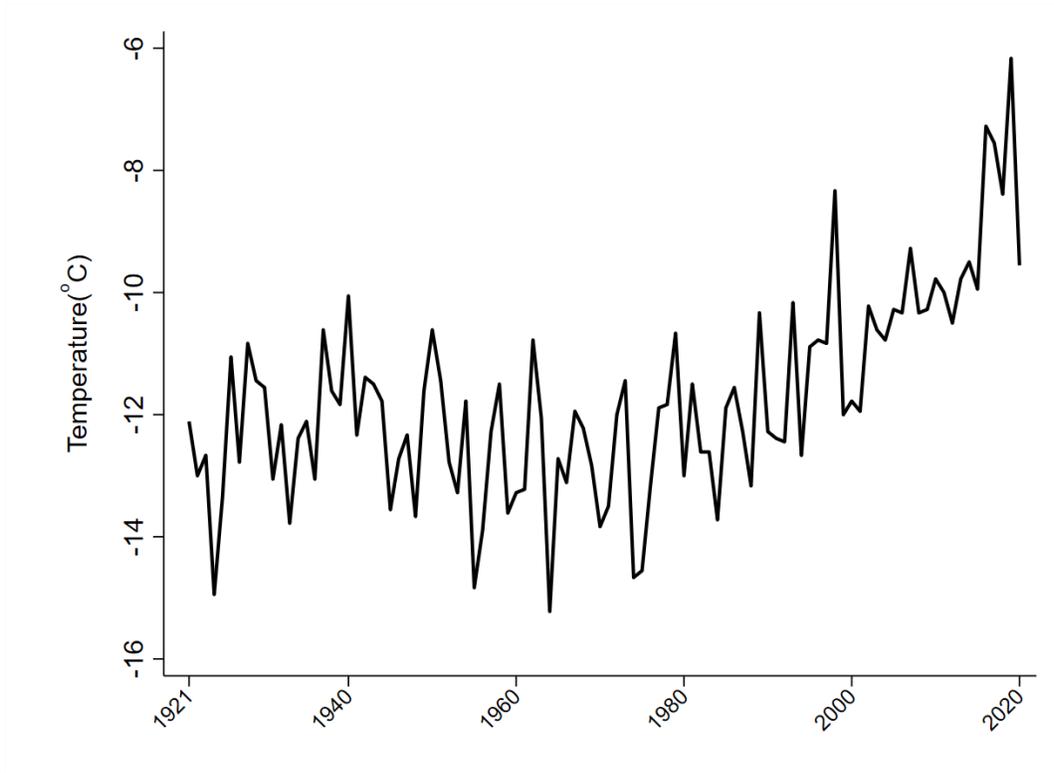
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286 According to AMAP, “Arctic warming can also have effects far beyond the region: for example,
287 the recent rapid warming of the Arctic appears to have created conditions favoring a persistent
288 pattern in the jet stream that provokes unusual extreme temperature events in the Northern
289 Hemisphere.” (AMAP, 2019, p. 4). Taylor et al. (2017, p. 303) have indicated it is very likely that
290 human activities have contributed to these trends. While the literature supports this finding, it has
291 also been suggested that the significant natural weather and climate variability in the Arctic poses
292 an attribution challenge (Taylor et al., 2017, p. 319). Consistent with this reported variability, both

293 downward total solar irradiance and temperature at the hourly level are highly variable (Figures 5
 294 and 6). Concerning the hourly CO₂ concentration levels, there is a significant upward trend in the
 295 hourly CO₂ concentration levels over the sample (Figure 7). Despite the upward trend in both CO₂
 296 concentrations and temperature, there is no visually obvious relationship between the two variables
 297 (Figure 8). While some climate deniers may be tempted to claim that the data in this figure
 298 vindicates their position, the view here is that a lack of correlation between two variables only
 299 rules out causality when the hypothesized relationship is quite simple.



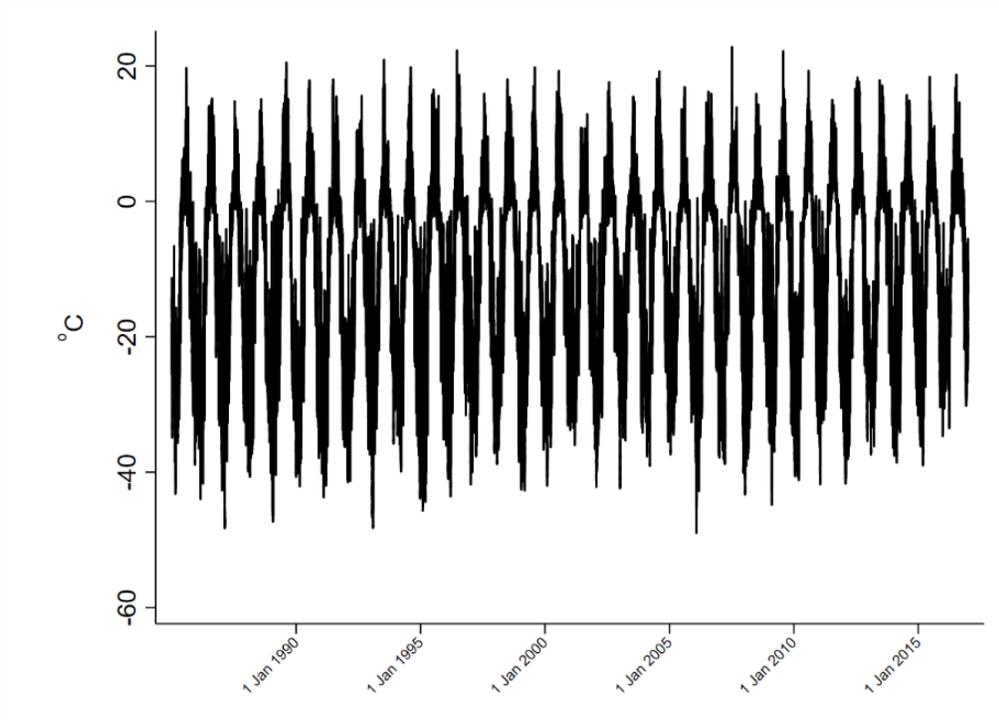
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Figure 3. The average hourly temperature at the Barrow Observatory, 1985 -2020



