# A hydrogeomorphological index of heavy-tailed flood behavior

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**Key Points:**

- The hydrograph recession exponent is identified as an index of heavy-tailed flood behavior.
- The proposed index enables robust identification of heavy-tailed flood behavior in a large set of case studies and from short data records.
- Unlike other frequently used metrics, the proposed index infers heavy-tailed flood behaviors from commonly observed discharge dynamics.

## Abstract

Floods are often disastrous due to underestimation of the magnitude of rare events. When the occurrence of floods follows a heavy-tailed distribution the chance of extreme events is sizable. However, identifying heavy-tailed flood behavior is challenging because of limited data records and the lack of physical support for currently used indices. We address these issues by deriving a new index of heavy-tailed flood behavior from a physically-based description of streamflow dynamics. The proposed index, which is embodied by the hydrograph recession exponent, enables inferring heavy-tailed flood behavior from daily flow records. We test the index in a large set of case studies across Germany. Results show its ability to identify cases with either heavy- or nonheavy-tailed flood behavior, and to evaluate the tail heaviness. Remarkably, the results are robust also for decreasing the lengths of data records. The new index thus allows for assessing flood hazards from commonly available data.



## Plain Language Summary

High flow events often cause severe damages when they occur unexpectedly, i.e., more often and with larger magnitudes than suggested by historical observations. This is usually the case with frequency distributions of floods which are heavy-tailed. However, a proper assessment of the tail behavior solely based on limited data records is difficult and might lead to an erroneous estimation of the underlying hazard. We start by analyzing runoff generation processes and find that the hydrograph recession is a proper descriptor of the emergence of heavy-tailed behavior. Our findings show that the new proposed index allows for (1) detecting cases with heavy-tailed behavior, (2) comparing severity across cases, and (3) displaying robust results also with short data records. These results address the main limitations of currently used metrics (which often require long records and lack physical meaning) and provide information on the characteristic flood hazard of river basins.


## 1 Introduction

Floods remain the leading natural hazards worldwide, which directly threaten at least one-fifth of people’s livelihoods (McDermott, 2022; Rentschler et al., 2022) and have caused enormous and increasing economic losses (Bevere & Remondi, 2022) in recent years. Floods are often disastrous because they occur unexpectedly (i.e., underestimated by water resources managers as well as residents) (Else, 2021; Merz et al., 2021), commonly due to poor estimates of the magnitude of rare events obtained from available observations. A number of studies in natural and anthropogenic phenomena use heavy-tailed distributions to describe the extreme behavior of variables (e.g., Katz, 2002; Kondor et al., 2014; Malamud, 2004; Sartori & Schiavo, 2015; Wang et al., 2022) because it indicates a sizable chance of the occurrence of extreme value. We can better assess the flood hazards if we may know that floods follow a heavy-tailed distribution, i.e., robustly identify the heavy-tailed flood behavior (Merz et al., 2022).

A variable distribution's tail heaviness is traditionally estimated graphically or mathematically, while both have their limitations. In general, graphical methods such as log-log plots (Beirlant et al., 2004), generalized Hill ratio plots (Resnick, 2007; El Adlouni et al., 2008), and mean excess functions (Embrechts et al., 1997; Nerantzaki & Papalexiou, 2019) have less objectivity and efficiency (Cooke et al., 2014). Mathematical methods provide more objective insights into the estimation of tail behavior. The shape parameters of Generalized Extreme Value (GEV) distributions quantify the tail behavior by fitting the parameters of an underlying distribution on limited records of maxima (Morrison & Smith, 2002; Villarini & Smith, 2010; Papalexiou et al., 2013), and a group of non-parametric metrics evaluates the spread of data (e.g., upper tail ratio (Lu et al., 2017; Smith et al., 2018; Villarini et al., 2011; Wang et al., 2022), Gini index (Eliazar & Sokolov, 2010; Rajah et al., 2014), and obesity index (Cooke & Nieboer, 2011; Sartori & Schiavo, 2015)). These methods often require long records to obtain reliable estimates (Papalexiou & Koutsoyiannis, 2013). This is a challenge globally and even more challenging when it comes to analyzing maxima (which is indeed the key to assessing hazards of extreme floods). The bias caused by the data size restricts the comparability across sites with different record lengths (Wietzke et al., 2020). In addition, the correctness of the estimation of tail heaviness is influenced by the underlying physical processes of the case studies (Merz et al., 2022). However, to the best of our knowledge, physical processes are absent from these frequently used metrics. It is preferable to have a new index that can robustly estimate with data in different lengths (Bernardara et al., 2008; Merz & Blöschl, 2009) and is based on the physical processes that favor the heavy-tailed behavior of flood distributions.

