

# Nowcasting Solar EUV Irradiance with Photospheric Magnetic Fields and the Mg II Index

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## Key Points:

- Improved nowcast models for commonly used extreme ultraviolet (EUV) and far ultraviolet (FUV) solar irradiance bands
- Utilization of well-calibrated Mg II observations decreases the error between the modeled and observed EUV values
- Real-time EUV observations are not required to correct and improve the EUV irradiance models

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**Abstract**

A new method to nowcast spectral irradiance in extreme ultraviolet (EUV) and far ultraviolet (FUV) bands is presented here, utilizing only solar photospheric magnetograms and the Mg II index (i.e., the core-to-wing ratio). The EUV and FUV modeling outlined here is a direct extension of the SIFT (Solar Indices Forecasting Tool) model, based on Henney et al. (2015). SIFT estimates solar activity indices using the earth-side solar photospheric magnetic field sums from global magnetic maps generated by the ADAPT (Air Force Data Assimilative Photospheric Flux Transport) model. Utilizing strong and weak magnetic field sums from ADAPT maps, Henney et al. (2015) showed that EUV & FUV observations can also be well modeled using this technique. However, the original forecasting method required a recent observation of each SIFT model output to determine and apply a 0-day offset. The new method described here expands the SIFT and ADAPT modeling to nowcast the observed Mg II index with a Pearson correlation coefficient of 0.982. By correlating the Mg II model-observation difference with the model-observation difference in the EUV & FUV channels, Mg II can be used to apply the 0-day offset correction yielding improvements in modeling each of the 37 studied EUV & FUV bands. With daily global photospheric magnetic maps and Mg II index observations, this study provides an improved method of nowcasting EUV & FUV bands used to drive thermospheric and ionospheric modeling.

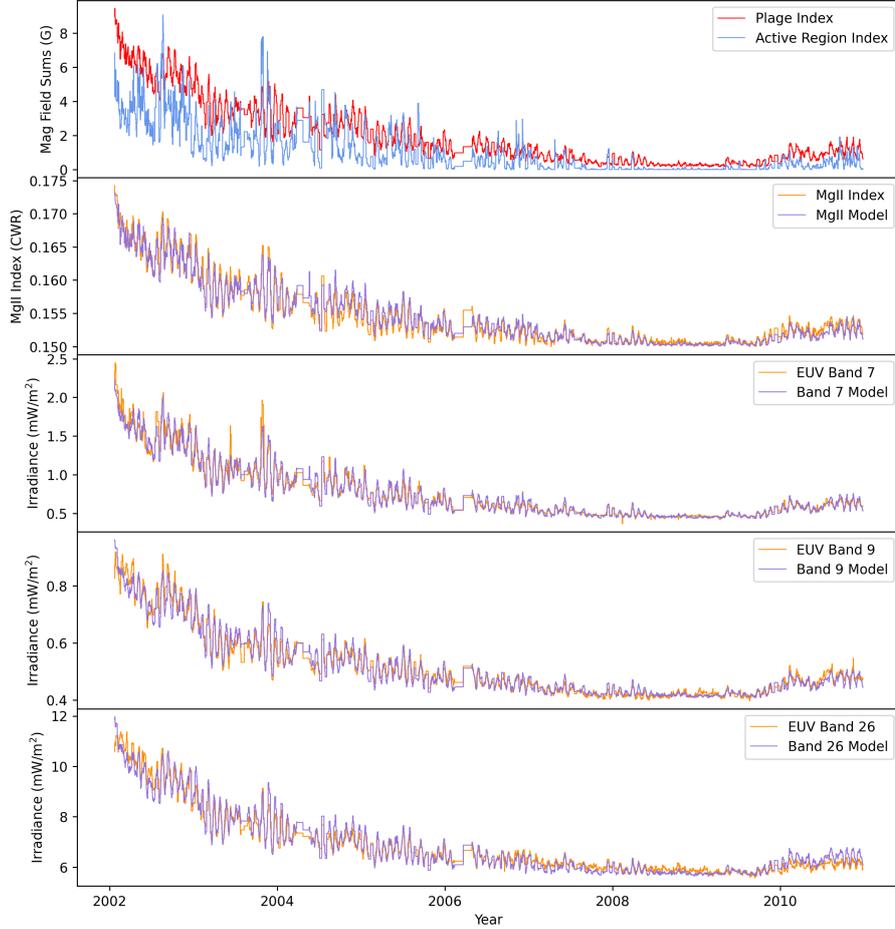
**1 Plain Language Summary**

Ultraviolet irradiance from the Sun can create variability in Earth's atmosphere and cause problems, for example, with satellite communication and their orbital paths. However, we are limited in measuring solar ultraviolet irradiance since it must be observed from space and therefore models of the irradiance are important. In this paper, we present an improved way to model ultraviolet irradiance using solar magnetic fields and a well-calibrated solar activity proxy. We find that models of the irradiance improve when the proxy is used to correct daily variations compared to models driven using just the magnetic fields.

**2 Introduction**

Solar irradiance, specifically the ultraviolet (UV) band vacuum UV (VUV; 0.1 to 200 nm) which includes X-ray UV (XUV; 0.1 to 10 nm), extreme UV (EUV; 10 to 120 nm) and far UV (FUV; 120 to 200 nm), is an important driver for modeling variability in the earth's upper atmosphere. For example, the solar EUV flux causes ionization, dissociation, and excitation of the atoms and molecules in the terrestrial upper atmosphere (Lilensten et al., 2008). All of these interactions lead to heating, and this solar irradiance both creates the ionosphere and is the main source of energy in the thermosphere (Fuller-Rowell et al., 2004). The atmospheric variability induced by changes in the solar EUV irradiance can impact radio communications (due to an enhanced ionosphere e.g., Klobuchar, 1985; McNamara, 1985) and atmospheric drag on satellites (due to increased density at high altitudes e.g., De Lafontaine & Garg, 1982). Because of these impacts, real-time knowledge of solar irradiance is necessary to drive nowcast models of the terrestrial upper atmosphere (e.g., Goncharenko et al., 2021).

However, measurements of the solar EUV irradiance have serious limitations because these wavelengths are absorbed in the earth's upper atmosphere, so they must be observed from space. While such measurements began in the 1960s, this spectral range has been inconsistently observed and there are large gaps in both time and spectral coverage when no observatories were taking measurements (Pesnell, 2016). Furthermore, even when measurements exist, they are notoriously difficult to calibrate due to instrumental degradation (e.g., R. a. Hock et al., 2012). Because of these observational dif-



**Figure 1.** From top to bottom: the active and plage weighted magnetic sums, the Mg II nowcast model and observed values, and the Band 7 (15.5 - 22.4 nm), Band 9 (29.0 - 32.0 nm), and Band 26 (121.6 nm) EUV nowcast models and observed values. Note that the magnetic Plage Index variability, both long and short term, agrees with Mg II and the EUV Band 7, 9, and 26 time series over the full period. Similar figures for all 37 bands are available at Kniezewski et al. (2023).