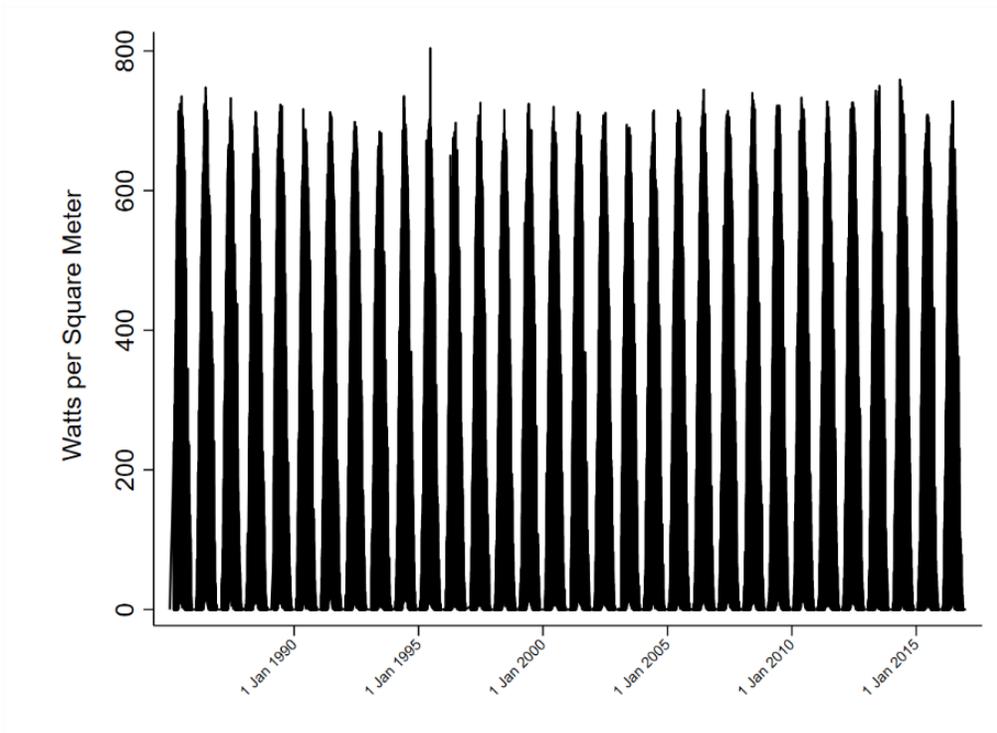
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Figure 4. The average annual temperature at the PABR/Barrow Airport weather station, 1921 - 2020

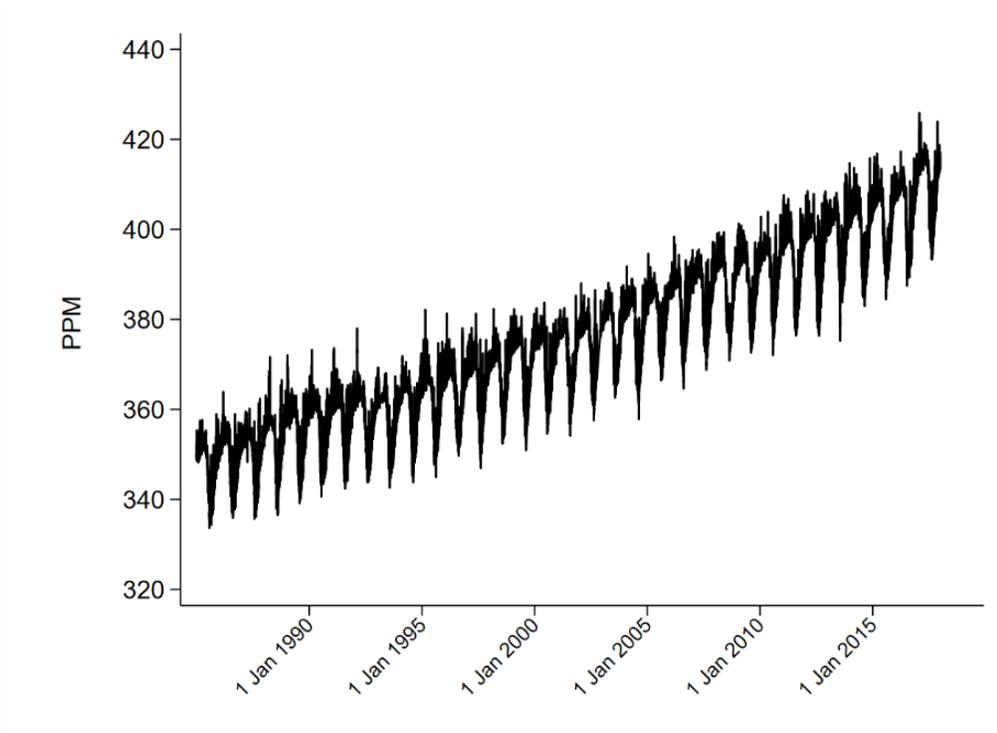


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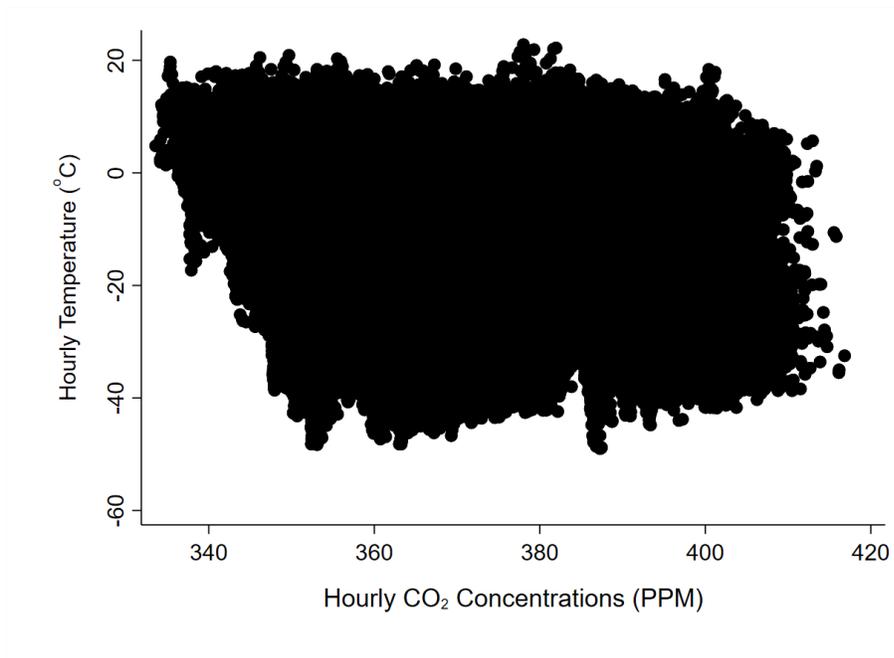
Figure 5. The hourly temperature at the Barrow Observatory, 1 Jan 1985 – 31 Dec 2016



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317 **Figure 6.** Hourly downward total solar irradiance levels at the Barrow Observatory, 1 Jan 1985
318 – 31 Dec 2016



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320 **Figure 7.** Hourly CO₂ concentration levels at the Barrow Observatory, 1985 -2019
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325 **Figure 8.** A scatter diagram of hourly temperature and CO₂ concentration levels at BRW, 1 Jan
326 1985 – 31 Dec 2015

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329 The autocorrelative nature of hourly temperature is an important characteristic of the data (Figure
330 9). As the figure indicates, the magnitude and the duration of the autocorrelative process are
331 significant. In terms of magnitude, the estimated one-hour autocorrelation in temperature equals
332 0.9970, a value that is so large that it is reasonable to wonder if there is a unit root issue. If this is
333 indeed the case, the results of this study could be spurious for the reasons explained by Kennedy (
334 2008, p. 301).