We propose a new index of heavy-tailed flood behavior, which can be estimated by common discharge dynamics. Unlike fitting a statistical distribution to observed series of maxima (which may not clearly exhibit heavy-tailed behavior due to data scarcity), the index infers the tail heaviness of floods by examining the intrinsic dynamics of the hydrological system. Reliable identification of heavy tails by the proposed index is tested in datasets with decreasing lengths in a great number of case studies with various climate and physiographic features. We leverage common discharge dynamics to facilitate flood peril assessment and demonstrate its usefulness in areas with limited records.

## 2 Identifying tail behavior from hydrological dynamics

We describe key hydrologic dynamics occurring at the catchment scale and the resulting probability distributions of streamflow and floods by means of the PHysically-based Extreme Value (PHEV) distribution of river flows (Basso et al., 2021). This framework is grounded on a well-established mathematical description of precipitation, soil moisture, and runoff generation in river basins (Laio et al., 2001; Porporato et al., 2004; Botter et al., 2007b, 2009). Rainfall is described as a marked Poisson process with frequency $\lambda_p [\mathrm{T}^{-1}]$ and exponentially distributed depths with average $\alpha$ [L]. Soil moisture increases due to rainfall infiltration and decreases due to evapotranspiration. The latter is represented by a linear function of soil moisture between the wilting point and an upper critical value expressing the water holding capacity of the root zone. Runoff pulses occur with frequency $\lambda < \lambda_p$ when the soil moisture exceeds the critical value. These pulses replenish single catchment storage, which drains according to a nonlinear storage-discharge relation. The related hydrograph recession is described via a power law function with exponent $a$ $[-]$ and coefficient $K$ $[\mathrm{L}^{1-\mathrm{a}}/\mathrm{T}^{2-\mathrm{a}}]$ (Brutsaert & Nieber, 1977), which allows for mimicking the joint effect of different flow components (Basso et al., 2015). Such a description of runoff generation and streamflow dynamics was successfully tested in a variety of hydro-climatic and physiographic conditions (Arai et al., 2020; Botter et al., 2007a; Botter et al., 2010; Ceola et al., 2010; Doulatyari et al., 2015; Mejía et al., 2014; Müller et al., 2014; Müller et al., 2021; Pumo et al., 2014; Santos et al., 2018; Schaefli et al., 2013).

PHEV provides a set of consistent expressions for the probability distributions of daily streamflow, ordinary peak flows (i.e., local flow peaks occurring as a result of streamflow-producing rainfall events; Zorzetto et al., 2016), and floods (i.e., flow maxima in a certain timeframe; Basso et al., 2021). For example, the probability distribution of daily streamflow $q$ can be expressed as (Botter et al., 2009):

$$p(q) = C_1 \cdot q^{-a} \left( e^{\frac{-1}{\alpha K(2-a)} \cdot q^{2-a}} \right) \left( e^{\frac{\lambda}{K(1-a)} \cdot q^{1-a}} \right) \tag{1}$$

where $C_1$ is a normalization constant.

Taking the limit of Equation (1) for $q \to +\infty$ gives indications of the tail behavior of the flow distribution (Basso et al., 2015). This is determined by the three terms in the equation, namely, one power law and two exponential functions, which behave differently depending on the value of the hydrograph recession exponent $a$ (Equation 2; notice that $a > 1$ in most natural river basins; Tashie et al., 2020a).

$$\lim_{q \to +\infty} p(q) = \lim_{q \to +\infty} \left\{ C_1 \cdot \overbrace{\underbrace{q^{-a}}_{\mapsto 0}}^{\mapsto 0} \overbrace{\underbrace{\left( e^{\frac{-1}{\alpha K(2-a)} \cdot q^{2-a}} \right)}_{\mapsto e^0 = 1}}^{\mapsto 0} \overbrace{\underbrace{\left( e^{\frac{\lambda}{K(1-a)} \cdot q^{1-a}} \right)}_{\mapsto e^0 = 1}}^{\mapsto e^0 = 1} \right\} \quad \begin{matrix} \text{for } 1 < a < 2 \\ \\ \text{for } a > 2 \end{matrix} \tag{2}$$