62 difficulties, there is significant benefit to modeling rather than observing the solar EUV ir-  
 63 radiance spectrum.

64 Solar EUV originates in the solar atmosphere from plasma at a wide variety of tem-  
 65 peratures, from 50 kK in the upper chromosphere to 10 MK in the corona, and typically  
 66 increases with solar activity. Many solar irradiance models use one (e.g., Richards et al.,  
 67 1994) or more (e.g., P. C. Chamberlin et al., 2020) activity proxies and correlate them  
 68 with individual channels of EUV irradiance spectra. Then, simply by measuring the proxy,  
 69 select EUV and FUV spectral bands can be estimated. Two commonly used proxies are

70 the solar 10.7 cm (2.8 GHz) radio flux (Covington, 1947; Tapping, 2013), abbreviated  
 71 as  $F_{10.7}$  and the Mg II core-to-wing ratio (often referred to as the Mg II Index, and here-  
 72 inafter referred to as Mg II; Heath & Schlesinger, 1986).

73 Besides using proxies similar to  $F_{10.7}$ , it is also possible to drive an EUV model us-  
 74 ing solar magnetic field measurements (e.g., full-disk magnetograms and global magnetic  
 75 maps) since the magnetic fields provide the energy to heat the solar atmosphere that pro-  
 76 duces the EUV irradiance. Henney et al. (2012, 2015, hereafter Henney2012 and Hen-  
 77 ney2015, respectively) used earth-side weak and strong solar photospheric magnetic field  
 78 sums from global magnetic maps to estimate irradiance in EUV bands, along with  $F_{10.7}$ .  
 79 Similar work by (Warren et al., 2021) utilized more bins in the magnetic field strength  
 80 combined with principle component analysis and demonstrated similar success model-  
 81 ing  $F_{10.7}$ , Mg II, and selected EUV emission lines.

82 This paper expands on the nowcasting components of Henney2012 and Henney2015  
 83 by focusing on Mg II rather than  $F_{10.7}$  and using it to correct EUV nowcasts. The Hen-  
 84 ney2015 EUV forecast method required a recent EUV observation to determine and ap-  
 85 ply a 0-day (nowcast) correction. The method described here instead uses the Mg II model  
 86 to estimate corrections to EUV nowcast models. The data used in this study are described  
 87 in Section 3. The addition of the Mg II modeling, its use as a corrective factor to the  
 88 Solar Indices Forecasting Tool (SIFT), and the results of this study are described in Sec-  
 89 tion 4. We provide a summary of the results in Section 5.

### 90 3 Solar Data Sources

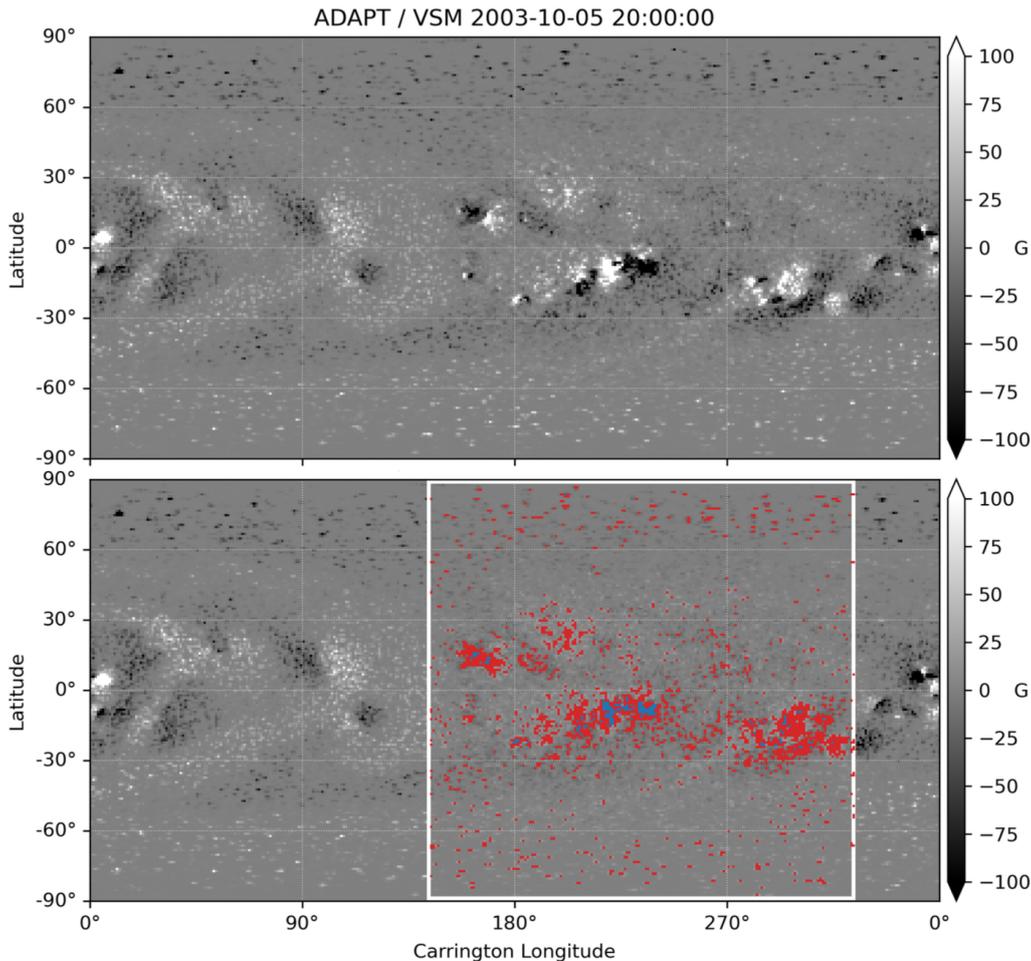
91 Beginning on January 22nd, 2002, the Thermosphere Ionosphere Mesosphere En-  
 92 ergetic and Dynamics (TIMED) Solar EUV Experiment (SEE) observations define the  
 93 start of our investigation period. Figure 1 shows the daily trend of solar activity dur-  
 94 ing our period of investigation, from the maximum of Solar Cycle 23 through 2010 and  
 95 the Cycle 23/24 minimum. This date range matches Henney2012 and Henney2015.