335 Fortunately, an Augmented Dickey-Fuller test yields a *P*-value that is less than 0.0001 both with
336 and without a possible trend, and thus the null hypothesis of a unit root is rejected. Consistent
337 with this finding, the Phillips-Perron test for a unit root also yields a *P*-value less than 0.0001 both
338 with and without a possible trend. Consideration was given to further unit root testing using the
339 DF-GLS test developed by Elliot et al. (1996). This test is regarded as a leading “second-
340 generation” unit root test that avoids some of the shortcomings of the Augmented Dickey-Fuller

341 and Phillips-Perron tests (Baum and Hurn, 2021, pp. 117-120). The application of this
342 methodology requires a data series without any gaps. The Barrow data set has 325 gaps in terms
343 of temperature, and thus, the DF-GLS test cannot be applied.

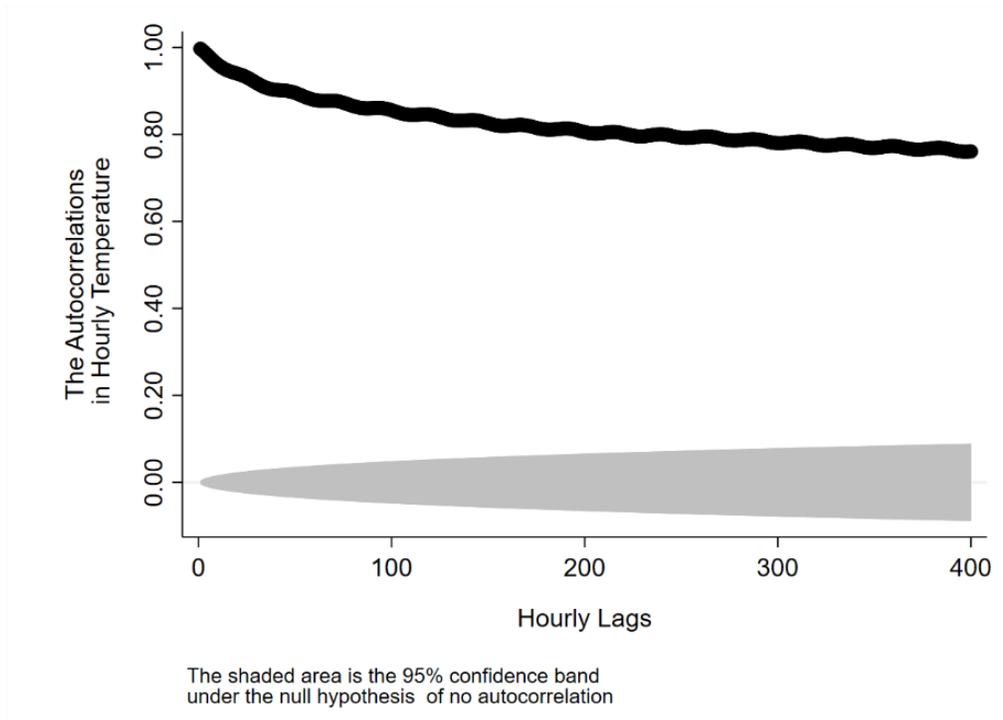
344 Fortunately, hourly temperature data analysis at another observatory in the polar region
345 may be instructive. One of the few stations in the polar region that substantially meets the zero
346 data gap requirements of the DF-GLS test is the Syowa station on East Ongle Island, located about
347 4km from the Antarctic continent with a latitude 69.0125° South and a longitude of 39.5900°
348 East. This station is supported by the National Institute of Polar Research in Japan. The data
349 from this station was obtained from NASA's CERES/ARM Validation Experiment ([https://ceres-](https://ceres-tool.larc.nasa.gov/ord-tool/jsp/SYN1degEd41Selection.jsp)
350 [tool.larc.nasa.gov/ord-tool/jsp/SYN1degEd41Selection.jsp](https://ceres-tool.larc.nasa.gov/ord-tool/jsp/SYN1degEd41Selection.jsp)).

351 From 14 Apr 2002 through 31 Jan 2016, a period with 120,982 hours and no data gaps, the mean
352 temperature at the Syowa Observatory was about -10.7°C , with the hourly values ranging from
353 41.25°C to 7.65°C . At one hour lagged, the autocorrelation in temperature equals 0.9959, a
354 value seemingly suggestive of a unit root issue. This possible suspicion is not supported by the
355 Augmented Dickey-Fuller, Phillips-Perron, or the DF-GLS tests.

356 While the available tests do not support the null hypothesis of a unit root in the hourly
357 temperature data, a quantitative analysis of hourly time-series temperature data needs to control
358 its time-series nature to effectively extract the signal from the noise in the data. The method of
359 ordinary least squares is woefully deficient in this regard. This point is consistent with a warning
360 by Granger and Newbold (1974, p. 117), who note the following: "In our opinion the
361 econometrician can no longer ignore the time series properties of the variables with which he is
362 concerned - except at his [or her] peril." The consequences of ignoring their warning include
363 inefficient estimates of the regression coefficients, suboptimal forecasts, and invalid tests of

364 statistical significance. Unfortunately, an inspection of “Statistical Methods in the Atmospheric
 365 Sciences,” authored by Wilks (2019), suggests that this warning has not been fully heeded in the
 366 atmospheric sciences.

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368

369 **Figure 9.** The autocorrelations in hourly temperature at Barrow, 1 Jan 1985 – 31 Dec 2015

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372 **5 An ARCH/ARMAX Model of Hourly Temperature**

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374 The model employed in this paper is an Autoregressive Conditional Heteroskedasticity/

375 Autoregressive–Moving-Average with Exogenous Inputs model of temperature (henceforth, an

376 ARCH/ARMAX model of temperature). The ARCH terms are employed to model the

377 conditional heteroskedasticity, an important consideration in the convergence process. The

378 Autoregressive–Moving-Average (ARMA) component models the autocorrelations in

379 temperature depicted in Figure 9. In this section, the role of the exogenous inputs is discussed.