When $1 < a < 2$, the last term on the right-hand side converges to a constant value of one as $q$ increases, thereby no more influence on how the distribution decreases toward zero. The first two terms instead decrease toward zero, affecting how the probability decreases for increasing values of $q$. The tail behavior is in this case determined by both a power law and an exponential functions, indicating that the probability decreases faster than an exponential but slower than a power law. When $a > 2$, both the exponential terms converge to a constant value of one as $q$ increases, and thus no more influence on how the probability decreases toward zero. In this case the tail of the distribution is solely determined by the power law function. Despite being aware that several definitions of heavy-tailed distribution exist (El Adlouni et al., 2008; Vázquez et al., 2006), in the remaining of the manuscript we refer to heavy-tailed behavior for the case of distributions which exhibit a power law tail (i.e., the cases with a > 2). We thus aim to distinguish them from cases which display a lighter tail because of the simultaneous effect of exponential decay (i.e., the cases with $1 < a < 2$).

From the above derivations, the hydrograph recession exponent emerges as a key index of the tail behavior of streamflow distributions, which shall be heavy-tailed for values of $a > 2$. The same analysis applies to infer the tail behavior of the probability distributions of ordinary peak flows (Botter et al., 2009) and floods (Basso et al., 2016) (see supporting information Text S1). Remarkably, we find that the same critical value of the recession exponent indicates the emergence of heavy-tailed behavior also in peak flow and flood distributions. We therefore propose the hydrograph recession exponent $a$ as an index for identifying heavy-tailed flood behavior, and test its capability to correctly predict such behavior in Section 4.

Recent studies showed that the hydrograph recession exponent is a convincing descriptor of the geomorphological signature of drainage areas (Biswal & Marani, 2010, 2014; Biswal & Kumar, 2014; Ghosh et al., 2016; Mutzner et al., 2013). The river network structure primarily defines how the geometry of saturated (Mutzner et al., 2013) and unsaturated areas (Biswal & Marani, 2010) of a river basin change over the draining process, which essentially determines the streamflow dynamics at the outlet. Despite being aware of the influences of seasonal climate (Jachens et al., 2020; Tashie et al., 2019), the geomorphological structure of the contributing river network has been demonstrated as the major determinator of the hydrograph recession exponent (Biswal & Kumar, 2014; Ghosh et al., 2016). We thus refer to the hydrograph recession exponent for a hydrogeomorphological index of heavy-tailed flood behavior.

## 3 Data and parameter estimation

To test the proposed hydrogeomorphological index of heavy-tailed flood behavior (i.e., the hydrograph recession exponent $a$), we use streamflow records with daily time resolution of 98 gauges across Germany (Figure S1). The analyzed river basins encompass a variety of climate and physiographic settings (Tarasova et al., 2020), while not being heavily affected by anthropogenic flow regulation and snow dynamics across seasons. Their areas range from 110 to 23,843 $km^2$ with a median value of 1,195 $km^2$. The minimum, median, and maximum lengths of the streamflow records are 35, 58, and 63 years (inbetween 1951 – 2013). We perform all analyses on a seasonal basis (winter: December–February, spring: March–May, summer: June–August, fall: September–November) to account for the seasonality of the hydrograph recessions and flood distributions (Durrans et al., 2003; Tashie et al., 2020b). This results in an overall number of 386 case studies used in our study.

We estimated $a$ as the median value of the exponents of power law functions fitted to $dq/dt - q$ pairs of each hydrograph recession observed in the daily flow series (Jachens et al., 2020; Biswal, 2021). Notice that the proposed indicator of heavy-tailed flood behavior is thus estimated based on commonly available daily discharge observations.

The identification of case studies with either heavy- or nonheavy-tailed behavior resulting from the proposed index must be evaluated against a suitable benchmark. This is obtained by means of a state-of-the-art approach to fit power law functions to empirical distributions and evaluate their plausibility for the analyzed data (Clauset et al., 2009). The fitted exponent is here noted as $b$. We analyze three types of empirical data, namely daily streamflow, ordinary peaks, and monthly maxima (Fischer & Schumann, 2016; Malamud & Turcotte, 2006), and obtain estimates of the fitted exponent $b$ for each case. These results will be used to validate the capabilities of the proposed hydrogeomorphological index to infer heavy-tailed flood behavior from the analysis of hydrograph recessions.