#### 96 3.1 Mg II Index

97 For this study we use the Mg II daily composite index from the University of Bre-  
 98 men (Snow et al., 2014), available online at [http://www.iup.uni-bremen.de/gome/solar/  
 99 MgII\\_composite.dat](http://www.iup.uni-bremen.de/gome/solar/MgII_composite.dat). The Bremen composite data set (Skupin et al., 2005) includes daily  
 100 indices back to 1978. The solar Mg II Index is derived by taking the ratio between the  
 101 spectral irradiance of the Mg II h and k absorption lines near 280 nm and the nearby  
 102 background solar continuum (Heath & Schlesinger, 1986). Mg II varies with solar activ-  
 103 ity on many timescales (Dudok de Wit et al., 2008, 2009) and performs well as a proxy  
 104 for solar activity and for some EUV emission (i.e., 25.0 - 35.0 nm Viereck et al., 2001).  
 105 Since Mg II is generated from a ratio of measurements taken with the same instrument,  
 106 despite requiring a spacecraft UV observation, the Mg II index is robust against instru-  
 107 ment degradation and aging. The Mg II data is recorded in a single 50 second observa-  
 108 tion window daily at 1200 UT. No effort is made to remove the effects of solar flares in  
 109 these data.

#### 110 3.2 EUV and FUV Irradiance

111 The irradiance data used in this study are from the TIMED/SEE observations from  
 112 the EUV Grating Spectrograph (EGS) and XUV Photometer System (XPS) (Woods et  
 113 al., 1998). These data include low-resolution ( $\sim 5$  nm) diode measurements below 25 nm  
 114 (XPS) and 0.4 nm resolution spectra between 25 and 195 nm (EGS) collected over  $\sim 3$ -  
 115 minute observation windows once per  $\sim 90$ -minute orbit. We use the calibration version  
 116 11 EGS level 3 and XPS level 4 data products for this study. These data are averaged



**Figure 2.** *Top:* An example ADAPT global photospheric magnetic map on October 5, 2003 at 20:00 UT, generated by data assimilating NSO SOLIS/VSM magnetograms. *Bottom:* The same ADAPT map with the Earth pointing side of the Sun delineated by the white box and the SIFT active region and plage fields highlighted in blue and red, respectively.

117 over a day to create this daily cadence data and flares have been removed. Additionally,  
 118 we de-spike EUV Band 1 (i.e., range 0.05 - 0.4 nm) values above  $0.7 \mu W/m^2$ , replacing  
 119 them with the average of the previous and following days' data points. Four data points  
 120 (i.e., large "spikes") are removed from Band 1 across the entire nine-year period.

121 For this study, we re-bin these data into 37 bands between 0.05 nm to 175 nm shown  
 122 in Table 1. These include the 22 bands defined in Solomon and Qian (2005) for input  
 123 in general thermosphere and ionosphere models, plus 14 additional bands which cover  
 124 the Shumann-Runge range (Torr et al., 1979), and the Lyman  $\alpha$  line. While these 37 bands  
 125 include XUV, EUV, and FUV irradiance, we will refer to them all as EUV bands and  
 126 the spectrum they cover as the EUV for simplicity. The emission sources for each band  
 127 include atomic transitions from the chromosphere through the corona. Shorter wavelengths  
 128 (i.e.,  $< 20$  nm) are generally from coronal emission, and longer wavelengths (i.e.,  $> 50$   
 129 nm) generally come from the chromosphere and upper transition region (Doschek & Feld-  
 130 man, 2010), although this is not a sharp distinction.

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### 3.3 Photospheric Magnetic Field

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Following Henney2012 and Henney2015, the magnetic field data used for this study are from global photospheric magnetic maps created by the ADAPT model (Arge et al., 2010, 2013; Hickmann et al., 2015). The ADAPT maps are generated by assimilating observations when available and applying surface flux transport based on Worden and Harvey (2000) to account for differential rotation, meridional circulation, and supergranulation flows between observations. The ADAPT model generates 12 realizations of the photospheric magnetic field to represent the variable state of the Sun outside of the observed field of view. However, since the model nearside data is strongly dependent on the observations directly assimilated into the models, the difference in the magnetic field on the Earth-facing hemisphere in the 12 realizations is quite small. Therefore for simplicity, SIFT currently uses only the first realization of ADAPT to generate the magnetic sums.

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The ADAPT sequence used in this study assimilates line-of-sight magnetograms from the Kitt Peak Vacuum Telescope (KPVT; Jones et al., 1992) and Vector Spectromagnetograph (VSM; Henney et al., 2009). For this paper, the VSM magnetograms used as input to ADAPT were reprocessed with improved calibration and new bias and scaling updates, as compared to the original VSM data used in Henney2012 and Henney2015. The recalibration resulted in changes depending on center-to-limb variation and field strength. These ground-based observations were obtained at irregular times, sometimes with many days between observations. For the model and observation comparison in this study, we applied a cubic spline interpolation to the TIMED/SEE EUV and Mg II daily indices to sample these series only when new data was assimilated into ADAPT.

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## 4 EUV Nowcasts

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### 4.1 SIFT: Solar Indices Forecasting Tool

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The SIFT model uses empirical linear relationships to nowcast and forecast solar activity proxies and irradiance from photospheric magnetic fields. The fundamental assumption is that the magnetic field on the Earth-facing hemisphere of the Sun determines the observed solar irradiance. Following Henney2012 and Henney2015, the Earth-facing magnetic field in the ADAPT maps is summed into two bins corresponding to plage ( $20 \text{ G} < B_r < 150 \text{ G}$ ),  $S_P$ , and active regions ( $150 \text{ G} \leq B_r$ ),  $S_A$ . Although Henney2012 and Henney2015 started the plage bin at 25 G, we chose 20 G to remain consistent with the current SIFT implementation. The difference is also negligible to model performance. As outlined in Henney2012, the two sums are calculated as

$$S_P = \frac{1}{\sum \omega_\theta} \sum_{20\text{G} < |B_r|}^{|B_r| < 150\text{G}} |B_r| \omega_\theta \quad (1)$$

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and

$$S_A = \frac{1}{\sum \omega_\theta} \sum_{|B_r| \geq 150\text{G}} |B_r| \omega_\theta, \quad (2)$$

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where  $B_r$  is the radial magnetic field and  $\omega_\theta$  is an area weighting to account for the unequal pixel areas in the plate carée ADAPT map (180 latitude pixels by 360 longitude pixels). All of the sums are over only the Earth-facing pixels. An example ADAPT global magnetic map, generated with VSM magnetograms, is illustrated in Figure 2, where the Earth-facing side of the sun is delineated by the white box and the regions with plage and active region fields are highlighted in red and blue, respectively. We then use linear regression to determine the coefficients for a model of the following form:

$$I_{model}^n = m_0^n + m_1^n S_P + m_2^n S_A \quad (3)$$

173 where  $n$  is the solar index or irradiance band number modeled and  $m_0$ ,  $m_1$ , and  $m_2$  are  
 174 best fit coefficients. In Henney2012 and Henney2015 these models were trained indepen-  
 175 dently for nowcasts and forecasts out to seven days. In this work, we create only now-  
 176 cast models, although the procedures described below should work equally well for fore-  
 177 casts.