380

381 Following from Forbes and St. Cyr (2017, 2019) and Forbes and Zampelli (2019, 2020), the
382 modeling approach employed in this paper accepts the proposition that “All models are wrong;
383 some models are useful” (Box et al., 2005, p. 440). They are all “wrong” because they represent
384 a simplification of reality; they can be useful if important features of that reality are captured. A
385 possibly related proposition that may be relevant during these times of sharp differences in
386 opinions is “that all modeling results can easily be dismissed out of hand as being wrong, even if
387 they are useful.” In the case of this research, it may be asserted that the results are “wrong” because
388 the model is adversely affected by “specification errors,” “multicollinearity,” “autocorrelation,”
389 “heteroskedasticity,” “overfitting,” and “unit-root issues.” Other readers may conclude that the
390 model is “wrong” because it somehow “forces” the estimated relationship between CO₂
391 concentrations and temperature to be positive because both are rising over time (note: the
392 correlation between temperature and CO₂ equals -0.1495). Still, others will argue that the results
393 are “biased” because the model’s dependent variable is the natural logarithm of temperature.

394
395 Following from Forbes and Zampelli (2020, p. 13), this paper accepts the proposition that the
396 “...vulnerability of a model to be deemed as wrong even though all models are “wrong” represents
397 a challenge to the recognition of insights provided by models that are useful.” Fortunately, this
398 challenge can be addressed by assessing a model’s predictive accuracy. Common sense informs
399 us that a model that yields accurate predictions is useful if the evaluation interval is sufficiently
400 long. Based on this perspective, the approach in this paper proceeds by estimating the model using
401 228,085 observations and performing an out-of-sample analysis with 13,175 observations.

402

403 In the model, the association between CO₂ concentrations and temperature is presumed to be
 404 conditional on the level of downward total solar irradiance measured at the Earth's surface,
 405 downward total solar irradiance being the primary driver of the weather and climate system. The
 406 other drivers of the surface energy balance, such as upward and downward longwave irradiance,
 407 are not included as explanatory variables in the model because they are hypothesized to be affected
 408 by CO₂ concentrations. Upward short-wave irradiance is not hypothesized to be directly affected
 409 by CO₂ concentrations. Its inclusion as an explanatory variable is open to question, given that it
 410 is largely driven by downward solar irradiance and temperature. The inclusion of this variable
 411 would significantly reduce the sample size, given that ESRL only commenced reporting this
 412 variable in 1993.

413 In the model, CO₂ concentrations are lagged one hour to avoid the issue of possible two-
 414 way causality between temperature and CO₂ concentrations. The model also includes binary
 415 variables representing the solar zenith angle, the hour-of-the-day, day-of-the-year, and year. These
 416 variables are included as proxies for the drivers of the diurnal variation in temperature, the seasonal
 417 variation in temperature, and the possible non-anthropomorphic drivers of temperature unrelated
 418 to total downward solar irradiance. In terms of functional form, linearity is not presumed. Instead,
 419 the data are permitted to speak for themselves on this important issue.

420

421 The initial version of the model is given by:

$$\begin{aligned}
 422 \text{lnTemp}_t &= \alpha_0 + \alpha_1 \text{ZeroSolar}_t + \alpha_2 \text{Solar}_t + \alpha_3 (\text{CO}_{2,t-1} * \text{ZeroSolar}_t) \\
 423 &+ \alpha_4 (\text{CO}_{2,t-1} * \text{Solar}_t) + \alpha_5 \text{Solar}_t * \text{CO}_{2,t-1} + \sum_{h=1}^9 \beta_h \text{Angle}_h \\
 424 &+ \sum_{i=2}^{24} \phi_i \text{HourOfDay}_i + \sum_{j=2}^{365} \gamma_j \text{DOY}_j + \sum_{k=1985}^{2014} \delta_k \text{Year}_k \quad (1) \\
 425 & \\
 426 & \\
 427 & \\
 428 & \\
 429 &
 \end{aligned}$$

429 Where

430 $\ln\text{Temp}_t$ is the natural logarithm of temperature measured in Kelvin in hour t .

431

432 ZeroSolar_t is a binary variable. The variable is assigned a value of one if the downward total
433 solar irradiance level at Barrow in period t equals zero. Its value equals zero otherwise.

434

435 Solar_t equals the downward total solar irradiance level at Barrow in period t .

436

437 CO2_{t-1} is the atmospheric level of CO_2 concentrations at Barrow in hour $t-1$.

438

439 PosSolar_t is a binary variable that equals one if the level of downward total solar irradiance at
440 Barrow in period t is positive. Its value equals zero otherwise.

441

442 Angle_h is a vector of nine variables representing the solar zenith angle.

443

444 HourOfDay_i is a series of 23 variables representing the hour of the day.

445

446 DOY_j is a series of 364 binary variables representing the day of the year.

447

448 Year_k is a series of 30 binary variables representing the year.

449

450 Please note that α_1 , α_2 , and α_3 , etc. are the coefficients corresponding to this linear version of the

451 model. From (1), the total number of coefficients to be estimated equals 432. Some may strongly

452 suspect that this number of explanatory variables indicates that the model is "overfitted." If this

453 claim is true, the model would be unlikely to yield accurate out-of-sample predictions even if the

454 within-sample explanatory power is very high (Brooks, 2019, p. 271). The "rule of thumb" by

455 Trout (2006) that overfitting is avoided when there are at least ten observations per estimated

456 coefficient does not support this possible suspicion given that the structural model present in this

457 paper entails over 500 observations per estimated coefficient. Moreover, as will be seen, the model

458 does not suffer from the consequences of overfitting in terms of out-of-sample predictive accuracy.

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464 **6 Estimation and Results**

465

466 The model was estimated using hourly data over the 1 Jan 1985 - 31 Dec 2015 time interval. The
467 analysis was conducted in two distinct stages. In the first stage, the functional form given by Eq.
468 (1) was evaluated. A nonlinear functional form was subsequently identified.

469 The analysis also recognizes that the disturbance term's variance in a regression equation is
470 heteroskedastic instead of homoscedastic, i.e., variable instead of constant over time. As
471 suggested in the previous section, the accepted approach involves estimating an ARCH model.
472 This approach was proposed by Engle (1982) to improve the analysis of financial data. It has
473 since proven itself invaluable in modeling any time-series variable in which there are periods of
474 turbulence followed by relative calm at some point. Hourly temperature is one of those
475 variables. Those tempted to claim otherwise are cheerfully invited to consult the book entitled
476 "Environmental Econometrics Using Stata," authored by Baum and Hurn (2021).