## 4 Results and discussion

We examine if power law distributions fitted to the empirical distributions of daily streamflow, ordinary peaks, and monthly maxima well describe the observed data for the case studies identified as having heavy-tailed behavior (i.e., a > 2) according to the hydrogeomorphological index (Figure 1). First, we identify the case studies with either heavy- (a > 2; red) or nonheavy (a < 2; green) -tailed behavior based on the hydrogeomorphological index. Then, we use the Kolmogorov-Smirnov (KS) statistic $\kappa$ to evaluate the reliability of the fitted power law function in describing the data ($\kappa \in [0,\infty]$, $\kappa=0$ denotes the highest reliability). The KS statistic $\kappa$ indicates how likely the data are to be drawn from a power law. Figures 1a-1c show that the histograms of the number of case studies are significantly skewed toward lower values of $\kappa$ for all cases of daily streamflows, ordinary peak flows, and monthly flow maxima with a > 2 (red histograms), whereas this is not true for cases with a < 2 (green histograms). Statistical significance of the skewnesses was evaluated through the Jarque–Bera test at a significance level of 0.05. The result essentially indicates that data from case studies which are identified with heavy-tailed behavior according to the hydrogeomorphological index (a>2, red) are indeed more likely to come from power law distributions.

We further estimate the accuracy of the hydrogeomorphological index based on the fraction of case studies that are correctly identified by the hydrogeomorphological index among all heavy-tailed cases. To define the number of cases with heavy tails based on the available observations, we choose a threshold value of $\kappa$ to determine whether the data are reliably described by power law functions. Mathematically, the accuracy can be expressed as $P_{a>2}(\kappa < \kappa_r) = N_p(a > 2)/N_p$, where $\kappa_r$ is the imposed threshold of $\kappa$, $N_p$ is the number of case studies whose $\kappa < \kappa_r$, and $N_p(a > 2)$ is the number of case studies with $a > 2$ among the $N_p$ case studies. Higher accuracy essentially means that a higher fraction of heavy-tailed cases (as defined by fitted power laws and a set $\kappa_r$ threshold) are correctly identified by means of the hydrogeomorphological index. Notice that the smaller the $\kappa_r$ threshold, the more reliable the description of power law distributions for data. The blue frame and dot in figures 1a and 1d display an example of defined reliability and the corresponding accuracy.

Figures 1d-1f display the accuracy of the hydrogeomorphological index as a function of the reliability threshold $\kappa_r$. In all three cases (daily streamflows, ordinary peak flows, and monthly flow maxima), the accuracy values increase with the reliability level of the power law function fitted on observed data. This means that the hydrogeomorphological index shows higher accuracy for case studies where the empirical distributions of observed data are more consistent with power laws. In other words, the proposed hydrogeomorphological index, which is estimated as the hydrograph recession exponent from commonly available daily flow records, is a robust indicator of heavy-tailed flood behavior.