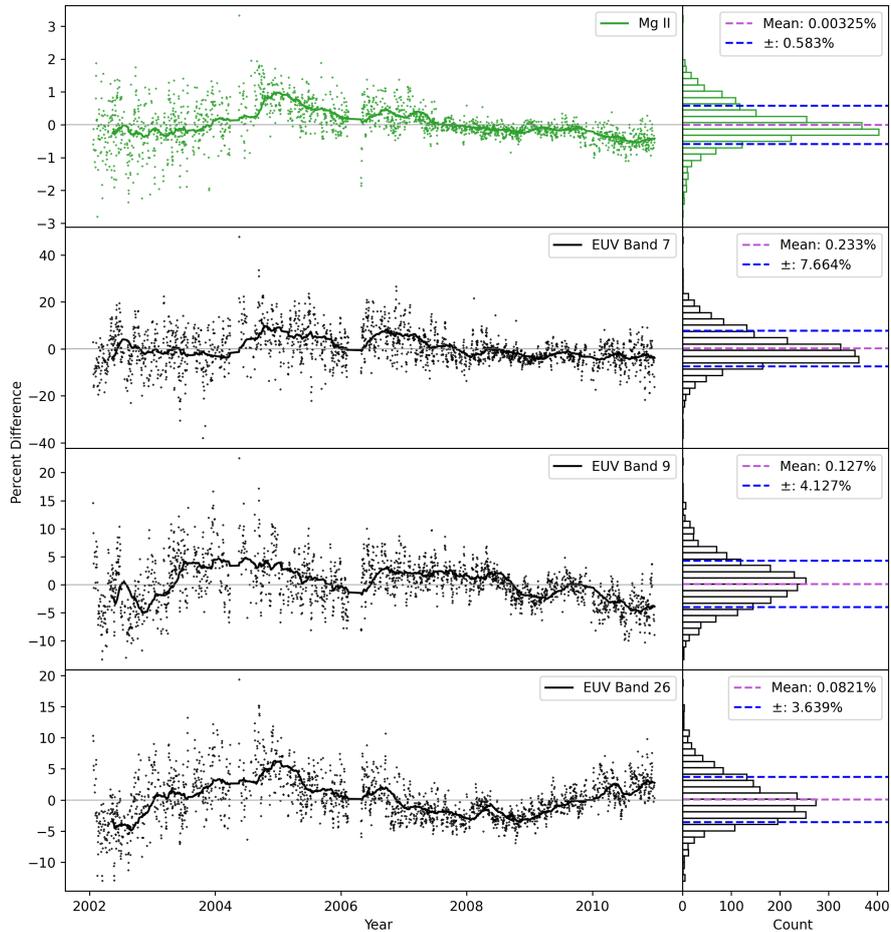
## 178 4.2 Nowcasting the Mg II Index and EUV Irradiance

179 Using equation 3, independent models are generated for Mg II and each of the 37  
 180 EUV bands using the entire 9-year data set. Timeseries of the magnetic sums, Mg II ob-  
 181 servations and model, and three EUV bands of interest observations and model are shown  
 182 in Figure 1. Since it is impractical to display all 37 EUV bands, we chose to display Band  
 183 7 (15.5 - 22.4 nm) for its strong coronal lines, Band 9 (29.0 - 32.0 nm) which contains  
 184 the strong He II 304 Å emission line, and Band 26 (121.6 nm) which is the Lyman- $\alpha$  line.  
 185 Consistent with the findings in Henney2012 and Henney2015, both the Mg II and EUV  
 186 time series have similar variability to the magnetic sums over all observed levels of so-  
 187 lar activity. The simple multiple linear regression Mg II model reproduces the observed  
 188 Mg II well with a Pearson correlation coefficient of 0.982. The correlation of the observed  
 189 and modeled EUV Band 7 is 0.978, Band 9 is 0.978, and Band 26 is 0.977. The corre-  
 190 lations of all the EUV bands is given in Table 1. Note that the  $r(I_{model}^n)$  values in Ta-  
 191 ble 1 slightly differ from Henney2012 and Henney2015. Since we chose to interpolate the  
 192 Mg II and EUV timeseries to when new data was assimilated into ADAPT maps and  
 193 the VSM magnetograms were recalibrated by NSO since Henney2012 and Henney2015,  
 194 some variation in our model correlation values are expected. In general, the EUV bands  
 195 perform similarly well, although there are some with notably lower correlation coefficients.  
 196 Band 25, which has the lowest correlation of the 37 bands, is just blue-ward of Lyman  
 197  $\alpha$  and the filter to ensure EGS does not saturate makes measuring this spectral range  
 198 difficult (Woods et al., 2005). Meanwhile, Band 1 with the second worst correlation con-  
 199 tains the highly-variable soft X-ray (SXR) that is particularly sensitive to solar flares.  
 200 All the other EUV bands have a Pearson correlation better than 0.9.

201 The difference between the models and observed values in the various bands are  
 202 not random in time. Figure 3 shows both the daily (points) and long-term, 81-day trail-  
 203 ing running average, trend (line) of the difference between the observed and modeled Mg  
 204 II (top) and EUV Bands 7, 9, and 26. These time series demonstrate the long-term devi-  
 205 ation of the models from observations (which are small) are temporally correlated over  
 206 the nine-year period displayed in Figure 3. The daily differences are typically largest dur-  
 207 ing maximum solar magnetic activity when the irradiance is most variable. This is ex-  
 208 pected because both the magnetic sums and Mg II vary more during solar maximum than  
 209 solar minimum, so the same relative difference results in larger absolute differences. In-  
 210 terestingly, the time-dependent long-term bias in all four of these models is largest at  
 211 the intermediate activity levels during the decline of Solar Cycle 23.