477
478 The second estimation stage also recognizes that the temperature in hour t is not statistically
479 independent from the temperature outcomes in previous hours, as seen in Figure 9. As suggested
480 in the previous section, this is done using an ARMAX specification. In this case, the
481 transformed explanatory variables from the first stage (e.g., $\text{Solar}_t^{1/4}$) are the exogenous inputs.
482 Given this specification, the disturbance terms are presumed to follow an ARMA specification
483 that models the autocorrelations reported in Figure 9. The ARMA specification applied in this
484 paper is not parsimonious because the autocorrelative process in Figure 9 is not short in duration.
485 It is recognized that this approach runs counter to the traditional time-series philosophy (Box and
486 Jenkins, 1976, p. 17), which suspected that there was more room for prediction errors when more
487 time-series parameters were estimated (Hamilton, 1994, p. 106). The view here is that the goal
488 of predictive accuracy can sometimes be enhanced by including more ARMA terms. This

489 approach makes sense given the long memory property of the autocorrelations evidenced in
 490 Figure 9 and the high level of variability in temperature, as evidenced by Figure 5. The
 491 heteroskedasticity is modeled as a function of the solar zenith angle, the hour of the day, the day
 492 of the year, the year of the sample, and the following variables: $\sqrt{CO2_{t-1}}$, $\sqrt{Solar_t}$. Instead of
 493 assuming that hourly temperature is independent of the conditional variance, the model permits
 494 the data to speak for itself on this issue. This linkage is relevant if the level of a variable depends
 495 on the variance in the disturbance term. The ARCH-in-mean model introduced by Engel et al.
 496 (1987) offers an approach to estimate this linkage.

497
 498 The possible merits of representing the explanatory variables using a nonlinear specification are
 499 addressed using the multivariable fractional polynomial (MFP) methodology (Royston and
 500 Sauerbrei, 2008). Its application includes Forbes and St Cyr (2017, 2019) and Forbes and
 501 Zampelli(2019, 2020). The methodology considers the effects of nonlinear transformations of the
 502 explanatory variables. In the present case, the MFP results suggest the following specification:

$$\begin{aligned}
 503 \quad \ln Temp_t = & \alpha'_0 + \alpha'_1 ZeroSolar_t + \alpha'_2 Solar_t^{1/4} + \alpha'_3 (CO2_{t-1} * ZeroSolar_t)^3 \\
 504 & + \alpha'_4 (CO2_{t-1} * PosSolar_t)^{1/4} + \alpha'_5 (Solar_t * CO2_{t-1})^{1/4} + \sum_{h=1}^9 \beta'_h Angle_h \\
 505 & + \sum_{i=2}^{24} \phi'_i HourOfDay_i + \sum_{j=2}^{365} \gamma'_j DOY_j + \sum_{k=1985}^{2014} \delta'_k Year_k \quad (2)
 \end{aligned}$$

509
 510
 511 Please note that α'_1 , α'_2 , and α'_3 etc. are the estimated coefficients in this specification. Least
 512 squares estimation of (2) produces a seemingly respectable level of explanatory power, the R^2
 513 being about 0.831. However, a Portmanteau test for autocorrelation (Box and Pierce, 1970; Ljung
 514 and Box, 1978) reveals that the residuals are highly autocorrelated. Consistent with Forbes and
 515 St. Cyr (2019, p.17), for lags one through 100, the P values are less than 0.0001. The null
 516

517 hypothesis of no ARCH effects is rejected with a P -value less than 0.0001. Consistent with these
518 issues, the least-squares model is not useful. This finding is supported by out-of-sample
519 predictions over the period 1 Jan 2016 - 31 Aug 2017 time interval that have a root-mean-squared-
520 error (RMSE) of about 5.67 °C, a value that is clearly indicative of a suboptimal prediction
521 process.

522

523 ARCH/ARMAX methods can generate predictions that are much more accurate than the
524 predictions from a least-squares model when the dependent variable is autoregressive and
525 heteroskedastic in nature. In this case, the ARCH process's modeled lag lengths are lags 1 and 2.
526 Consideration was given to including additional ARCH terms to model the apparent diurnal
527 pattern of the ARCH process (e.g., 24, 48, 72, 96 etc.). Consideration was also given to
528 employing alternative ARCH and GARCH specifications. These approaches were abandoned
529 due to model convergence issues. The modeled lag lengths for the AR process are 1 through 12,
530 23, 24, 25, 26, 47, 48, 49, 71, 72, 73, 96, 97, 120, 121, 144, 145, 167, 168, 169, 192, 193, 216,
531 240, 264, 288, 312, 335, 336, 337, 360, 384, 408, 432, 456, 480, 600, 671, 672, 673, 840, and
532 960. The MA modeled lag lengths are 1 through 25, 48, 49, 71, 72, 73, 96, 97, 120, 121, 144,
533 145, 167, 168, 169, 192, 193, 216, 240, 264, 288, 312, 335, 336, 337, 360, 384, 408, 432, 456,
534 480, 600, 671, 672, 673, 840, and 960.

535 Equation (2) was estimated assuming that the residual error terms correspond to the Student t
536 distribution instead of the more typical Gaussian distribution. This approach is believed to be
537 justified by the highly volatile nature of the weather system in the vicinity of Barrow. One
538 shortcoming in its application here is that the "degrees of freedom" parameter is less than the
539 minimum indicated by Harvey (2013, p. 20). Consideration was given to modeling the residual

540 error terms using the generalized error distribution, but this approach was abandoned due to model
541 convergence issues.

542

543 Selected estimates are reported in Table 1. It is revealed that α'_2 , the coefficient corresponding
544 to $\text{Solar}_t^{1/4}$ is positive and highly statistically significant. The CO_2 coefficients α'_3 and α'_4 are
545 also positive and highly statistically significant while α'_5 is negative and highly statistically
546 significant. These findings are consistent with the view that CO_2 concentrations have implications
547 for hourly temperature but do not address the magnitude. Concerning the possible non-
548 anthropomorphic drivers of temperature, it is interesting to note that 16 of the 30 variables in
549 question are statistically significant. With 2015 being represented in the constant term, negative
550 values for a year are consistent with higher predicted temperatures in 2015 than in the year in
551 question. There are 13 such cases. For these cases, the coefficients' median value is -0.00543, a
552 value that hardly seems important.