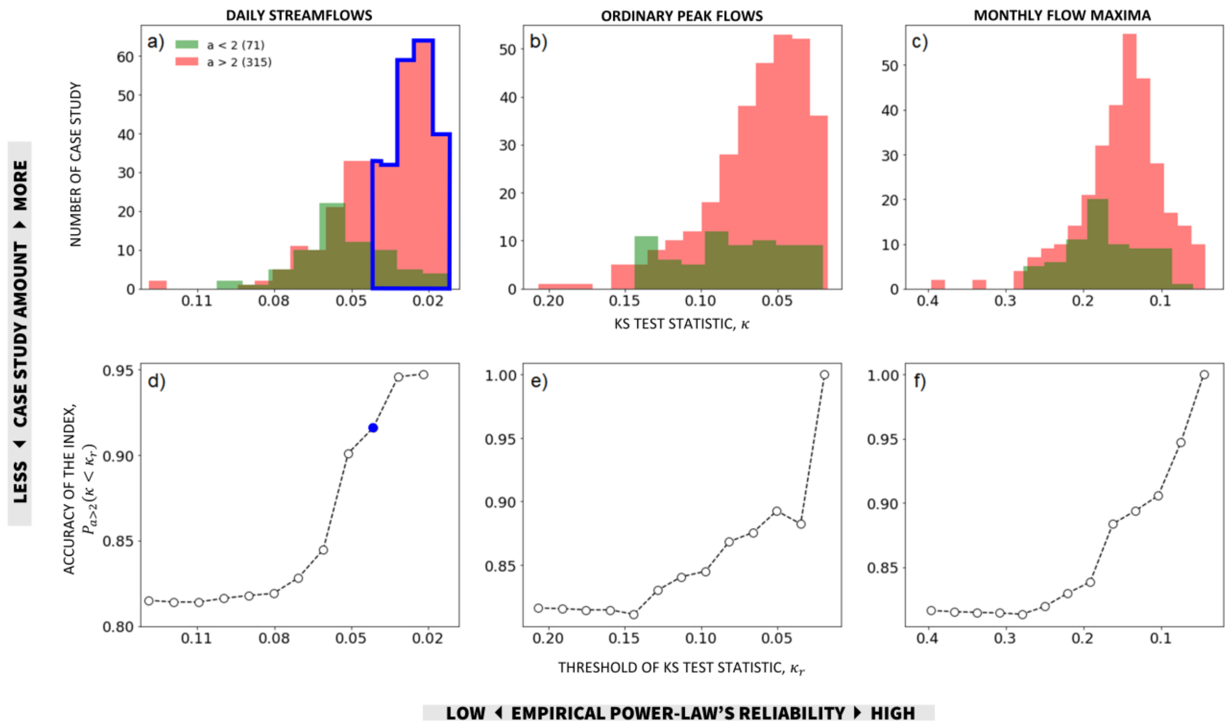


**Figure 1. Accuracy of the proposed hydrogeomorphological index.** (a)-(c) Number of analyzed case studies as a function of the KS statistic $\kappa$ of empirically fitted power law distributions (the latter is a measure of how reliable the power law is as a model for the given data: the lower $\kappa$, the more reliable the power law model). Case studies are identified with either heavy- ($a > 2$, red histograms) or nonheavy ($a < 2$, green histograms) –tailed behavior based on the hydrograph recession exponent $a$ estimated from daily flow records, which is proposed as a hydrogeomorphological index of heavy-tailed streamflow and flood behavior. (d)-(f) Accuracy of the hydrogeomorphological index as a function of decreasing thresholds of $\kappa_r$ (i.e., increasing reliability of empirical power laws). The accuracy $P_{a>2}(\kappa < \kappa_r)$ is essentially the fraction of the red area under a specified threshold of $\kappa$ (as explanatorily shown by the blue frames and dots in panels a and d). The values of the KS statistic $\kappa$ are derived from records of (a, d) daily streamflows, (b, e) ordinary peak flows, and (c, f) monthly flow maxima.

We further employ the goodness-of-fit testing procedure proposed by Clauset et al. (2009) (supporting information Text S2) to identify case studies for which the representation of daily streamflow, ordinary peak flows, and monthly maxima by means of power law distributions is convincingly supported by the available data. We refer to these case studies as ‘confirmed heavy-tailed cases’ (Figure 2, black dots). Conversely, we term the remaining ones as 'uncertain cases' (Figure 2, gray). The latter label denotes that the distribution underlying the available observations may or may not be a power law but, statistically speaking, we cannot be conclusive due to data scarcity.

Figure 2 shows the empirical power law exponent $b$ as a function of the hydrogeomorphological index of heavy-tailed flow behavior $a$. Red markers display the median values of $a$ and $b$ (squares), the interquartile intervals of $b$ (vertical bars), and the binning ranges of $a$ (horizontal bars, equal number of case studies in each bin), highlighting the correlation between the empirical power law exponent $b$ and the hydrograph recession exponent $a$ for confirmed heavy-tailed cases (black dots) in all three cases (i.e., daily streamflows, ordinary peak flows, and monthly flow maxima). We also test the correlation by calculating their distance correlation (Székely et al., 2007), which is valid for both potential linear and nonlinear associations between two random variables. We find that $a$ and $b$ are significantly correlated at a significance level of 0.05 in all three cases with distance (Spearman) correlation coefficients of 0.45, 0.44, and 0.81 (0.42, 0.46, and 0.60) for daily streamflows, ordinary peak flows, and monthly flow maxima. The last high value of correlation is likely affected by the existence of two clusters of black dots in Figure 2c. Nonetheless, the existence of a statistically significant correlation between the empirical power law exponent and the hydrogeomorphological index (confirmed for all panels a,b,c) confirms that the latter not only can be used to identify heavy-tailed flood behavior but also to evaluate the degree of the tail heaviness of the underlying distributions.