## 212 4.3 EUV Nowcast Correction

213 The simple linear regression models applied in SIFT have a number of known lim-  
 214 itations. Most fundamentally, while the magnetic field is responsible for solar activity  
 215 (Petrie et al., 2021), the solar atmospheric response to photospheric magnetic fields is  
 216 dynamic and non-linear (e.g., Tiwari et al., 2017), and may not always be well represented  
 217 by a static model. Furthermore, solar EUV irradiance is often concentrated in active re-  
 218 gions (depending on wavelength, see e.g., Kazachenko & Hudson, 2020), and the spatial  
 219 information in the magnetic field is not included in the current SIFT modeling. Finally,  
 220 the ADAPT maps that drive SIFT do not assimilate data near the limb (see Hickmann  
 221 et al., 2015; Barnes et al., 2023) to reduce the introduction of artifacts from the line-of-  
 222 sight magnetic field measurements that would otherwise be assumed to be radial (see,



**Figure 3.** The daily (points) and 81-day running average difference between the modeled and observed Mg II (top) and EUV Bands 7, 9, and 26 plotted as a percent difference from the observed value. To the right of each time series is a histogram indicating the distribution of daily offsets over the entire data set. The mean (purple) and standard deviation (blue) for each band’s offsets are included with each histogram. Notice that the Mg II and EUV offsets track each other well throughout the solar cycle.

223 e.g., Harvey et al., 2007). This leads to a  $\sim$ two-day delay between when a flux concen-  
 224 tration becomes visible on the Earth-facing solar hemisphere and when it is first assim-  
 225 ilated into ADAPT.

226 To mitigate signal delay issues, Henney2015 implemented a 0-day offset correction  
 227 for the SIFT forecast models. For each set of daily forecasts, the difference between the  
 228 model nowcast and associated observation was applied as a constant correction factor  
 229 to all forecasts made on that day. The 0-day offset technique compensates for local in-  
 230 adequacies in the model while still utilizing the full-Sun nature of ADAPT that enables

231 forecasting. However, the technique applied by Henney2015 requires an observation in  
 232 each band of the model to determine and apply the corresponding correction. Currently,  
 233 with aging EUV irradiance observatories and limited EUV spectral coverage (P. Cham-  
 234 berlin et al., 2023), selected bands of EUV observations are not reliably available. It is  
 235 therefore valuable to apply a similar correction without the need for daily measurements  
 236 in each EUV band.

237 The difference between the modeled and observed Mg II (top) and EUV Bands 7,  
 238 9, and 26 in Figure 3 appear to correlate somewhat over a solar cycle timescale. This  
 239 suggests that the errors in the EUV band models could be reduced by applying a time-  
 240 dependent correction to each band by using the difference between the daily observed  
 241 and modeled Mg II. We create this correction model by linearly correlating the daily model-  
 242 observation difference in Mg II with each of the EUV bands such that

$$I_{model}^n - I_{observed}^n = m_3^n \left( I_{model}^{Mg II} - I_{observed}^{Mg II} \right) = m_3^n C \quad (4)$$

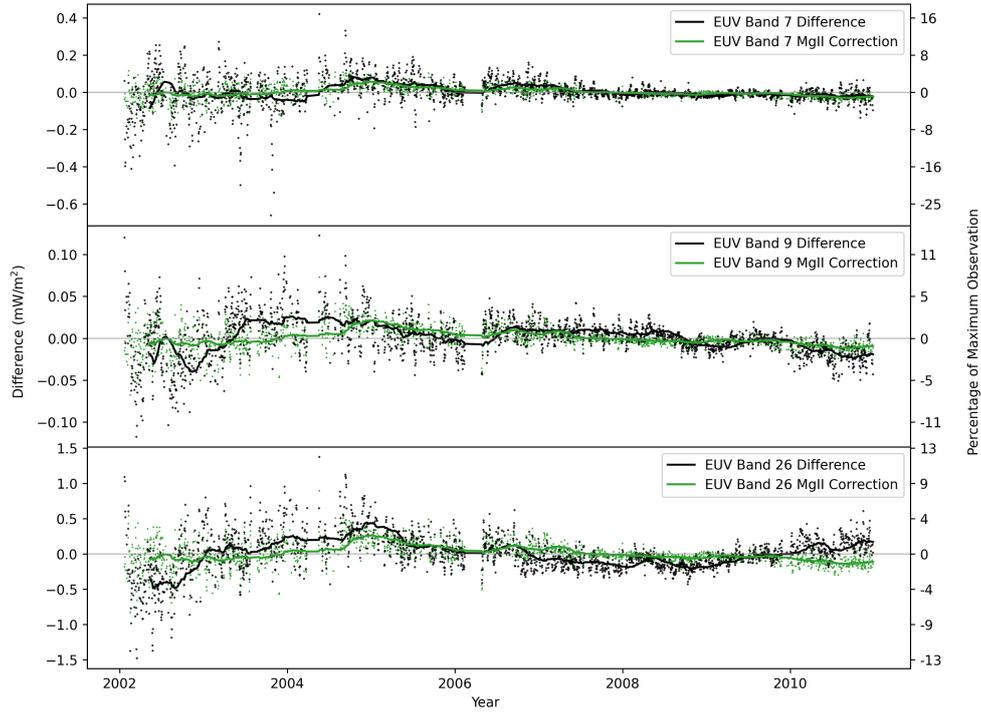
243 and then applying this correction term to equation 3, we get the following

$$I_{corrected}^n = m_0^n + m_1^n S_P + m_2^n S_A - m_3^n C, \quad (5)$$

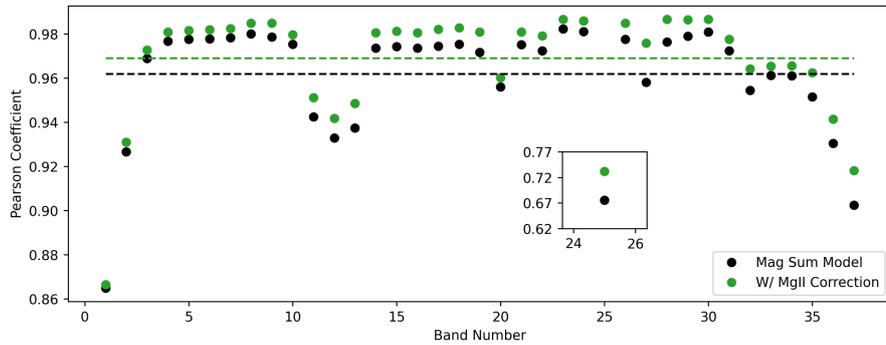
244 which yields an Mg II-corrected multiple linear regression for each band. We chose to  
 245 model the Mg II correction term with only one coefficient, vice a multi-coefficient lin-  
 246 ear regression, because additional constants were several orders of magnitude smaller than  
 247 the  $m_3$  correction coefficient, as well as  $m_0$ ,  $m_1$ , and  $m_2$ . Therefore, additional coeffi-  
 248 cients had no effect on model performance or improvement. The coefficients for these  
 249 models are shown in Table A1 in the appendix. The Mg II correction term on EUV Bands  
 250 7 ( $m_3^7 C$ ), 9 ( $m_3^9 C$ ), and 26 ( $m_3^{26} C$ ) are plotted (green) in Figure 4 along with the origi-  
 251 nal model-observation difference (black) from Figure 3. If these points (and lines) over-  
 252 lapped perfectly then the Mg II correction term would allow perfect nowcasting of the  
 253 EUV band, and anywhere that the two have opposite sign indicates when the Mg II cor-  
 254 rection harms the nowcast. This correction term does not provide improvements at all  
 255 times, however, on average the model-observation difference is reduced with this correc-  
 256 tion.