553

554 The model's explanatory power based on the estimated structural parameters (all the parameter
555 estimates) is 0.8105 (0.9968.) Those who believe that the latter level of explanatory power is
556 somehow "too outstanding to be true," are cheerfully invited to reinspect Figure 9 and contemplate
557 the concept of autocorrelation and how modeling this autocorrelation can affect a model's level of
558 explanatory power. In any event, the view here follows Hyndman and Athanasopoulos (2018,
559 3.4), who note that true adequacy... " can only be determined by considering how well a model
560 performs on new data that were not used when fitting the model." It is also noted that even though
561 a model's R^2 equivalence is a well-recognized measure of model adequacy, a good case can be
562 made that achieving white noise in the residuals is also important (Beckett, 2013, p. 256;

563 Kennedy, 2008, p. 315; and Granger and Newbold, 1974, p. 119). To assess whether this measure
 564 of adequacy is achieved, Portmanteau tests for autocorrelation were conducted for the hourly lags
 565 1 through 100, 192, 284, and 672. At lag 1, the P -value is 0.1958. For the remaining 111 lags that
 566 were assessed, the P -values are less than .05, thereby rejecting the null hypothesis of a white noise
 567 error structure.

568

569

570 **Table 1. Estimation Results**

571

Variable	Estimated Coefficient	Absolute Value of the t-Statistic	P -Value
Constant term	-84.5387	3.41	< 0.001
ZeroSolar _t	0.053421	9.25	< 0.001
Solar _t ^{1/4}	0.01102	11.23	< 0.001
(CO2 _{t-1} *ZeroSolar _t) ³	7.70E-11	7.57	< 0.001
(CO2 _{t-1} *PosSolar _t) ^{1/4}	0.01296	9.04	< 0.001
(Solar _t * CO2 _{t-1}) ^{1/4}	-0.00232	10.42	< 0.001
Year ₁₉₈₅	-0.01111	9.96	< 0.001
Year ₁₉₈₆	-0.00371	2.36	0.018
Year ₁₉₈₇	-0.00983	6.91	< 0.001
Year ₁₉₈₈	-0.00808	6.87	< 0.001
Year ₁₉₈₉	-0.00498	1.76	0.079
Year ₁₉₉₀	-0.0033	1.47	0.141
Year ₁₉₉₁	-0.00285	1.82	0.068
Year ₁₉₉₂	-0.00664	2.21	0.027
Year ₁₉₉₃	-0.00265	2.52	0.012
Year ₁₉₉₄	-0.00339	2.47	0.014
Year ₁₉₉₅	-0.00384	4.43	< 0.001
Year ₁₉₉₆	-0.00305	1.73	0.083
Year ₁₉₉₇	0.001996	1.06	0.288
Year ₁₉₉₈	0.005733	3.48	0.001
Year ₁₉₉₉	-0.00766	4.34	< 0.001

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Year ₂₀₀₀	-0.00543	4.26	< 0.001
Year ₂₀₀₁	-0.00359	2.97	0.003
Year ₂₀₀₂	0.002124	0.61	0.541
Year ₂₀₀₃	-0.00658	3.21	0.001
Year ₂₀₀₄	-0.00449	4.07	< 0.001
Year ₂₀₀₅	-0.00211	1.11	0.265
Year ₂₀₀₆	0.000883	0.33	0.743
Year ₂₀₀₇	0.005622	4.31	< 0.001
Year ₂₀₀₈	1.92E-06	0	0.999
Year ₂₀₀₉	0.002597	1.98	0.048
Year ₂₀₁₀	0.000847	0.38	0.707
Year ₂₀₁₁	0.001634	0.23	0.817
Year ₂₀₁₂	-0.00044	0.22	0.829
Year ₂₀₁₃	0.001147	0.46	0.643
Year ₂₀₁₄	0.002601	1.40	0.162
Number of Observations	228,085		
R-Square equivalence based on the full model	0.9968		
R-Square equivalence based on the model's structural component.	0.8105		

Regarding the binary variables not reported above, 336 of the 364 day-of-the-year coefficients are statistically significant, while 22 of the 23 hour-of-the-day variables are statistically significant. Only three of the nine solar angle coefficients are statistically significant.

Concerning the AR and MA terms, 44 of the 53 AR terms and 31 of the 61 MA terms are statistically different from zero. Both of the ARCH terms are statistically significant. Only one of the three ARCH-in-Mean terms is statistically significant. Regarding the variables that model the heteroskedasticity in the conditional variance, 298 of the 429 variables are statistically different from zero.

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586 **7 The Model's Out-of-Sample Performance**

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588 The out-of-sample evaluation period consists of 13,175 hours over the 1 Jan 2016 to 31 Aug 2017

589 time interval. Recalling that the dependent variable in the model is the natural logarithm of

590 temperature measured in Kelvin, it might seem that a simple retransformation would yield the

591 optimal predicted value. Unfortunately, merely taking the antilogarithm of the predicted natural

592 logarithm of temperature measured in Kelvin may result in a biased temperature prediction

593 (Granger and Newbold, 1976, pp. 196-197). This bias is easily resolved when the error distribution

594 is Gaussian using a method presented by Guerrero (1993). Given the non-Gaussian nature of the

595 error distribution in this case, the matter was resolved by estimating a post-processing regression

596 without a constant term using all of the observations in the sample. The explanatory variable in

597 this post-processing regression is the hourly temperature measured in Kelvin, while the

598 explanatory variable in this regression is the antilog of the transformed predicted values. The

599 estimated coefficient corresponding to the explanatory variable equals 0.9999895. The associated

600 R-Square equals 1.0000. The estimated parameter from this regression was used to detransform

601 the out-of-sample transformed predicted temperature values.

602 The out-of-sample predictions were compared with the ERA5 predictions for the same general

603 location. For those unfamiliar with the ERA5 modeling results, it was produced by the Copernicus

604 Climate Change Service at ECMWF. In a significant advance from its earlier databases, it reports

605 hourly values across the globe. The ERA5 hourly temperature values for the Barrow location were

606 obtained from Meteoblue ([https://content.meteoblue.com/en/specifications/data-](https://content.meteoblue.com/en/specifications/data-sources/weather-simulation-data/reanalysis-datasets)

607 [sources/weather-simulation-data/reanalysis-datasets](https://content.meteoblue.com/en/specifications/data-sources/weather-simulation-data/reanalysis-datasets)).