Figure 2c is of particular interest because it shows a common issue in the practice of flood hazard assessment. The power law is a plausible representation of the empirical distribution of monthly maxima in some cases (black dots) that are characterized by large values of the recession exponent $a$ and are therefore classified as having heavy-tailed behavior according to the hydrogeomorphological index. In other cases (gray dots), conclusive evidence of possible heavy-tailed flood behavior cannot be drawn from the limited observations of monthly maxima. However, the hydrogeomorphological index retains its capability to provide estimates of the tail heaviness based on the value of the hydrograph recession exponent and classifies the case studies as heavy-tailed. Such a classification is deemed robust, provided that the predictions of the hydrogeomorhological index are confirmed by observations in cases (panels a and b) where data size is not a limitation (i.e., for daily streamflow and ordinary peak flows). The ability of the hydrogeomorphological index to infer the tail heaviness of flood distributions by examining the intrinsic dynamics of the hydrological system constitutes an advantage of the approach, that is especially useful in the very common cases when the tail of the flood distribution cannot be known from limited observations of maxima only.

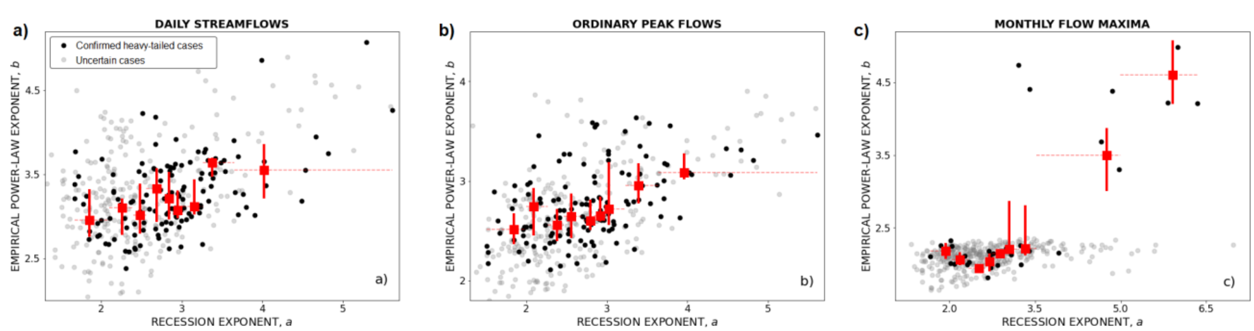


**Figure 2. Empirical power law exponent $b$ as a function of the hydrogeomorphological index of heavy-tailed behavior $a$.** Case studies are classified into groups of confirmed heavy-tailed (black dots) and uncertain (gray dots) cases on the basis of the goodness-of-fit testing procedure (Clauset et al., 2009). The former denotes cases for which a power law provides a reliable description of the empirical data distribution, while the latter denotes cases whose data cannot convincingly support such a distribution. Red markers highlight the correlation between the empirical power law exponent $b$ and the hydrograph recession exponent $a$ for confirmed heavy-tailed cases in the case of (a) daily streamflows ($n$=121 case studies), (b) ordinary peak flows ($n$=116), and (c) monthly flow maxima ($n$=34). Red markers display the median values

of $a$ and $b$ (squares), the interquartile intervals of $b$ (vertical bars), and the binning ranges of $a$ (horizontal bars, equal number of case studies in each bin).

In Figure 3, we test the index stability of the categorization of case studies into heavy/nonheavy-tailed flood behavior for decreasing data lengths. We benchmark the hydrogeomorphological index (i.e., the hydrograph recession exponent $a$) against two other frequently used metrics of heavy tails in hydrological studies: (1) the upper tail ratio (UTR) (Lu et al., 2017; Smith et al., 2018; Villarini et al., 2011; Wang et al., 2022) and (2) the shape parameter $\xi$ of the GEV distribution (Morrison & Smith, 2002; Papalexiou et al., 2013; Villarini & Smith, 2010). The UTR is derived as the ratio of the maximum record to the 0.9 quantiles of floods (Smith et al., 2018), and the $\xi$ is estimated using the python package OpenTURNS 1.16 (Baudin et al., 2017). We compute both using data of monthly flow maxima. For all three indices ($a, UTR,$ and $\xi$), we estimate the index for decreasing data lengths from 35 (bounded by the shortest record length in the dataset) to 2 years in each case study. The index for each test length is calculated based on the median value of the estimates derived from 30 random fragments (with the assigned test length) of the entire record.

To have the reference of the stability of the categorization, we use the entire data record computing the values of the hydrogeomorphological index and the GEV shape parameter (notations with an asterisk in Figure 3, i.e., $a^*$ and $\xi^*$). Each case study is categorized as either having (red) or not (green) the heavy-tailed behavior by the criteria of heavy (nonheavy) tails for the geomorphological index as $a^* > 2$ ($a^* < 2$) or for the GEV shape parameter as $\xi^* > 0$ ($\xi^* \leq 0$) (Godrèche et al., 2015). For the UTR, however, there is no specific threshold for the identification of heavy/nonheavy tails, but a larger value indicates a heavier tail.