257 Improved nowcasting is found to be consistent across all 37 bands as reported in  
 258 Table 1 and displayed in Figure 5. This shows the Pearson correlation coefficient between  
 259 both the original and corrected models and the observations of all bands over the entire  
 260 period studied. The Mg II correction yields improved correlations across all bands, with  
 261 particular improvement in Band 25 which has the worst correlation. The  $m_1/m_2$  val-  
 262 ues (see Table A1) also demonstrate why a Mg II correction term is suitable for these  
 263 models. The  $m_1/m_2$  Mg II and all of EUV band  $m_1/m_2$  values, except for Band 1, are  
 264 greater than 1, demonstrating that there is a larger dependence on plage regions for the  
 265 Mg II and the EUV bands. Henney2015 found that  $m_1/m_2$  for  $F_{10.7}$  is less than 1, in-  
 266 dicated that it is more strongly dependent on active regions. This indicates that the Mg  
 267 II proxy, rather than the active-region dependent  $F_{10.7}$ , is more consistent with the be-  
 268 havior of the solar EUV spectrum.

269 Additionally, Figure 6 exhibits the long-term variability of the EUV Band 7, 9, and  
 270 26 models before (grey) and after (green) applying the Mg II offset correction. This plot  
 271 shows that the error between the observations and model are typically smaller (i.e., the  
 272 distribution shifts closer to 0) and the range in variation decreases (i.e., the vertical range  
 273 of each box is smaller). Interestingly, the overall trend of the model-observation differ-  
 274 ence over the solar cycle does not change, with the models tending to predict more ir-  
 275 radiance than observed during the decline of the solar cycle (2003-2007) and less dur-  
 276 ing the maximum (2002). Warren et al. (2021) identify a similar trend in their models  
 277 which they attribute to discrepancies in the weak magnetic fields ( $B_r < 80$  G) between  
 278 the full-Sun magnetic maps and the original observed magnetograms. We identify two  
 279 additional possible explanations for this effect. It could indicate that the conversion of



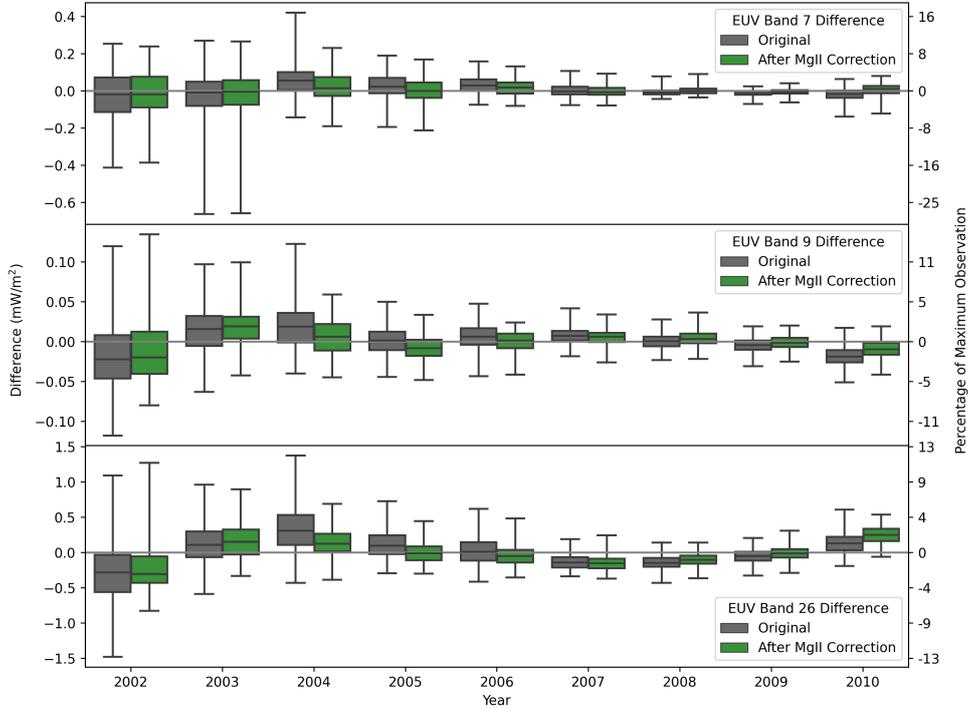
**Figure 4.** Plots of the difference between observed and modeled Bands 7, 9, and 26 EUV values, and the EUV difference models. The difference models were developed by comparing EUV to Mg II offset values.



**Figure 5.** Pearson correlation coefficients which compare the relationship between each observed EUV spectral band and the nowcast models with (green) and without (black) a Mg II correction. Since Band 25 did not perform as well compared to the other bands, its Pearson coefficients are included on a separate, sub-graph to enhance the results of the other bands. The horizontal dashed lines indicate the average Pearson correlation coefficient across all bands (except band 25).

280 magnetic energy into plasma heating in the solar atmosphere is slightly more efficient  
 281 during the rising phase and solar maximum (leading to more emission than predicted)  
 282 than the declining phase (with less emission than predicted). It could also be the result  
 283 of some other long-term variation in the ADAPT maps. For example, because of the de-  
 284 lay between the rotation of magnetic flux onto the Earth-facing hemisphere and the in-  
 285 corporation of this flux into ADAPT, the ADAPT maps in general under-represent the  
 286 magnetic flux on the Earth-facing hemisphere. This effect will be stronger during the  
 287 rising phase and maximum of the solar cycle when flux emergence is greatest and there-  
 288 fore more flux appears on the farside and is not included in ADAPT until it rotates into  
 289 the data assimilation window. A more detailed study is needed to better understand the  
 290 source of this long-term residual trend (e.g., adding another solar cycle of data analy-  
 291 sis and/or using different magnetograph inputs, e.g., SDO/HMI and NSO/GONG).