608

609 The out-of-sample temperature predictions from the ARCH/ARMAX model presented in this
610 paper have a predictive R-square of 0.9962. The predictions are visually more accurate than the
611 ERA5 values for the same general location (Figure 10), although it should be noted that the ERA5
612 values correspond to a grid that includes land and ocean while Barrow represents a land location
613 within that grid. Nevertheless, the ERA5 values may serve as a useful benchmark for the
614 ARCH/ARMAX out-of-sample predictions. Regarding the RMSEs, the predictions associated
615 with the ARCH/ARMAX model have an RMSE equal to about 0.682 °C, while the ERA5
616 outcomes have an RMSE of about 3.117 °C. Interestingly, an ordinary least-squares estimation
617 of the ERA5 predictions indicates that the prediction errors are not purely random. Specifically,
618 the prediction error is conditional on the magnitude of the predicted temperature and lagged value
619 of the CO₂ concentration. The latter finding is consistent with the central thesis of this paper.
620 Following Granger's discussion of prediction errors (1986, p. 91), both of these findings suggest
621 a pathway to improving the accuracy of the ERA5 predictions.

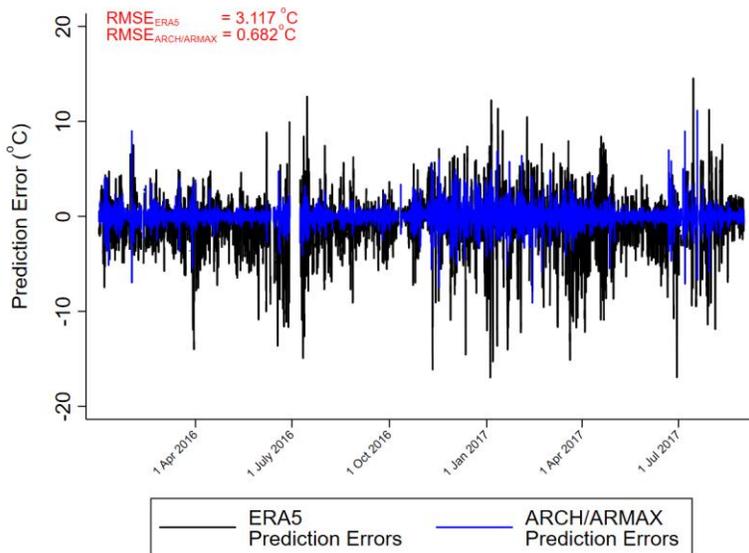
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623 The out-of-sample temperature predictions from the ARCH/ARMAX model are significantly
624 degraded when the estimated effects of CO₂ are ignored (Figure 11). The differential in
625 predictive accuracy is visually apparent if one inspects the vertical distance between the scatter
626 points and the 45° line representing the relationship between predicted and actual temperature
627 when the predictions are perfect. As reported above, the full model presented in this paper has
628 an RMSE equal to 0.682 °C over the evaluation period, constraining the CO₂ estimated effects to
629 be equal to zero results in predictions with an RMSE equal to 3.379 °C.

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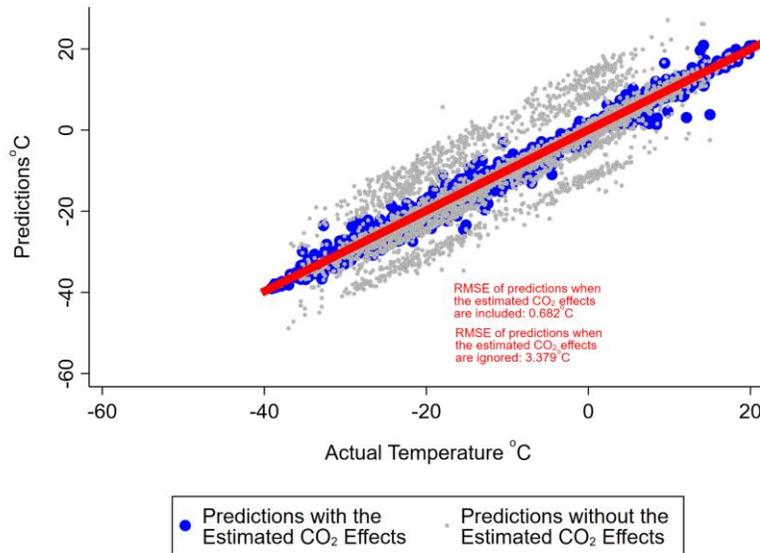
631 The out-of-sample analysis is supportive of the earlier discussion indicating the unimportance of
 632 factors other than CO₂ and the total downward solar irradiance being drivers of the increase in
 633 annual temperature over the sample period. Specifically, using the full model, the mean
 634 predicted temperature over the evaluation period equals - 8.725218 °C. The mean predicted
 635 temperature over the evaluation period is -8.725221 °C if the estimated effects of the binary
 636 variables for 1986 through 2014 are constrained to equal zero. In short, the binary variables that
 637 control for the possibility of annual temperature being affected by factors other than CO₂ or total
 638 downward solar irradiance have virtually no effect on the out-of-sample predicted temperature.
 639 Interestingly, the mean actual temperature over the evaluation period equals -8.712713 °C, a
 640 very close value to the mean of the predicted values.

641



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643 **Figure 10.** The ERA5 and the ARCH/ARMAX prediction errors, 1 Jan 2016 – 31 Aug 2017.



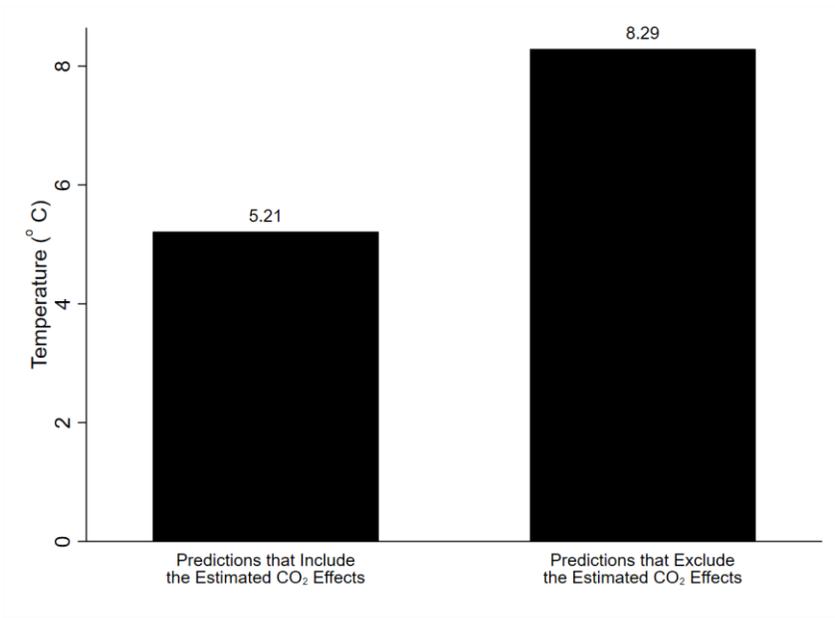
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645 **Figure 11.** The ARCH/ARMAX model predictions with and without the CO₂ estimated effects
 646 and the actual temperature outcomes, 1 Jan 2016 – 31 Aug 2017.