The categorization of the hydrogeomorphological index is consistent across the test data length (Figure 3a). Specifically, the index estimates retain beyond 2 for most heavy-tailed cases (red) and below 2 for most nonheavy-tailed cases (green) when the data length decreases. The vertical shaded bar and line show the 0.25–0.75 and 0.05–0.95 quantile ranges of the index estimates across case studies. Besides the consistent categorization, the index estimates vary in a narrow range over the test data length both for the median value (i.e., from 2.64 to 2.92 for heavy-tailed cases and from 1.84 to 2.0 for nonheavy-tailed cases) and for the variation (e.g., the coefficient of variation ranges from 0.29 to 0.33 for heavy-tailed cases and from 0.29 to 0.33 for nonheavy-tailed cases). The small fluctuation of the variation across the test data length implies that the variation in index estimates is primarily caused by case study heterogeneity rather than decreasing data length. These results essentially confirm the stability of the hydrogeomorphological index for decreasing data lengths.

In contrast, the upper tail ratio shows pronounced instability for decreasing data lengths (Figure 3b). The median value of the index estimates ranges from 1.32 to 2.36, and the coefficient of variation ranges from 0.15 to 0.64, indicating that the tail heaviness is underestimated as data length decreases, in agreement with Smith et al. (2018) and Wietzke et al. (2020). The differential variation for decreasing data length denotes an apparent bias in the index estimates caused by the short data in addition to the heterogeneity across case studies.

Figure 3c shows the categorization of tail behavior based on the estimates of the GEV shape parameters. When the test data length is above five years, case studies with index estimates in the interquartile range (the vertical shaded bar) are consistent in the categorization of heavy/nonheavy-tailed behavior. When the data length is below five years, the underestimation of tail heaviness exists. Meanwhile, the index estimate changes slightly in its median but evidently in its coefficient of variation across the test data length. The former (latter) ranges from 0.39 to 0.52 (0.37 to 1.03) for the heavy-tailed cases and keeps 0 (--; the coefficient of variation is not applied for data with zero mean) for the nonheavy-tailed cases. These results show that the GEV shape parameter may still be considered a practical index for the heavy/nonheavy-tailed categorization because most applications have data that are more than five years. Nonetheless, the bias in the variation of index estimates across data length and the apparent underestimation in cases with very limited data point to the dependence on data lengths, in agreement with Papalexiou and Koutsoyiannis (2013).

We demonstrate the hydrogeomorphological index is robust in cases with limited data, i.e., it is stable in the categorization of heavy/nonheavy-tailed flood behavior for decreasing data lengths. Given that most data records worldwide are relatively short (Lins, 2008), this is a valuable tool to infer the tail behavior of streamflow in river basins. Moreover, given that generally all available records are too short of estimating the tail behavior of maxima (e.g., floods), this approach is even more valuable because it allows scientists or engineers to estimate the heavy-tailed flood behavior and assess the hazards from common discharge dynamics.