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**Figure 6.** Box and whisker plots for EUV spectral Bands 7, 9, and 26, highlighting the distributions of the difference between the models and observations during the study period. The box indicates the extent of the 25% and 75% quartiles and the line through the box indicates the distribution median over one year of data. The whiskers (i.e., the vertical lines) indicate the minimum and maximum. The distributions including the Mg II correction do not strictly improve, however the improvements (e.g. 2004) are much more significant than the occasional times when the distributions worsen. Similar figures for all 37 bands are available at Kniezewski et al. (2023).

Band (n)	Range (nm)	r(Mg II)	$r(I_{model}^n)$	$r(I_{model}^n$ with offset)
1	0.05-0.4	0.845	0.865	0.866
2	0.4-0.8	0.920	0.927	0.931
3	0.8-1.8	0.965	0.969	0.973
4	1.8-3.2	0.975	0.976	0.981
5	3.2-7.0	0.976	0.977	0.982
6	7.0-15.5	0.976	0.977	0.982
7	15.5-22.4	0.977	0.978	0.983
8	22.4-29.0	0.980	0.979	0.985
9	29.0-32.0	0.982	0.978	0.985
10	32.0-54.0	0.975	0.974	0.980
11	54.0-65.0	0.948	0.942	0.951
12	65.0-79.8 (low)	0.937	0.933	0.942
13	65.0-79.8 (high)	0.945	0.937	0.948
14	79.8-91.3 (low)	0.978	0.974	0.981
15	79.8-91.3 (middle)	0.978	0.974	0.982
16	79.8-91.3 (high)	0.978	0.974	0.981
17	91.3-97.5 (low)	0.980	0.974	0.982
18	91.3-97.5 (middle)	0.981	0.975	0.983
19	91.3-97.5 (high)	0.979	0.971	0.981
20	97.5-98.7	0.955	0.957	0.961
21	98.7-102.7	0.978	0.975	0.981
22	102.7-105.0	0.977	0.972	0.979
23	105.0-110.0	0.982	0.982	0.987
24	110.0-115.0	0.982	0.981	0.986
25	115.0-120.0	0.714	0.671	0.736
26	121.6 (Lyman $\alpha$ )	0.981	0.977	0.985
27	120.0-125.0	0.975	0.956	0.976
28	125.0-130.0	0.985	0.976	0.987
29	130.0-135.0	0.985	0.979	0.987
30	135.0-140.0	0.983	0.981	0.987
31	140.0-145.0	0.974	0.973	0.978
32	145.0-150.0	0.963	0.955	0.965
33	150.0-155.0	0.961	0.962	0.966
34	155.0-160.0	0.962	0.962	0.966
35	160.0-165.0	0.962	0.951	0.963
36	165.0-170.0	0.941	0.930	0.942
37	170.0-175.0	0.918	0.902	0.918

**Table 1.** EUV irradiance bands and associated correlation coefficients.  $r(\text{Mg II})$  is the correlation between the modeled band irradiance and the observed Mg II.  $r(I_{model}^n)$  is the correlation between the modeled band irradiance and the observed band irradiance, and  $r(I_{model}^n$  with offset) includes the Mg II correction term (i.e. equation 5) .

## 5 Summary

This study builds on the work of the SIFT model, outlined in Henney2012 and Henney2015, that demonstrated the ability of ADAPT global photospheric magnetic maps to drive irradiance nowcasts and forecasts. The original SIFT EUV forecasts benefited greatly from daily calibration of the models to the observed irradiance which corrected short-term errors between the models and observations. However, for periods without

299 real-time calibrated EUV spectral measurements, the original correction technique is not  
 300 an option for real-time predictions.

301 In the study presented here, we develop an alternative implementation of daily cor-  
 302 rections that does not rely on current EUV irradiance observations. Instead, the daily  
 303 model and observation is regularly measured for a proxy, in this case the Mg II index.  
 304 Then, that Mg II index nowcast offset is scaled and a corresponding correction is applied  
 305 to each EUV irradiance band independently. Applying this correction term to simple mul-  
 306 tiple linear regression models yields improved nowcasts across the entire spectral range,  
 307 with the average Pearson correlation coefficient increasing from 0.962 to 0.969 as rep-  
 308 resented by the horizontal dashed lines in Figure 5. In this work we use the science-quality  
 309 Bremen Mg II dataset to demonstrate the viability of this technique, but this method  
 310 can be applied using existing operationally available data products such as the Geosta-  
 311 tionary Operational Environmental Satellite (GOES) Extreme Ultraviolet and X-ray Sen-  
 312 sors (EXIS) Extreme Ultraviolet Sensor (EUVS; Eparvier et al., 2009) Mg II dataset which  
 313 began in 2017. This technique can also easily be extended to forecasting EUV bands to  
 314 drive terrestrial atmospheric models. It can also be applied as a post-processing term  
 315 to more complex machine learning techniques where it would serve the same function  
 316 as a daily correction to the model output. This kind of solar proxy-modeling using deep  
 317 learning and neural networks has recently shown promising results (e.g, see Stevenson  
 318 et al., 2022; Daniell & Mehta, 2023).

319 We also identify a solar-cycle trend in the regression models that typically under-  
 320 predict the irradiance during solar maximum and over-predict the irradiance during the  
 321 declining phase. This could indicate deficiencies in the ADAPT maps driving these ir-  
 322 radiance nowcasts or an underlying nonlinear conversion of photospheric magnetic en-  
 323 ergy and chromospheric and coronal heating (e.g., not captured with the simple linear  
 324 regression models applied here). Future work is needed to better understand the source  
 325 of the model and observation residuals over the solar cycle such as analyzing an addi-  
 326 tional solar cycle and using different magnetograph inputs.

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 337 fense (DoD) or of the United States Air Force.

### 338 **Open Research**

#### 339 **Data Availability Statement**

340 The Mg II composite index is provided by the University of Bremen at [http://](http://www.iup.uni-bremen.de/gome/solar/MgII_composite.dat)  
 341 [www.iup.uni-bremen.de/gome/solar/MgII\\_composite.dat](http://www.iup.uni-bremen.de/gome/solar/MgII_composite.dat). The Mg II index data used  
 342 in this study along with figures for all 37 EUV bands and the scripts used to create and  
 343 visualize the SIFT models are available through Zenodo at Kniezewski et al. (2023). The  
 344 solar magnetic sums based on ADAPT are available through Zenodo at Henney et al.  
 345 (2023). The EUV irradiances in the 37 bands are provided through Zenodo at R. A. Hock  
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**Appendix A**

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Coefficients for the SIFT linear regression models defined in equation 5 are given in Table A1.