647

648 The structural predictions are less accurate than the predictions from the full model but may
 649 yield useful insights. The predictions from the structural model have an RMSE equal to 5.21 °C
 650 while constraining the CO₂ estimated effects to be equal to zero results in predictions with an
 651 RMSE equal to 8.29 °C (Figure 12). In short, constraining the estimated effects of CO₂ to be
 652 equal to zero reduces the structural model's predictive accuracy. In terms of temperature, the
 653 predicted level is significantly lower when the estimated structural effects of CO₂ are ignored
 654 (Figure 13). Observe that the difference in the mean levels of predicted temperature is
 655 nontrivial.

656



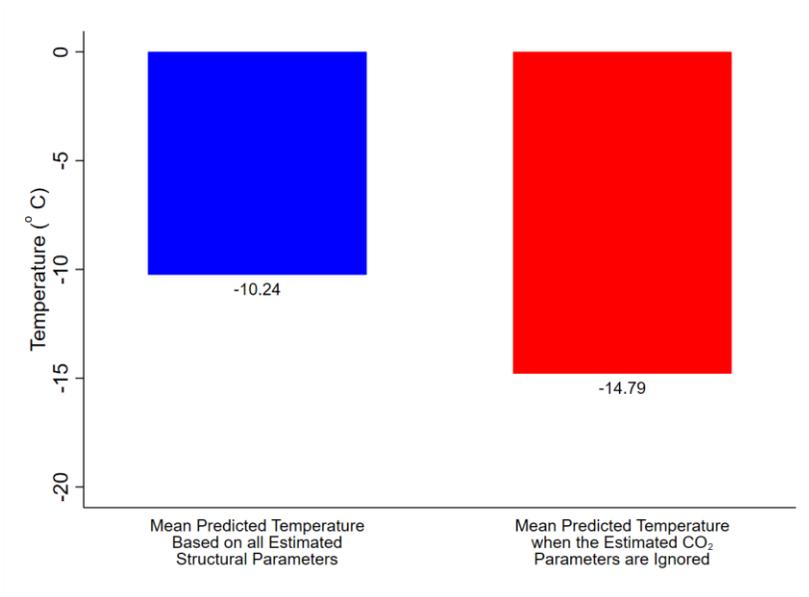
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659 **Figure 12.** The RMSEs in the out-of-sample structural predictions

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665 **Figure 13.** The out-of-sample structural predictions of temperature (°C)

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669 **8 Summary and Conclusion**

670
671 This paper employed an ARCH/ARMAX model with statistical controls for total downward
672 solar irradiance and 426 binary variables to examine the relationship between CO₂
673 concentrations and hourly temperature at the Barrow Atmospheric Observatory in Alaska. The
674 model was estimated using hourly data over the time interval of 1 Jan 1985 - 31 Dec 2015. The
675 model was evaluated using hourly data from 1 Jan 2016 through 31 Aug 2017. The predictive R-
676 square equivalence of 0.9962 over the evaluation period suggests that the model has reduced the
677 attribution challenge associated with the significant natural meteorological variability in the
678 Arctic. Consistent with this view, the predictions over the evaluation period are more accurate
679 than the highly regarded ERA5 values for the same general vicinity. Thus, though the model
680 fails to achieve the metric of “white noise” in the standardized residuals, the accuracy of its
681 predictions over the evaluation period indicates that the model is “useful.” These results are
682 consistent with the physics that indicates that rising CO₂ concentrations have consequences for
683 temperature, a point that even climate deniers such as Richard Lindzen, William Happer, Roy
684 Spencer, Patrick Michaels, and the other members of the CO₂ Coalition have conceded. What is
685 different is that the model also offers useful insights into the magnitude of the relationship
686 between CO₂ concentrations and hourly temperature. Specifically, the predictions over the
687 evaluation period are significantly more accurate when they reflect the estimated and statistically
688 significant CO₂ coefficients compared to when those coefficients are ignored. The out-of-sample
689 results indicate that CO₂ concentrations have nontrivial implications for hourly temperature. The
690 modeling results also addressed the possible contribution of factors other than CO₂ being drivers
691 of increased temperature over the sample. The mean of the out-of-sample predicted temperature

692 over the evaluation period is not materially affected by these variables, even though some of
693 those variables are statistically significant.

694

695 Given that all models are “wrong,” it is a picayune task to dismiss the estimation results reported
696 in Table 1. It is much more challenging to rationally dismiss the implications of the large decline
697 in the out-of-sample predictive accuracy when the estimated CO₂ effects are ignored. One
698 possibility is that some unknown natural factor at work is the true culprit of the decline in
699 predictive accuracy. While climate deniers may find this an attractive explanation for the results
700 presented in this paper, the model’s high level of predictive out-of-sample accuracy suggests that
701 unknown factors are not an important driver of temperature. There is also the point that
702 attributing the large decline in the out-of-sample predictive accuracy when the estimated CO₂
703 effects are ignored to an “unknown variable” is highly likely to represent obscurantism as opposed
704 to a conclusion that represents the best of all competing explanations as explained by Lipton (2004,
705 p. 56). In short, the beliefs of the climate change deniers are not supported by the hourly
706 temperature data at NOAA’s Barrow Observatory in Alaska. Considering the inadequate results
707 of COP26, this suggests that the current outlook for the Earth’s future is quite grim. Research that
708 further illuminates the shortcomings of the views by climate deniers might help matters. One
709 approach being considered is an analysis of the drivers of the hourly surface energy imbalance, a
710 metric that is easily understood as being important but that climate deniers almost never mention.
711 This research path appears feasible using the methods presented here in light of a preliminary
712 analysis indicating that the hourly surface energy imbalance at Barrow and other locations is
713 autoregressive and heteroskedastic. It is not overly optimistic to believe that modeling these
714 properties will facilitate the recognition of CO₂’s “signal” in the data.

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Conflict of Interest

The author declares no conflicts of interest relevant to this study.

Data Availability Statement

Data used in this research and reproducing STATA codes are deposited on Zenodo at [10.5281/zenodo.5833580](https://zenodo.org/doi/10.5281/zenodo.5833580).

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