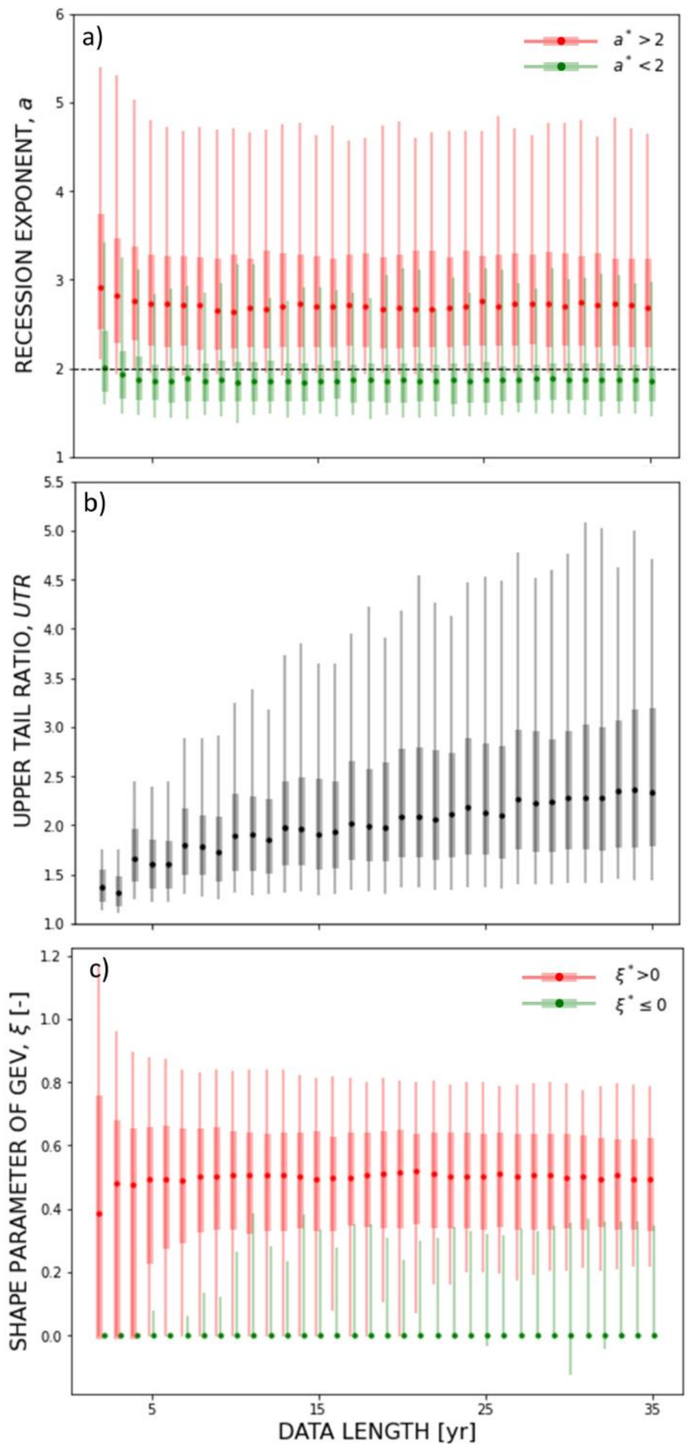


**Figure 3. Stability of the categorization of case studies into heavy/nonheavy-tailed flood behavior for decreasing data lengths.** Estimates of three different indices of tail behavior as a function of data length. (a) Hydrograph recession exponent $a$ (i.e., the proposed hydrogeomorphological index of this study). Two frequently used metrics of heavy tails in hydrological studies: (b) the upper tail ratio $UTR$, and (c) the shape

parameter $\xi$ of the GEV distribution. Dots display the median values of the estimates for 386 case studies; vertical shaded bars and lines respectively show the 0.25-0.75 and 0.05-0.95 quantile ranges of the estimates. The entire data record was used for computing the reference values of the hydrograph recession exponent $\alpha^*$ and the GEV shape parameter $\xi^*$ and categorizing each case study as either having (red) or not (green) the heavy-tailed behavior.

## 5 Conclusions

The hydrograph recession exponent is identified as an index of heavy-tailed flood behavior from a physically-based description of hydrological dynamics. It is essentially a hydrogeomorphological index of heavy-tailed flood behavior because it originates from the geomorphological structure of the contributing river basin. We show that the proposed hydrogeomorphological index enables the identification of heavy/nonheavy-tailed flood behavior and the evaluation of the tail heaviness across case studies. Remarkably, it leverages the information of common discharge dynamics and shows robust identification of tail behavior for decreasing data length. We demonstrate all these capabilities in a large set of case studies across Germany on a seasonal basis, featuring the diversity in climatic and physiographic conditions. The hydrogeomorphological index addresses the limitations of other frequently used indices (e.g., lack of physical support, low effectiveness/ineffectiveness in cases with limited data) and allows for robust identification of heavy-tailed flood behavior, which is particularly useful in assessing hazards of extreme floods in data-scarce areas.

## Acknowledgments

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## Data Availability Statement

For providing the discharge data for Germany, we are grateful to the Bavarian State Office of Environment (LfU, https://www.gkd.bayern.de/de/fluesse/abfluss) and the Global Runoff Data Centre (GRDC) prepared by the Federal Institute for Hydrology (BfG, http://www.bafg.de/GRDC). Climatic data can be obtained from the German Weather Service (DWD; ftp://ftp-cdc.dwd.de/pub/CDC/). The digital elevation model can be retrieved from Shuttle Radar Topography Mission (SRTM; https://cgiarcsi.community/data/srtm-90m-digital-elevation-database-v4-1/).

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