Band (n)	$m_0$	$m_1$	$m_2$	$m_3$	$m_1/m_2$
Mg II	$1.494 \times 10^{-1}$	$2.044 \times 10^{-3}$	$5.321 \times 10^{-4}$	N/A	3.841
1	$-6.375 \times 10^{-9}$	$1.492 \times 10^{-8}$	$2.068 \times 10^{-8}$	$3.620 \times 10^{-6}$	0.721
2	$-1.811 \times 10^{-7}$	$6.190 \times 10^{-7}$	$5.728 \times 10^{-7}$	$2.065 \times 10^{-4}$	1.081
3	$-1.393 \times 10^{-6}$	$2.193 \times 10^{-5}$	$1.352 \times 10^{-5}$	$6.112 \times 10^{-3}$	1.622
4	$1.449 \times 10^{-5}$	$1.095 \times 10^{-5}$	$5.350 \times 10^{-6}$	$2.969 \times 10^{-3}$	2.047
5	$5.734 \times 10^{-5}$	$1.891 \times 10^{-5}$	$9.077 \times 10^{-6}$	$5.115 \times 10^{-3}$	2.083
6	$1.054 \times 10^{-4}$	$4.429 \times 10^{-5}$	$2.129 \times 10^{-5}$	$1.212 \times 10^{-2}$	2.080
7	$3.860 \times 10^{-4}$	$1.370 \times 10^{-4}$	$6.407 \times 10^{-5}$	$3.374 \times 10^{-2}$	2.138
8	$9.538 \times 10^{-5}$	$3.947 \times 10^{-5}$	$3.314 \times 10^{-6}$	$9.787 \times 10^{-3}$	11.910
9	$3.916 \times 10^{-4}$	$5.032 \times 10^{-5}$	$8.284 \times 10^{-6}$	$1.453 \times 10^{-2}$	6.074
10	$2.461 \times 10^{-4}$	$6.129 \times 10^{-5}$	$1.234 \times 10^{-5}$	$1.535 \times 10^{-2}$	4.968
11	$1.462 \times 10^{-4}$	$7.596 \times 10^{-6}$	$4.128 \times 10^{-6}$	$2.991 \times 10^{-3}$	1.840
12	$5.954 \times 10^{-5}$	$1.824 \times 10^{-6}$	$1.226 \times 10^{-6}$	$7.773 \times 10^{-4}$	1.488
13	$3.210 \times 10^{-5}$	$1.139 \times 10^{-6}$	$7.029 \times 10^{-7}$	$5.338 \times 10^{-4}$	1.620
14	$4.117 \times 10^{-5}$	$4.389 \times 10^{-6}$	$7.483 \times 10^{-7}$	$1.281 \times 10^{-3}$	5.866
15	$1.148 \times 10^{-4}$	$1.461 \times 10^{-5}$	$2.240 \times 10^{-6}$	$4.173 \times 10^{-3}$	6.525
16	$5.311 \times 10^{-5}$	$5.979 \times 10^{-6}$	$1.019 \times 10^{-6}$	$1.727 \times 10^{-3}$	5.868
17	$1.776 \times 10^{-5}$	$1.731 \times 10^{-6}$	$3.693 \times 10^{-7}$	$5.382 \times 10^{-4}$	4.687
18	$4.001 \times 10^{-5}$	$3.727 \times 10^{-6}$	$9.899 \times 10^{-7}$	$1.182 \times 10^{-3}$	3.765
19	$1.720 \times 10^{-5}$	$2.195 \times 10^{-6}$	$3.766 \times 10^{-7}$	$7.399 \times 10^{-4}$	5.831
20	$5.417 \times 10^{-5}$	$1.105 \times 10^{-5}$	$1.422 \times 10^{-6}$	$2.401 \times 10^{-3}$	7.769
21	$8.049 \times 10^{-5}$	$1.196 \times 10^{-5}$	$2.418 \times 10^{-6}$	$3.241 \times 10^{-3}$	4.945
22	$8.414 \times 10^{-5}$	$1.081 \times 10^{-5}$	$2.200 \times 10^{-6}$	$3.208 \times 10^{-3}$	4.913
23	$7.619 \times 10^{-5}$	$6.424 \times 10^{-6}$	$1.795 \times 10^{-6}$	$1.560 \times 10^{-3}$	3.579
24	$6.830 \times 10^{-5}$	$5.224 \times 10^{-6}$	$1.423 \times 10^{-6}$	$1.358 \times 10^{-3}$	3.671
25	$1.626 \times 10^{-4}$	$2.925 \times 10^{-6}$	$2.125 \times 10^{-6}$	$4.095 \times 10^{-3}$	1.377
26	$5.444 \times 10^{-3}$	$6.080 \times 10^{-4}$	$3.115 \times 10^{-5}$	$1.760 \times 10^{-1}$	19.519
27	$8.198 \times 10^{-4}$	$6.062 \times 10^{-5}$	$8.048 \times 10^{-6}$	$2.913 \times 10^{-2}$	7.533
28	$1.978 \times 10^{-5}$	$1.289 \times 10^{-6}$	$2.281 \times 10^{-7}$	$4.654 \times 10^{-4}$	5.652
29	$3.588 \times 10^{-4}$	$1.945 \times 10^{-5}$	$5.450 \times 10^{-6}$	$6.208 \times 10^{-3}$	3.569
30	$1.812 \times 10^{-4}$	$8.200 \times 10^{-6}$	$2.413 \times 10^{-6}$	$2.307 \times 10^{-3}$	3.398
31	$2.249 \times 10^{-4}$	$7.655 \times 10^{-6}$	$2.082 \times 10^{-6}$	$1.977 \times 10^{-3}$	3.677
32	$3.242 \times 10^{-4}$	$7.213 \times 10^{-6}$	$2.338 \times 10^{-6}$	$2.665 \times 10^{-3}$	3.085
33	$5.609 \times 10^{-4}$	$1.502 \times 10^{-5}$	$5.474 \times 10^{-6}$	$3.504 \times 10^{-3}$	2.744
34	$7.857 \times 10^{-3}$	$1.711 \times 10^{-5}$	$4.471 \times 10^{-6}$	$4.153 \times 10^{-3}$	3.828
35	$1.114 \times 10^{-3}$	$1.854 \times 10^{-5}$	$5.369 \times 10^{-6}$	$7.270 \times 10^{-3}$	3.454
36	$2.053 \times 10^{-3}$	$2.889 \times 10^{-5}$	$7.706 \times 10^{-6}$	$1.113 \times 10^{-2}$	3.749
37	$3.391 \times 10^{-3}$	$4.590 \times 10^{-5}$	$7.587 \times 10^{-6}$	$2.041 \times 10^{-2}$	6.050

**Table A1.** EUV model coefficients, including the difference model coefficients using Mg II.

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